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Article

# Electron-Phonon Interaction in Non-Stoichiometric $\text{Bi}_2\text{Sr}_2\text{Ca}\text{Cu}_2\text{O}_{8+\delta}$ Superconductor from the Diffuse Elastic Helium Atom Scattering

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**Abstract:** Previously helium atom scattering (HAS) has been shown to probe the electron-phonon interaction at conducting crystal surfaces via the temperature dependence of the specular peak intensity. This method is now extended to non-stoichiometric superconductors. The electron-phonon interaction, as expressed by the mass-enhancement factor  $\lambda$ , is derived from the temperature dependence of the diffuse elastic scattering intensity, which specifically depends on the non-stoichiometric component responsible for superconductivity. The measured value of the mass-enhancement factor for  $\text{Bi}_2\text{Sr}_2\text{Ca}\text{Cu}_2\text{O}_{8+\delta}$  at the optimal doping  $\delta = 0.16$  is  $\lambda = 0.55 \pm 0.08$  in good agreement with values of  $\lambda$  recently estimated with other methods. This confirms the relevant role of electron-phonon interaction also in high-temperature non-stoichiometric cuprate superconductors.

**Keywords:** superconductivity; electron-phonon coupling; cuprates

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## 1. Introduction

The layered compound  $\text{Bi}_2\text{Sr}_2\text{Ca}\text{Cu}_2\text{O}_{8+\delta}$  (Bi-2212) owes its hole-doping and high-temperature superconductivity to a deviation from stoichiometry, spontaneously produced in the growth process [1] and consisting in an excess  $\delta$  of oxygen ions, essentially concentrated in the Bi-O layers. Superconductivity is observed for roughly  $0.09 < \delta < 0.29$ , with a maximum  $T_c = 95$  K at about  $\delta = 0.17$  [2]. The doping with additional oxygen atoms, besides injecting free holes and producing static deformations of the stoichiometric lattice, also affects the electronic and phonon structure by introducing localized and resonance states, which may eventually play a role in the superconducting properties activated by the doping itself [3]. A natural question is whether also the electron-phonon interaction is significantly affected by doping. High- $T_c$  superconductors, notably Bi-2212, do not explicitly rely on the electron-phonon interaction like traditional BCS superconductors, although the electron-phonon interaction has been shown to largely contribute, with a mass-enhancement factor  $\lambda \approx 0.6$  at the optimal doping [4,5]. Recently, O'Mahony *et al.* [6] have provided experimental evidence in favour of Anderson superexchange [7] as the dominant pairing mechanism in high- $T_c$  superconductivity in Bi-2212.

In the last decade it has been demonstrated that He atom scattering (HAS) from conducting crystal surfaces permits a direct determination of the electron-phonon interaction, as represented by the mass-enhancement factor  $\lambda$ , from measurements of the temperature dependence of the Debye-Waller (DW) exponent, as derived from the elastic specular or diffraction peak intensities [8,9]. In inelastic HAS time-of-flight (TOF) spectra, currently used to measure the dispersion curves of surface



phonons [10], there is always an additional peak at zero-energy transfer, called the diffuse elastic (DE) peak. This peak originates from the elastic scattering from surface defects, or, in general, from any feature which perturbs the surface periodicity. Thus, the contribution from static and dynamic effects of doping to the electron-phonon interaction in doped superconductors such as Bi-2212, can be extracted from the temperature dependence of the HAS DE peak intensities.

