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Article

A Forecasting Model Approach: Investigating Calendar Anomalies and Volatility Patterns in the Cryptocurrency Market

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Abstract: This paper investigates calendar anomalies, volatility patterns, and the best forecasting model for predicting volatility in the cryptocurrency market, focusing on ten prominent cryptocurrencies: Binance USD, Bitcoin, Binance Coin, Cardano, Dogecoin, Ethereum, Solana, Tether, USD Coin, and Ripple. Spanning from January 2016 to December 2023, the study utilizes sophisticated statistical models such as GARCH (p,q), EGARCH (p,q), and GJR-GARCH (p,q) to analyze precise changes in market dynamics and the impact of day-of-week fluctuations on cryptocurrency returns. Empirical evidence reveals significant findings regarding the persistence of volatility, positive and negative news effects on volatility, and day-of-week effects on cryptocurrency returns. Post-COVID-19, Sunday emerges as the least volatile day for cryptocurrencies, while Thursdays and Tuesdays exhibit greater volatility. Binance, Ethereum, Dogecoin, and Tether show anomalies where returns on Tuesday and Thursday significantly differed from those on other days of the week. Many other currencies, like the USD coin, Cardano, and Ripple, show anomalies only in the pre-COVID-19 period. The findings highlight the best forecast model for volatility for each top cryptocurrency, offering practical implications for investors, traders, regulators, and policymakers. These insights emphasize the importance of understanding and addressing calendar anomalies in the cryptocurrency market for informed decision-making, trading strategies, regulatory frameworks, and market stability.

Keywords: calendar anomalies; cryptocurrency; day-of-the-week effect; GARCH; volatility; forecasting

1. Introduction

Calendar anomalies in financial time series datasets have been the subject of research for more than a century. Calendar anomalies, which are patterns or effects beyond the explanation of conventional asset pricing models, are subject to the influence of psychological and seasonal factors [1]. Kumar [2] presents a counterargument to the Efficient Market Hypothesis (EMH) by asserting that investors can capitalise on predictable patterns in asset prices to generate abnormal returns, thereby facilitating the development of efficient trading strategies.

Cryptocurrencies have posed new challenges in the analysis of calendar anomalies. With over 22,235 cryptocurrencies listed on CoinMarketCap, the emergence of digital assets has upended traditional monetary systems and called into question established standards [3,4]. As cryptocurrencies gain popularity, retail investors are increasingly including them in their portfolios [5]. This emerging phenomenon entails incorporating the rapidly expanding cryptocurrency sector, which represents a new and distinct financial domain, into the investigation of calendar anomalies.

In contrast to conventional financial theories, the Adaptive Market Hypothesis (AMH) posits that market inefficiency and efficiency can coexist, enabling market participants and investors to adapt to fluctuating market conditions [6]. The hypothesis proposes that as market participants' knowledge and market dynamics evolve, they adapt their strategies, leading to the development of trading strategies and pricing models that are more precise [7]. Miralles-Quirós & Miralles-Quirós [8]

found evidence of calendar anomalies in cryptocurrencies, including the day-of-the-week effect, which shows predictable patterns in returns based on specific days. The AMH's emphasis on market adaptability is consistent with reported anomalies in cryptocurrency markets, where investors may modify their trading methods based on calendar impacts [9]. Understanding these anomalies is crucial for developing effective investment strategies and regulatory frameworks.

To enhance risk management, regulatory compliance, and forecasting precision, it is imperative to employ sophisticated statistical models to simulate the volatility and day-to-day fluctuations of cryptocurrencies. Generalized autoregressive conditional heteroscedasticity (GARCH) models, whether symmetrical or asymmetric, are appropriate for this objective. They influence crypto regulatory policies [10] aid regulators in analyzing crypto risk and volatility [11], facilitate market surveillance [12], and provide insights into market risks [13].

This study aims to investigate the volatility patterns of the cryptocurrency market both before and after the COVID-19 epidemic. We utilized sophisticated statistical models such as GARCH (p,q), EGARCH (p,q), and GJR-GARCH (p,q) to detect subtle changes in market dynamics. Furthermore, we shall examine the impact of day-of-week fluctuations on cryptocurrency returns to shed light on possible irregularities and their repercussions on market efficiency. To ensure extensive market coverage and representativeness, we used data on the ten most prominent cryptocurrencies in terms of market share. Moreover, our research ascertains the most effective GARCH model for forecasting the volatility of cryptocurrencies. This provides valuable insights that can assist policymakers, regulators, investors, and traders in effectively traversing the intricate dynamics of this rapidly growing financial domain.

The subsequent sections of this paper have the following structure: The following sections elaborate on our study: Section 3 provides an overview of the relevant literature; Section 4 analyzes and discusses empirical data; and, finally, Section 5 concludes our research.

2. Literature Review

Studying anomalies and volatility is critical for developing smart investing strategies, effective risk management, and market stability [14]. Anomalies call into question the efficient market hypothesis, implying the existence of regular patterns in asset prices that investors can exploit for abnormal returns [15]. The market conditions may cause these anomalies to vary over time, so a detailed analysis of their dynamics is necessary [16]. The Russian bond and stock markets, Turkish markets, US markets, Asia-Pacific stock markets, Thai stock market, Gulf Cooperation Council stock exchanges, Nigerian stock market, and Swedish stock market have historically noted calendar anomalies [17–22].

The day-of-the-week and month-of-the-year effects, divided into religious and non-religious anomalies, have received the most attention in empirical research [23]. Religious anomalies include the Yom Kippur, Diwali, and Ramadan effects; non-religious anomalies include the day-of-the-week, month-of-the-year, Halloween, turn-of-the-month, and turn-of-the-year effects [24,25]. Though calendar effects in stock markets are well-known, very little is known about calendar effects in cryptocurrency markets, particularly with regard to cryptocurrencies other than Bitcoin, Ethereum, and Litecoin [26]. Several authors have explained calendar irregularities in cryptocurrency markets by attributing them to liquidity, market moods, and other outside variables [7,27]. Important factors in cryptocurrency markets, such as sentiment analysis of social media data and liquidity dynamics, can influence calendar anomalies [28,29].

Knowing these dynamics is necessary to understand the fundamental causes of calendar anomalies. Cryptocurrency was one of the many financial markets that the COVID-19 epidemic severely affected [30]. Numerous studies have looked into these impacts in various markets, emphasizing their major influence on cryptocurrencies and stock markets [31]. The epidemic had a negative impact on several economies and completely changed the function of cryptocurrencies worldwide [32]. Though they experienced notable negative return shocks during the first wave of the epidemic, cryptocurrencies like Bitcoin, Ethereum, and Litecoin showed resilience despite the early shocks [33].

Researchers have extensively studied calendar anomalies and volatility in bitcoin markets using GARCH models, including asymmetric GARCH models [10,34]. Particularly asymmetric GARCH models are well-suited to simulate anomalies and volatility in cryptocurrencies because they can capture asymmetric volatility patterns [35]. By providing insightful information on the dynamics of cryptocurrency markets, these models improve forecasting and risk management skills [36].

Kinateder and Papavassiliou [37], Kaiser [38], Aharon and Qadan [39], Dangi [40], and Süreyya and ÖLÇEN [41] have published in-depth studies of the phenomenon of seasonality and calendar effects in cryptocurrencies. They offer empirical proof of the effect of the day of the week, indicating that some Fridays show unique trends in terms of volatility and price changes in the cryptocurrency market. By examining the day-of-the-week effect, researchers can better understand the trends and patterns in cryptocurrency returns and volatility. This knowledge may have ramifications for risk management and investment strategies in the digital asset market.

Despite the evolving nature of cryptocurrency research, there remains a notable gap in the literature concerning a comparative analysis of the day-of-the-week effect in the cryptocurrency market before and after the onset of the COVID-19 pandemic. This gap offers a chance to look into how temporal patterns and anomalies have changed in reaction to the pandemic, offering insightful information about how external shocks affect market dynamics and trading techniques according to the day of the week. We aim to address this gap and contribute to a deeper understanding of the evolving relationship between external events and cryptocurrency market behavior.

3. Data and Methodology

In our empirical investigation, we examined a dataset of daily closing prices in US dollars obtained from CoinMarketCap (<https://coinmarketcap.com/coins/>). We focused on the top term cryptocurrencies in terms of diffusion and market capitalization: Binance USD, Bitcoin, Binance Coin, Cardano, Dogecoin, Ethereum, Solana, Tether, USD Coin, and Ripple. From January 2016 to December 2023, we separated the dataset into two periods: pre-COVID-19 (January 1, 2016, to December 31, 2019, excluding Solana and Binance USD owing to data paucity) and post-COVID-19 (January 1, 2020, to December 31, 2023).

Table 1 displays a summary of our 10 cryptocurrencies' daily closing returns. Pre-COVID-19, Binance coin had the highest average return, followed by Ripple; post-COVID-19, Binance coin had the highest average return, followed by Cardano. Among the 10 cryptocurrencies, Binance USD experienced the least fluctuation during the pre-COVID-19 period, while USD Coin experienced the least fluctuation during the post-COVID-19 period. The distribution of returns during the pre-COVID-19 period favourably skews left for Binance USD, Ethereum, and Tether, and positively for the remaining coins. The post-COVID-19 timeframe exhibits a leftward skew for the majority of cryptocurrencies, such as Binnacle USD, Bitcoin, Binance Coin, Cardano, Solana, Ethereum, and Ripple.

Table 1. Daily descriptive statistics of ten cryptocurrencies in pre- and post-COVID-19 periods.

Descriptive statistics		Binance USD	Bitcoin	Binance Coin	Cardano	Dogecoin	Solana	Ethereum	Tether	USD Coin	Ripple
Mean	Pre-COVID	0.122%	12.015%	58.287%	2.719%	20.358%	-	-12.189%	-0.017%	-0.110%	31.179%
	Post-COVID	-0.025%	9.981%	29.489%	24.346%	-11.627%	37.451%	23.580%	0.005%	-0.033%	8.463%
Maximum	Pre-COVID	60.014%	2870.990%	32699.360%	8721.609%	4553.488%	-	2625.760%	1265.370%	253.691%	8812.683%
	Post-COVID	650.371%	1760.260%	5526.562%	2691.957%	7324.953%	3844.862%	2194.057%	250.046%	192.579%	4233.534%
Minimum	Pre-COVID	-71.155%	- 2251.580%	-10024.390%	-2698.714%	-4781.982%	-	- 2185.820%	- 2833.380%	-209.640%	- 4962.824%
	Post-COVID	-649.448%	- 4337.140%	-5590.344%	-5244.024%	-4667.967%	-4521.549%	- 5630.799%	-197.281%	-158.485%	- 5495.483%
Standard Deviation	Pre-COVID	0.191	4.393	15.609	7.708	6.921	-	5.152	1.486	0.475	7.703
	Post-COVID	0.428	3.874	5.700	5.859	7.457	7.792	5.209	0.292	0.282	6.276
Coefficient of Variation	Pre-COVID	156.065	36.563	26.78	283.529	33.996	-	-42.271	-9004.824	-431.951	24.706
	Post-COVID	-1697.48	38.813	19.33	24.065	-64.137	20.806	22.092	5760.118	-854.539	74.162
Skewness	Pre-COVID	-0.184	0.076	10.643	2.92	0.829	-	-0.201	-5.635	0.186	2.437
	Post-COVID	-0.107	-1.429	-0.185	-0.442	1.464	-0.058	-1.464	0.159	0.045	-0.205
Kurtosis	Pre-COVID	5.897	7.796	237.267	31.126	12.965	-	5.857	148.928	9.022	27.515
	Post-COVID	106.763	19.683	24.491	11.051	24.921	6.64	18.420	15.488	9.884	17.856