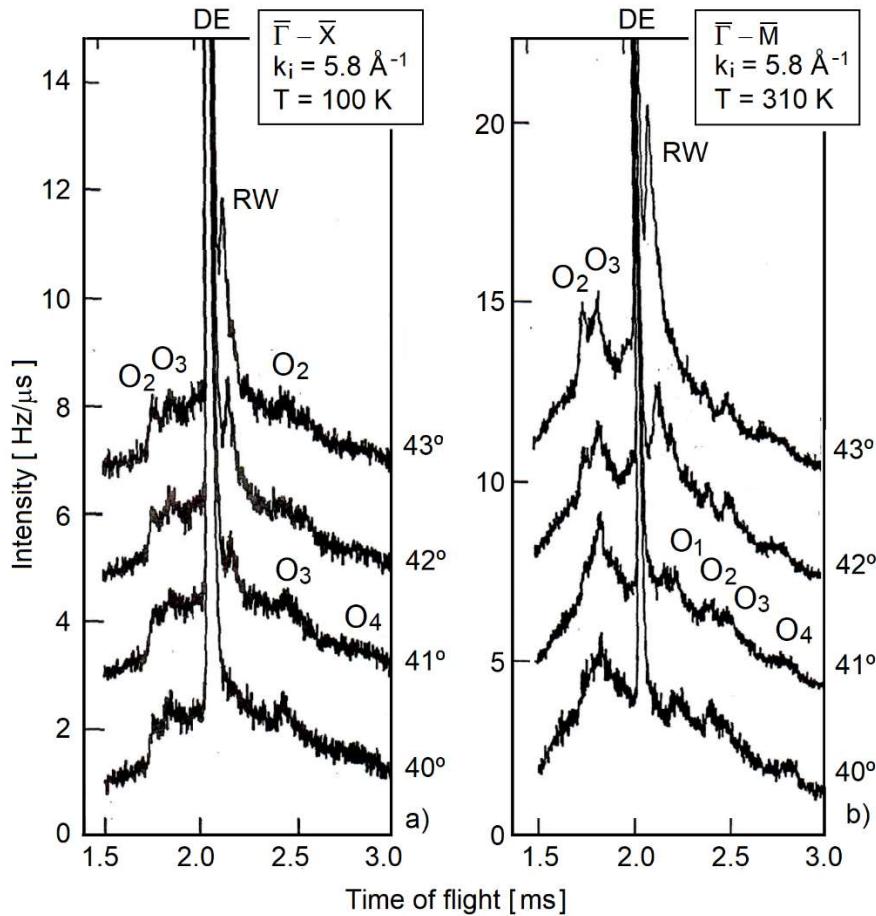
Here we report on HAS TOF measurements from Bi-2212 at optimal doping. These provide, besides a set of surface phonon dispersion curves in the range of energy below 10 meV [13], the DE peak intensities at two different temperatures 100 and 310 K. The electron-phonon interaction  $\lambda = 0.55 \pm 0.08$  derived for Bi-2212 from two different temperatures at about the optimal doping is in good agreement with what is currently known from other methods. This supports the present conjecture that also the DE peak can be used to extract information on the electron-phonon interaction at conductive surfaces where the conductivity is essentially induced by doping.

It is important to note that in the specific case of high-T<sub>c</sub> cuprates, where the unit cell includes several atomic layers and superconductivity is essentially associated with copper oxide layers, the critical temperature does not decrease in ultrathin films, down to a single cell thickness corresponding to one formula [11]. In this regard, bulk Bi<sub>2</sub>Sr<sub>2</sub>CaCu<sub>2</sub>O<sub>8+δ</sub> behaves as a genuine 2D superconductor, which is equivalent to saying that HAS-DE data are providing in this case information on the actual  $\lambda$  of the bulk material.