Source- Elaborated by the author

Our investigation began with the calculation of returns, defined as the natural logarithm of the ratio between two consecutive prices using the following formula:

$$R_n = (In CP_n - In CP_{n-1}) \times 100 \quad (1)$$

where R_n denotes returns on an n^{th} day in percentage; CP_n denotes closing price on an n^{th} day; CP_{n-1} denotes the closing price on the previous trading day; and In is a natural log.

We performed the Jarque-Bera and Anderson Darling statistical tests, both of which validated the observation that the ten cryptocurrencies exhibit leptokurtic characteristics. Utilizing the returns series for all ten currencies, we conducted unit root tests, namely the Augmented Dickey-Fuller (ADF) and Phillips-Perron tests (Tables 2.1 and 2.2), to see if the data was stationary. Our results confirmed that the data is stationary.

Table 2. 1: Augmented Dickey-Fuller test results pre-and post-COVID-19 period.

Augmented Dickey-Fuller Test Statistics										
Pre- COVID-19 Period										
	Binance USD	Bitcoin	Binance Coin	Cardano	Dogecoin	Solana	Ethereum	Tether	USD Coin	Ripple
t-										
Statistic	-12.454	-33.183	-31.552	-16.336	-20.820		-28.069	25.340	-14.962	-20.492
P-value	0.000	0.000	0.000	0.000	0.000	N/A	0.000	0.000	0.000	0.000
Post- COVID-19 Period										
t-										
Statistic	-26.466	-33.829	-21.147	-33.867	-25.908	-32.832	-34.677	24.210	-23.482	-32.970
P-value	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000

Source: Elaborated by the author.

Table 2. 2: Phillips-Perron Test results pre-and post-COVID-19 period.

Phillips-Perron Test statistic										
Pre- COVID-19 Period										
	Binance USD	Bitcoin	Binance Coin	Cardano	Dogecoin	Solana	Ethereum	Tether	USD Coin	Ripple
t-										
Statistic	-16.307	-33.201	-31.727	-27.945	-31.612		-28.245	68.989	-33.266	-33.572
P-value	0.000	0.000	0.000	0.000	0.000	N/A	0.000	0.000	0.000	0.000
Post- COVID-19 Period										
t-										
Statistic	-30.657	-33.784	-43.953	-34.209	-32.753	-33.492	-29.931	74.346	-41.548	-35.457
P-value	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000

Source: Elaborated by the author.

We used dummy variables in an OLS regression, and after conducting unit root tests, we carried out Engle's [42] ARCH test. This test revealed the presence of volatility clustering both before and after the COVID-19 pandemic (as shown in Table A.1 in Appendix A). As all p-values were less than

0.05, the presence of ARCH effects was confirmed. These results support the use of GARCH frameworks to model volatility.

To incorporate the leptokurtic nature of cryptocurrencies, we implemented the Normal Inverse Gaussian (NIG) distribution for the error element in the GARCH model. This distribution can capture additional skewness and kurtosis in the residual return series [43]. Table 3 shows the conditional variance equations of the various GARCH models used in the study. All coefficients (ω , α_i , and β_j) in the GARCH (p,q) model must be non-negative and satisfy the condition $\alpha_i + \beta_j < 1$. Higher α_i values suggest more volatility responses to market shocks, while larger β_j coefficients indicate the occurrence of market shocks. In the EGARCH (p, q) model, α_i assesses shock magnitude, β_j reflects volatility persistence, and γ_i represents the leverage effect. A negative γ_i indicates that negative news has a greater influence on volatility than positive news [44]. In the GJR GARCH (p,q) model, $\gamma_i > 0$ indicates the presence of the leverage effect. When $\gamma_i \neq 0$, "good news" and "bad news" have different impacts.

Table 3. Different GARCH model equations.

Model	Conditional Variance Equation
GARCH (p, q) Model	$\sigma_t^2 = \omega + \sum_{i=1}^p \alpha_i \varepsilon_{t-i}^2 + \sum_{j=1}^q \beta_j \sigma_{t-j}^2$
EGARCH (p, q) Model	$\log(\sigma_t^2) = \omega + \sum_{i=1}^p \left[\alpha_i \left(\frac{ \varepsilon_{t-i} }{\sigma_{t-i}} - \sqrt{\frac{2}{\pi}} \right) + \gamma_i \left(\frac{\varepsilon_{t-i}}{\sigma_{t-i}} \right) \right] + \sum_{j=1}^q \beta_j \log(\sigma_{t-j}^2)$
GJRGARCH (p, q) Model	$\sigma_t^2 = \omega + \sum_{i=1}^p (\alpha_i + \gamma_i I_{t-i}) \varepsilon_{t-i}^2 + \sum_{j=1}^q \beta_j \sigma_{t-j}^2$

In our analysis, we incorporated dummy variables into the mean equation of a GARCH model. To prevent multicollinearity between the independent variables, we excluded the intercept term and included dummy variables for all seven days of the week. This approach helps capture and quantify day-of-the-week effects in cryptocurrency returns, enabling the identification of systematic patterns. Moreover, it enhances model interpretability, improves forecasting accuracy, and controls for seasonality, contributing to a more comprehensive understanding of market behavior.

$$r_t = \sum_{i=1}^7 \beta_i D_{i,t} + \Phi_1 r_{t-1} + \Phi_2 r_{t-2} + \dots + \Phi_p r_{t-p} + \varepsilon_t \quad (2)$$

Where $D_{i,t}$ is the dummy variable for the day i at time t , β_i is coefficient, Φ_i are the autoregressive parameters, ε_t is the error term.