## 2. He-Atom Scattering Time-of-Flight Data

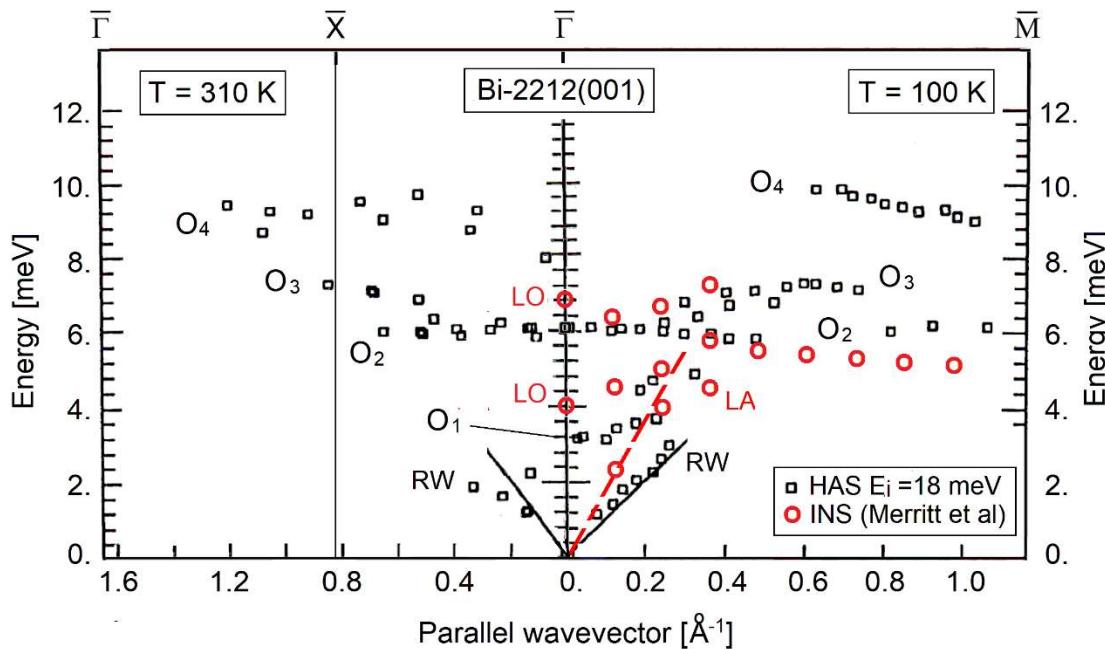
In previous HAS diffraction experiments [12,13] the structure of the Bi-O(001) surface of Bi<sub>2</sub>Sr<sub>2</sub>CaCu<sub>2</sub>O<sub>8+δ</sub>, with  $\delta = 0.16$  at about the optimal doping and corresponding to  $T_c \sim 91$  K, revealed, at temperatures well above  $T_c$ , an incommensurate striped superstructure in the  $\langle 1\bar{1}0 \rangle$  direction with a rectangular supercell approximated to  $(\sqrt{2}a, 5\sqrt{2}a)R45^\circ$ , as compared to the ideal square unit cell of edges  $(a, a)$ , where  $a = 3.814$  Å is the Bi-O distance [13]. This superstructure, detected by HAS diffraction in the reciprocal space, has been later clearly imaged by Zeljkovic *et al* [14] with scanning tunnelling microscopy (STM) at increasing critical temperatures up to the maximum  $T_c \sim 91$  K. The analysis by Zeljkovic *et al* at the optimal oxygen doping of ~4% per CuO<sub>2</sub> reveals random interstitials in the Bi-O plane, and similarly other interstitials at ~2.5% per CuO<sub>2</sub> in the Sr-O plane (type-B and type-A oxygen, respectively [15]). The association of superconducting properties to the inhomogeneities produced by non-stoichiometric oxygen also supports the present derivation of the electron-phonon interaction from the measured temperature dependence of the HAS DE peak.

Figure 1 displays the TOF spectra in the planar 90° scattering-angle configuration at four different incident angles ( $\theta = 40^\circ$  to  $43^\circ$ ) for the same incident He-atom momentum  $k_i = 5.8$  Å<sup>-1</sup> (incident energy  $E_i = 18$  meV) and for surface temperatures of 100 K (panel (a)) and 310 K (panel (b)) [12,13]. Note that the two sets of measurements have been performed along different directions,  $\langle 110 \rangle$  and  $\langle 100 \rangle$ , i.e.,  $\bar{\Gamma}\bar{X}$  and  $\bar{\Gamma}\bar{M}$ , respectively. Because of the intrinsic isotropy of the surface, both directions can be used for determining the temperature dependence of the DE peak. In both TOF spectra the largest off-scale peak is the diffuse elastic scattering from defects, labelled DE. The inelastic peaks, labelled RW (Rayleigh wave), or O<sub>1</sub>, O<sub>2</sub>, O<sub>3</sub>, O<sub>4</sub> are, in this order, much less intense. Recently inelastic neutron scattering (INS) has been used by Merritt *et al* [18] to measure the low-energy longitudinal acoustic (LA) and two longitudinal optical (LO) bulk modes of optimally doped Bi<sub>2</sub>Sr<sub>2</sub>CaCu<sub>2</sub>O<sub>8+δ</sub>.



**Figure 1.** HAS time-of-flight spectra from the Bi-O(001) surface of  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ , at about the optimal doping. The measurements have been performed at different incident angles (indicated on the right side of the spectra) with a  $90^\circ$  planar scattering geometry and incident He atom momentum of  $5.8 \text{ \AA}^{-1}$ : (a) in the  $\overline{\Gamma}\overline{X}$  symmetry direction at a surface temperature  $T = 100 \text{ K}$ , and (b) in the  $\overline{\Gamma}\overline{M}$  symmetry direction and  $T = 310 \text{ K}$ . Besides the diffuse elastic (DE) and Rayleigh wave (RW) peaks, various inelastic peaks, labelled  $O_1$  to  $O_4$  and assigned to phonon creation (right side) and annihilation (left side) are observed (adapted from [12]).