4. Empirical Evidence

We conducted a comparative analysis of ten cryptocurrencies using a variety of GARCH-type models, selecting the best model for p and q based on the smallest Akaike Information Criterion (AIC) information criteria as the optimal ones. We also carried out Ljung-Box and Lagrange multiplier (LM) tests on the residuals of the selected GARCH (p, q) models to assess their resilience. Notably, all coefficient p-values were highly significant at the 95% confidence level.

As indicated in Tables 4.1 (period preceding COVID-19) and 4.2 (period following COVID-19), The fact that the coefficients $\beta_1 + \beta_2 > \alpha_1$ indicates that when attempting to forecast present volatility, attention is directed towards the enduring consequences of past shocks rather than recent occurrences. Furthermore, the persistence of volatility was evaluated by summing the values of α_1 ,

β_1 , and β_2 . This parameter's sum, which is a critical indicator of model stability, must not exceed 1. A high value of the coefficient of β_1 suggested the presence of volatility clustering.

Table 4. 1: GARCH (p,q) model results Pre-COVID-19 period.

	Bitcoin	Binance Coin	Cardano	Dogecoin	Ethereum	Tether	USD Coin	Ripple
Best GARCH (p,q)	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>
Model	(1,2)	(1,1)	(1,1)	(1,1)	(1,1)	(1,1)	(1,1)	(1,2)
w	1.779	2.706	0.641	0.731	3.993	0.000	0.000	2.360
a₁	0.200	0.239	0.068	0.235	0.152	0.336	0.089	0.390
b₁	0.400	0.718	0.917	0.650	0.724	0.609	0.910	0.189
b₂	0.310							0.239
AIC Value	5.619	6.441	6.365	6.013	5.999	0.087	0.519	6.003
Ljung box test p-value	0.283	0.877	0.281	0.135	0.538	0.991	0.219	0.127
LM-Test P Value	0.792	0.628	0.107	0.696	0.713	0.851	0.584	0.809
Volatility persistence	0.911	0.957	0.985	0.885	0.876	0.944	0.999	0.818

Source: Elaborated by the author.

Table 4. 2: GARCH (p,q) model results in the Post-COVID-19 period.

	Binanc e USD	Bitcoin	Binanc e Coin	Carda no	Dogec oin	Solana	Ethere um	Tether	USD Coin	Ripple
Best GARCH (p,q)	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>	<i>GARCH</i>
Model	H(1,2)	H(1,1)	H(1,1)	H(1,1)	H(1,1)	H(1,1)	H(1,1)	H(1,1)	H(1,1)	H(1,1)
w	0.003	0.444	0.616	3.160	5.761	3.848	1.679	0.001	0.002	1.453
a₁	0.446	0.054	0.187	0.154	0.494	0.129	0.092	0.175	0.166	0.187
b₁	0.180	0.916	0.724	0.759	0.502	0.807	0.844	0.823	0.803	0.832
b₂	0.322									
AIC Value	-0.243	5.282	5.948	6.144	6.021	6.763	5.916	-0.631	-0.309	5.887
Lung box test p-value	0.657	0.724	0.678	0.808	0.364	0.258	0.531	0.073	0.297	0.737
ARCH LM-Test P Value	0.455	0.648	0.415	0.719	0.779	0.332	0.855	0.909	0.533	0.494
Volatility persistence	0.948	0.969	0.911	0.913	0.996	0.936	0.936	0.997	0.969	1.019

Source: Elaborated by the author.

Following the COVID-19 pandemic, Ripple demonstrated a heightened susceptibility to negative leaps and eruptive behavior, as indicated by the equation $\alpha_1 + \beta_1 + \beta_2 > 1$. This observed pattern indicates a decline in volatility, which aligns with the conclusions drawn by Chan [45]. Consistent with the findings of Queiroz [46], the GARCH (1,1) model demonstrated high performance in predicting volatility across most of the cryptocurrencies during both the pre-COVID-19 and post-COVID-19 periods, leaving only Bitcoin and Ripple during the pre-COVID-19 period and Binance USD in the post-COVID-19 period where GARCH (1,2) is a better fit.

Additionally, we examined the EGARCH and GJR-GARCH asymmetric GARCH models for ten distinct cryptocurrencies pre- and post-COVID-19 pandemic. Tailored to account for heavy tails and high kurtosis, these models capture inherent volatility asymmetry, specifically as it relates to positive and negative returns, in an effective manner. We have selected the optimal p-q model with the lowest AIC score. Tables 5.1 (pre-COVID-19 era) and 5.2 (post-COVID-19 era) illustrate the optimal selection of asymmetric models.

Table 5. 1: Asymmetric GARCH (p,q) model results pre-COVID-19 period.

	Bitcoin	Binance Coin	Cardano	Dogecoin	Ethereum	Tether	USD Coin	Ripple
Best Asymmetric Model	<i>GJR- GARCH (1,1)</i>	<i>EGARCH H (1,1)</i>	<i>EGARCH H (1,1)</i>	<i>EGARCH H (2,1)</i>	<i>GJR- Garch (1,1)</i>	<i>GJR- Garch (1,1)</i>	<i>EGARCH H (2,1)</i>	<i>EGARCH H (2,1)</i>
ω	1.539	-0.089	-0.066	-0.109	2.191	0.020	-0.163	-0.072
α_1	0.139	0.208	0.184	0.500	0.128	0.524	0.388	0.679
a_2				-0.260			-0.202	-0.498
γ_i	0.055	-0.074	0.006	0.049	0.003	0.539	0.077	0.056
β_1	0.757	0.986	0.982	0.982	0.804	0.688	0.989	0.985
AIC Value	5.407	6.426	6.167	6.005	6.181	0.038	0.660	5.987
Lung box test p-value	0.278	0.967	0.185	0.264	0.662	0.910	0.615	0.320
ARCH LM- Test P Value	0.348	0.415	0.600	0.887	0.648	0.973	0.599	0.416

Source: Elaborated by the author

Table 5. 2: Asymmetric GARCH (p,q) model results Post-COVID-19 period.

	Binance USD	Bitcoin	Binance Coin	Cardano	Dogecoin	Solana	Ethereum	Tether	USD Coin	Ripple
Best Asymmetric Model		<i>EGARCH H (1,2)</i>	<i>GJR- GARCH H (1,1)</i>	<i>EGARCH H (1,2)</i>	<i>GJR- GARCH H (1,1)</i>	<i>GJR- GARCH H (1,1)</i>	<i>GJR- GARCH (1,1)</i>	<i>EGARCH H (1,2)</i>	<i>EGARCH H (1,1)</i>	
ω	<i>NO</i>	0.040	0.721	0.176	5.745	5.933	2.145	-0.773	-0.317	<i>NO</i>
α_1	<i>asymmet</i>	0.087	0.158	0.235	0.474	0.168	0.061	0.617	0.264	<i>asymmet</i>
γ_i	<i>ric model</i>	-0.039	0.077	-0.035	0.083	0.039	0.116	0.179	0.067	<i>ric model</i>
β_1	<i>is a good</i>	1.469	0.813	1.480	0.498	0.753	0.808	0.286	0.960	<i>is a good</i>
β_2	<i>fit</i>	-0.507		-0.582				0.611		<i>fit</i>
AIC Value		5.490	5.946	5.261	6.003	6.829	5.033	-0.393	-0.311	
Lung box test p-value		0.844	0.760	0.805	0.719	0.266	0.834	0.441	0.232	

ARCH								
LM-Test	0.450	0.393	0.649	0.979	0.605	0.326	0.966	0.182
P Value								

Source: Elaborated by the author.

It is noteworthy that for the majority of cryptocurrencies, $\gamma_i > \text{zero}$, suggesting that positive news or events have a more pronounced effect on escalating volatility compared to negative news or events of comparable magnitude. In contrast, $\gamma_i < 0$ for Bitcoin and Cardano in the period following COVID-19, indicating that negative news has a more significant impact on escalating volatility compared to positive news of comparable magnitude.

We also did Q-Q plot tests on the residuals from the best-fitted GARCH model, as shown in Figure 3 (Pre-COVID) and Figure 4 (Post-COVID-19), to see how well the chosen GARCH family models fit the real-world data and to make sure they were appropriate.

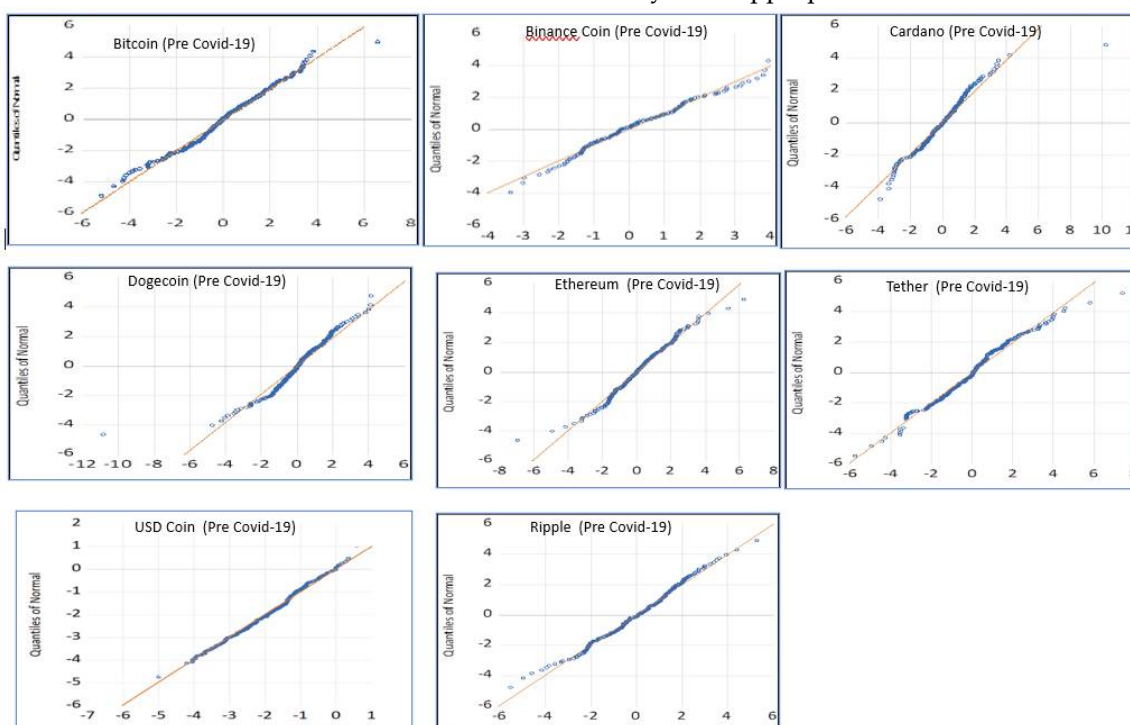


Figure 3. Q-Q plot of residuals pre-COVID-19 Period.