Figure 2 displays the HAS dispersion curves of the surface phonons (open squares), derived from TOF spectra like those of Figure 1 and the INS data (red symbols) along the two main symmetry directions  $\bar{\Gamma}\bar{X}$  and  $\bar{\Gamma}\bar{M}$ . The dispersion curves of the lowest acoustic branch corresponding to the RW and the other low-energy surface phonon branches,  $O_1$ ,  $O_2$ ,  $O_3$  and  $O_4$ , are clearly delineated. The branches  $O_2$ ,  $O_3$  and  $O_4$  are almost dispersionless. At the zone center  $\bar{\Gamma}$  the surface modes  $O_1$ , and  $O_2$  with  $O_3$  appear to be a somewhat softened version of the two bulk LO modes, as a possible effect of surface localization. Moreover, the branches  $O_2$ ,  $O_3$  and  $O_4$  look rather similar along the two symmetry directions, also suggesting some sort of isotropy.



**Figure 2.** Low-energy phonon dispersion curves at the Bi-O(001) surface of  $\text{Bi}_2\text{Sr}_2\text{Ca}\text{Cu}_2\text{O}_{8+\delta}$  (Bi2212) with  $\delta = 0.16$  at about the optimal doping, measured with HAS by Schmicker [12] and Paltzer et al [13,16] (open squares) along two different symmetry directions and surface temperatures (cfr. Figure 1), compared to INS data by Merrit *et al* (red open circles) [18]. The apparent isotropy of the  $\text{O}_2$ ,  $\text{O}_3$  and  $\text{O}_4$  phonon branches suggests their association to the non-stoichiometric oxygen randomly distributed in the Bi-O and Sr-O planes.

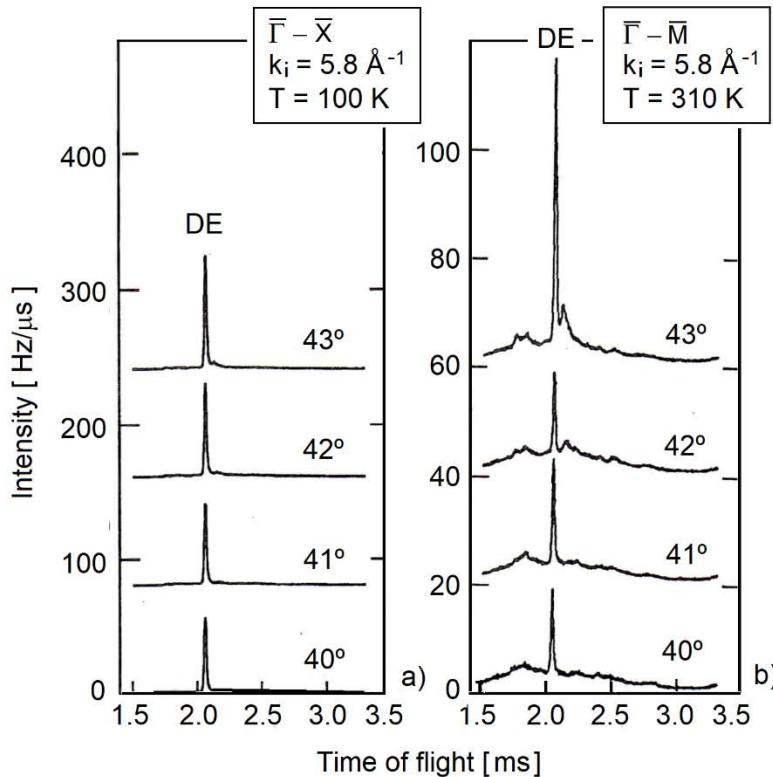
The present experimental nearly dispersionless curves for the optimally doped material are in contrast to the theoretical large frequencies and strong dispersion of the surface phonons calculated with the shell model for the stoichiometric ( $\delta = 0$ ) compound [16,17]. This suggests that the localized vibrations of random non-stoichiometric weakly-interacting oxygen atoms (as neutral acceptors) have a sufficiently high concentration and large vibrational amplitudes to exhibit flat and soft dispersion curves. This interpretation appears to be preferable to the one suggested in previous works [13,18] in which parts of the observed branches have been associated with folding effects from the stripe superstructure, despite the apparent isotropy.