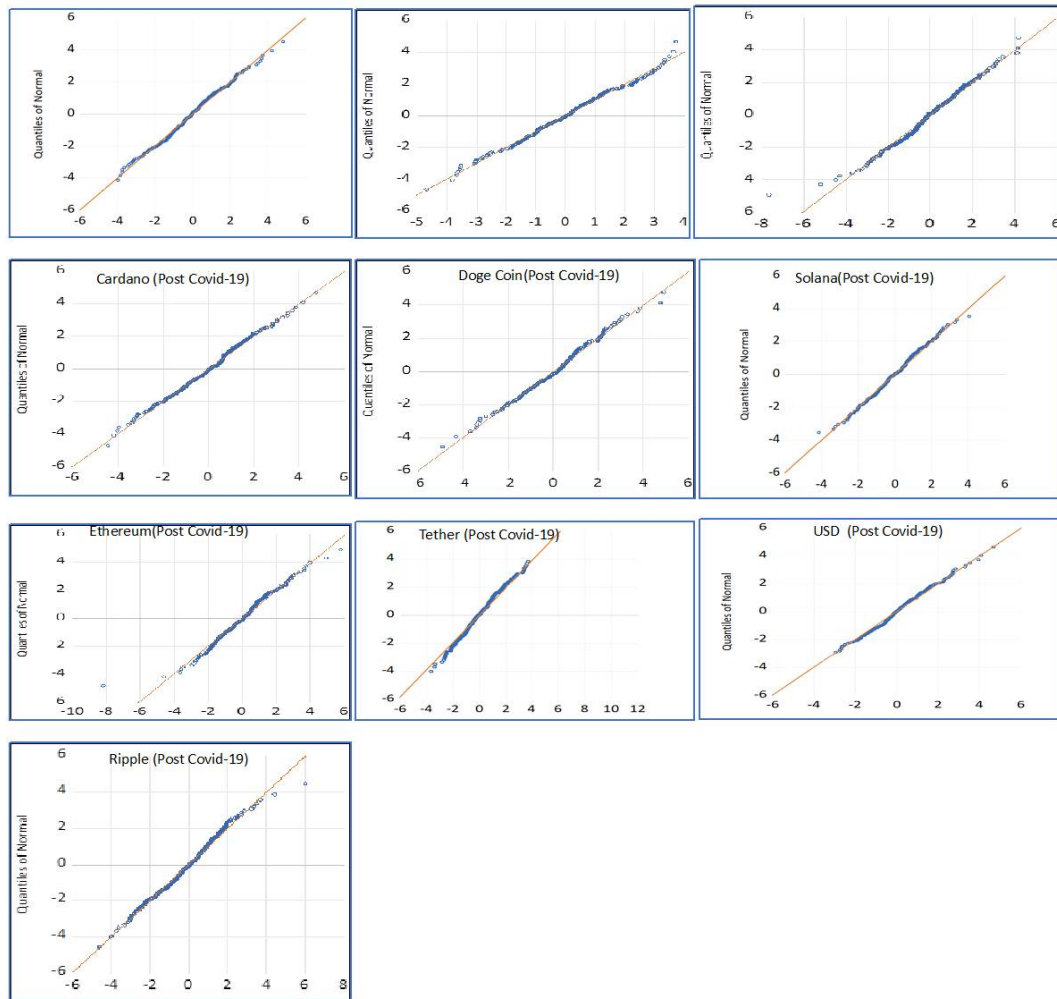


Figure 4. Q-Q plot of residuals post-COVID-19 Period.

In addition, as shown in Table 6, we assessed various GARCH models to determine which one predicted cryptocurrency volatility the most accurately. We utilized Mean Absolute Percentage Error (MAPE), Root Mean Squared Error (RMSE), Mean Absolute Error (MAE), and Theil's U to evaluate the efficacy of the models. Models with lower RMSE and MAE values demonstrated greater agreement with the observed data, while models with lower MAPE values predicted more accurate forecasts. With Theil's U, we were able to distinguish between predicted and actual values.

Table 6. Summary of Optimal GARCH Models for Cryptocurrency Volatility Forecasting.

	Best fit Model	Model type	RSME	MAE	MAPE	Theil's U
Binance USD	GARCH (1,2)	Symmetric	0.301	0.200	117.653	0.915
Bitcoin	GARCH (1,1)	Symmetric	3.869	2.610	371.537	0.898
Binance Coin	GJR-GARCH (1,1)	Asymmetric	5.699	3.574	119.400	0.961
Cardano	EGARCH (1,2)	Asymmetric	5.839	4.068	748.083	0.938
Dogecoin	GJR-GARCH (1,1)	Asymmetric	8.860	4.362	134.921	0.961
Solana	GARCH (1,1)	Symmetric	7.791	5.610	935.216	0.932
Ethereum	GJR-GARCH (1,1)	Asymmetric	5.199	3.596	140.540	0.905
Tether	GARCH (1,1)	Symmetric	0.293	0.189	137.435	0.906
USD Coin	EGARCH (1,1)	Asymmetric	0.282	0.190	134.030	0.910

Ripple	GARCH (1,1)	Symmetric	6.270	3.835	127.782	0.967
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Source: Elaborated by the author.



By comparing the low AIC scores of symmetric and asymmetric models for each cryptocurrency with seven dummy variables, we determined the optimal GARCH model and examined the effects of the day of the week. Table 7 presents the coefficients and corresponding p-values derived from the optimal GARCH model. We observed a noteworthy pattern on Sundays, where the majority of cryptocurrencies exhibited favorable returns both before and after the COVID-19 pandemic. In contrast to the negative Sunday effect previously documented by Dorfleitner and Lung [47] our discovery provides support for the results reported by Naz et al. [7]. Returns on Saturday also showed a discernible change. Cryptocurrencies generated favorable returns prior to the onset of the COVID-19 pandemic, which is consistent with findings from Ma & Tanizaki [48], Hamurcu [49], Lopez Martin [50], and Naz et al. [7]. Except for Tether, the majority of coins reversed this trend after COVID-19. This alignment is supportive of the adaptive market hypothesis.

Table 7. Coefficients and p-values for Day-of-Week Effects in the Best-Fit GARCH Model.

		Monday		Tuesday		Wednesday		Thursday		Friday		Saturday		Sunday	
		Pre-	Post	Pre-	Post	Pre-	Post	Pre-	Post	Pre-	Post	Pre-	Post	Pre-	Post
		CO	CO	CO	CO	CO	CO	CO	CO	CO	CO	CO	CO	CO	CO
		VID	VID	VID	VID	VID	VID	VID	VID	VID	VID	VID	VID	VID	VID
		-19	-19	-19	-19	-19	-19	-19	-19	-19	-19	-19	-19	-19	-19
	Coefficient	0.00	-	-	0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	-	
BINANCE USD	P-value	5	5	9	6	6	7	9	4	3	8	0	7	0.00	
	Coefficient	0.14	0.15	0.19	0.43	0.19	0.16	0.02	0.35	-	-	0.41	-	0.33	0.24
BITCOIN	P-value	7	0	6	5	7	5	7	4	1	5	2	6	7	5
	Coefficient	-	0.25	-	0.52	-	-	-	0.34	-	-	0.18	-	0.01	0.63
BINANCE COIN	P-value	0.33	2	0.29	3	0.60	0.01	0.47	0	0.19	0.62	8	0.03	8	5
	Coefficient	0.09	-	-	0.31	-	-	-	0.29	-	-	0.22	-	0.58	1.06
CARDANO	P-value	5	0	3	7	4	6	6	2	5	3	9	2	4	7
	Coefficient	0.19	0.47	0.29	0.04	0.03	0.95	0.06	0.29	0.48	0.02	0.43	0.92	0.94	0.10
CARDANO	P-value	1	5	6	6	1	6	3	1	5	9	6	9	9	0
	Coefficient	0.79	0.56	0.17	0.37	0.07	0.83	0.18	0.39	0.00	0.15	0.53	0.43	0.12	0.06
CARDANO	P-value	2	6	6	9	5	3	0	9	0	7	7	5	2	8

Dogecoin	Coefficient	0.23	-	-	-	-	-	0.10	-	-	0.08	0.32	-	-	0.43
	P-value	3	3	8	2	4	0	8	5	6	9	6	4	1	9
		0.21	0.09	0.24	0.00	0.00	0.40	0.61	0.55	0.00	0.55	0.12	0.03	0.80	0.00
SOLANA	Coefficient	-	-	-	-	-	-	0.60	-	-	-	-	-	-	0.79
	P-value	6	4	3	8	0	4	8	3	0	4	7	0	2	
		0.99	0.77	0.11	0.21	0.57	0.77	0.17							
ETHEREUM	Coefficient	0.01	0.28	0.43	0.55	-	-	-	0.90	-	-	0.71	-	0.49	0.78
	P-value	2	8	3	5	0	9	6	1	5	3	9	5	9	2
		0.97	0.50	0.24	0.09	0.83	0.87	0.02	0.01	0.23	0.10	0.79	0.35	0.09	
TETHER	Coefficient	-	-	-	-	0.00	0.00	-	-	-	-	0.02	0.02	0.01	0.01
	P-value	7	7	8	8	2	2	0	0	2	2	2	2	0	0
		0.37	0.37	0.02	0.02	0.77	0.77	0.01	0.01	0.84	0.84	0.00	0.00	0.16	0.19
USD COIN	Coefficient	-	0.02	0.01	-	0.02	-	0.01	0.01	0.02	0.00	0.00	-	0.00	0.00
	P-value	7	4	8	1	7	2	1	7	5	3	2	1	9	2
		0.05	0.09	0.37	0.33	0.20	0.15	0.62	0.21	0.24	0.84	0.90	0.17	0.66	0.89
Ripple	Coefficient	-	-	-	0.28	-	-	-	0.30	-	0.02	0.19	-	0.10	0.23
	P-value	5	7	6	2	0	2	3	0	3	7	2	0	6	5
		0.55	0.44	0.00	0.29	0.56	0.59	0.73	0.25	0.00	0.91	0.26	0.57	0.42	0.48

The p-values are significant at a confidence level of 95%.

 significant values in the pre-COVID-19 period
 significant values in the post-COVID-19 period

Source: Elaborated by the author

Anomalies persisted in Binance Coin, Dogecoin, Ethereum, and Tether during the period following COVID-19. Dogecoin, Tether, and Binance Coin all experienced anomalies on Tuesday. Dogecoin and Tether both exhibited anomalies on Saturday and Sunday, whereas Tether only did so on Saturday. On Thursdays, Ethereum consistently maintained its anomaly. In contrast, Cardano,

Ripple, and USD Coin did not exhibit these anomalies in the period following COVID-19. This suggests that the efficiency of these markets is increasing, possibly due to savvy and seasoned investors, advancements in communication and technology, and easy access to information. We can potentially attribute the observed fluctuations in cryptocurrency conduct to evolving investor sentiments, particularly in light of the COVID-19 pandemic. Market sentiment, fluctuating between positive and negative values, influences the price dynamics.