### 3. Electron-Phonon Interaction from the Temperature Dependence of the Diffuse Elastic Peak

Figure 3 reproduces the TOF spectra of Figure 1 on a reduced ordinate scale (different in panels (a) and (b)), so as to show the decrease of the DE peak intensity with increasing temperature from 100 K (a) to 310 K (b) for the four different incident angles. As seen from the values reported in Table 1, the intensity decrease at  $43^\circ$  is less pronounced than for the other three incident angles. This is attributed to the close proximity to the elastic specular peak at  $45^\circ$  and its intensity tail due to the finite experimental energy resolution. The fair consistency of the decrease rates for the other three incident angles suggests to consider  $\lambda$  and its standard deviation derived from the  $40^\circ$ ,  $41^\circ$  and  $42^\circ$  data as more reliable, than those derived from averaging over all four incidence angles.

**Table 1.** HAS diffuse elastic peak intensities at different incidence angles  $\theta_i$  and corresponding logarithmic variations with temperature.

$\theta_i$ [degrees]	$I_{DE}(100 \text{ K})$ [Hz/ s]	$I_{DE}(310 \text{ K})$ [Hz/ s]	$\ln[I_{DE}(T)]$
43°	83.3	49.5	0.52
42°	68.8	15.0	1.52
41°	58.3	20.0	1.07
40°	54.5	15.5	1.25



**Figure 3.** Comparison of the diffuse elastic (DE) peak intensities shown in Figure 1 in a larger ordinate scale measured at two different surface temperatures of 100 K and 310 K for the four incident angles. Note the reduced ordinate scale compared to Figure 1 and the differences in ordinate scale for  $T = 100 \text{ K}$  (a) and  $310 \text{ K}$  (b).

The electron-phonon coupling constant (mass-enhancement factor) can be expressed as in Ref. [9], Eq. (7), by adapting it to the case of the DE elastic peak:

$$\lambda = \frac{2\pi\phi}{n_s a_c (k_{fx} - k_{iz})^2} \left| \frac{\Delta \ln I_{DE}(T)}{k_B \Delta T} \right|. \quad (1)$$

Here  $\phi = 4.85 \text{ eV}$  is the work function of Bi-2212 at 85 K [19],  $n_s = 4$  is the number of layers hosting non-stoichiometric oxygen in the first half unit cell (corresponding to one formula),  $a_c = a^2 = 14.55 \text{ \AA}^2$  the surface unit cell,  $k_{iz} = -k_i \sin \theta_i$  and  $k_{fx} = k_i \sin \theta_f$  the incident and final components of the He wavevector normal to the surface, and  $I_{DE}(T)$  is the DE peak intensity, as given in Table 1 at the two temperatures.

With these input values and by averaging over  $\theta_i = 42^\circ$  to  $40^\circ$ , it is found  $\lambda = 0.55 \pm 0.08$ , with the error expressed by the standard deviation. Note that by averaging over all four  $\theta_i$  values, one would obtain  $\lambda = 0.47 \pm 0.16$ . Both these values compare well with those reported by Chia *et al* ( $0.46 \pm 0.03$  at the optimal doping) [20], by Lanzara *et al* ( $0.59 \pm 0.35$  at the optimal doping) [6,7],

#### 4. Conclusions

The method of measuring the electron-phonon interaction constant (mass-enhancement factor) at crystalline conducting surfaces by means of specular He atom scattering [8,9], has been extended to non-stoichiometric materials, where the specific contribution of doping to the electron-phonon interaction is contained in, and extracted from, the temperature dependence of the diffuse elastic (DE) peak. This new concept has been applied to HAS spectroscopy data for the non-stoichiometric high-temperature superconductor  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$  with  $\delta = 0.16$ , which is about the optimal doping and corresponds to the critical temperature  $T_c \sim 91\text{K}$ . The value of  $\lambda$  obtained in this way is in good agreement with the values recently estimated with other methods. This confirms that electron-phonon interaction, although not alone responsible for high- $T_c$  superconductivity, plays nevertheless a relevant role in this class of layered superconductors. Considering the comparatively expedient way of obtaining with He atom scattering the total electron-phonon interaction constant  $\lambda$ , it is hoped that the present experimental method will be soon applied to quasi-two-dimensional doped superconductors and other low-dimensional non-crystalline nanostructured materials.

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