5. Conclusions

In this paper, we investigated volatility patterns in the cryptocurrency market by employing the GARCH (p,q), EGARCH (p,q), and GJR-GARCH (p,q) models. Our analysis identified the most suitable model capable of forecasting the volatility of the top ten cryptocurrencies during the post-COVID period, which can help investors accurately assess and anticipate market fluctuations. Sunday was the least volatile day for all cryptocurrencies during the post-COVID-19 period, while Thursdays and Tuesdays exhibited greater volatility. The models successfully captured the phenomenon of volatility clustering and shed light on the distinct effects of positive and negative news on volatility, thereby improving our models' precision.

Furthermore, we investigated the day-of-week effect in the cryptocurrency market before and after the COVID-19 pandemic. Our study revealed that Cardano, USD Coin, and Ripple did not exhibit any significant day-of-the-week effects in the post-COVID-19 period, indicating potential enhancements in market efficiency. Conversely, Binance Coin maintained its day-of-the-week effect, transitioning from Wednesday in the pre-COVID-19 period to Tuesday and Friday in the post-COVID-19 period.

The day-of-week effect presents a challenge to the efficient market hypothesis. Inspired by these findings, investors ought to utilize technical and fundamental analysis in order to capitalize on foreseeable price trends and exploit market inefficiencies for the purposes of strategic trading and hedging. These observations can provide guidance to policymakers and regulators as they formulate more knowledgeable regulations, establish early warning systems, and execute macroprudential policies in order to protect investor interests and market stability.

In conclusion, our study offers practical implications for investors, traders, regulators, and policymakers. It reinforces the importance of understanding and addressing day-of-the-week anomalies in the cryptocurrency market, with the potential to shape investment decisions, trading strategies, regulatory frameworks, and market surveillance practices in a rapidly evolving and increasingly influential financial landscape.

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Appendix A

Table A1. Test results for Engle's Arch tes.

1	Binance USD	Post-COVID-19	F-statistic	236.151	Prob. F	0.000
			Obs*R-squared	324.169	Prob. Chi-Square	0.000
2	Bitcoin	Pre-COVID-19	F-statistic	19.672	Prob. F	0.000

			Obs*R-squared	38.077	Prob. Chi-Square	0.000
		Post-COVID-19	F-statistic	0.142	Prob. F	0.049
			Obs*R-squared	0.284	Prob. Chi-Square	0.049
		Pre-COVID-19	F-statistic	0.038	Prob. F	0.963
			Obs*R-squared	0.076	Prob. Chi-Square	0.963
3	Binance Coin	Post-COVID-19	F-statistic	23.340	Prob. F	0.000
			Obs*R-squared	44.775	Prob. Chi-Square	0.000
		Pre-COVID-19	F-statistic	26.171	Prob. F	0.000
			Obs*R-squared	49.309	Prob. Chi-Square	0.000
4	Cardano	Post-COVID-19	F-statistic	8.806	Prob. F	0.000
			Obs*R-squared	17.365	Prob. Chi-Square	0.000
		Pre-COVID-19	F-statistic	16.792	Prob. F	0.000
			Obs*R-squared	32.669	Prob. Chi-Square	0.000
5	Dogecoin	Post-COVID-19	F-statistic	24.146	Prob. F	0.000
			Obs*R-squared	44.661	Prob. Chi-Square	0.000
		Post-COVID-19	F-statistic	18.776	Prob. F	0.000
			Obs*R-squared	36.201	Prob. Chi-Square	0.000
		Pre-COVID-19	F-statistic	6.232	Prob. F	0.002
			Obs*R-squared	12.313	Prob. Chi-Square	0.002
7	Ethereum	Post-COVID-19	F-statistic	3.724	Prob. F	0.025
			Obs*R-squared	7.416	Prob. Chi-Square	0.025
		Pre-COVID-19	F-statistic	7.657	Prob. F	0.001
			Obs*R-squared	15.133	Prob. Chi-Square	0.001
8	Tether	Post-COVID-19	F-statistic	234.791	Prob. F	0.000
			Obs*R-squared	322.888	Prob. Chi-Square	0.000
		Pre-COVID-19	F-statistic	37.645	Prob. F	0.000
			Obs*R-squared	64.870	Prob. Chi-Square	0.000
9	USD Coin	Post-COVID-19	F-statistic	122.120	Prob. F	0.000
			Obs*R-squared	197.782	Prob. Chi-Square	0.000
		Pre-COVID-19	F-statistic	52.853	Prob. F	0.000
			Obs*R-squared	96.619	Prob. Chi-Square	0.000
10	Ripple	Post-COVID-19	F-statistic	23.880	Prob. F	0.000
			Obs*R-squared	45.766	Prob. Chi-Square	0.000

Source: Elaborated by the author.

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