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Article

Optimizing Travel Distance in a Synchronized-Zone Order Picking System: A Mathematical Programming Approach

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Abstract: This paper offers an integrated approach for correlated storage assignment strategy (CSAS) to optimize travel distance by considering item correlation, picking frequency, zoning, and slot constraints to improve operational efficiency in distribution centers. We simplify the mixed integer non-linear programming (MINLP) model and incorporate integrated heuristic procedures for faster convergence. We introduce positive and negative centroid deviations as techniques to guide the model convergence and explore different scenarios. In the second stage of item assignment, we prioritize items within zones using a ranking formula that is optimal for both single-item and multiple-item orders. By analyzing the distribution of correlated item across zones and the impact of their picking frequency on optimizing travel distance, we propose an improved CSAS that minimize travel distance by strategically placing items based on their proximity to the depot. Our model reduces trips in distant zones by prioritizing larger average order sizes, while maximizing trips for frequently ordered smaller lists in closer zones. This method significantly reduces travel distance by minimizing the need for pickers in distant zones to frequently travel to the depot. Simulation results show reductions of up to 36.75% for fitted data and 33.59% for recent data.

Keywords: correlated storage assignment strategy; FlexSim; mathematical programming model; MINLP; order picking optimization; resource allocation; simulation; synchronized-zone; travel distance

1. Introduction

In an extensive review on recent order picking trends and research topics, Casella et al. (2023) analyzed 269 journal papers from 2007 to 2022, emphasizing the crucial importance of optimizing order picking in warehouses. The study addresses various topics related to storage allocation policies, including the lack of research on correlated storage assignment strategy (CSAS) as one of the identified gaps. This strategy involves grouping items based on their historical correlation in customer orders. Frazelle (1989) pioneered the use of combined probabilities of pairs of items occurring in the same order as an item allocation method to minimize total travel distance. This approach that involves grouping items into zones was referred to as correlated assignment strategy in the work of Frazelle and Sharp (1989). Subsequently, many heuristic algorithms for this strategy have been developed. However, there is still a lack of dedicated research on correlated storage assignment. The review by Casella et al. also examined routing policies and note that the routing planning can be considered as a special case of the traveling salesman problem (TSP), which is known to be NP-hard. Finding an optimal solution in polynomial-time for the TSP is not always feasible. Additionally, due to the requirement for real-time operational decisions for picker routings, researchers commonly employ heuristic and meta-heuristic approaches to efficiently find near-optimal routing solutions. The review also highlights the interrelationship between routing and storage allocation policies. Optimal storage allocation is recognized as a key factor in routing optimization due to their dependence. Heuristic algorithms for routing problems were frequently proposed in conjunction with various storage assignment policies, particularly random storage; while meta-heuristic algorithms were commonly paired with random and class-based storage

policies. The review also identified a lack of available exact or meta-heuristic algorithms for routing problems that specifically designed for correlated storage policy case studies. In contrast to the routing problem, the storage assignment does not require a real-time solution, and an optimal solution is preferred over a near-optimal one, especially considering the impact that storage optimization can have on routing planning. Furthermore, an exact solution for the storage assignment is appropriate for relatively small problem size. However, incorporating travel distance assessments into the storage assignment model, as in routing models, presents considerable computational challenges. This is primarily due to the potential transformation of the storage assignment problem into NP-hard, unless the model is designed effectively. Despite these difficulties, it is crucial to consider the broader framework of warehouse strategies when addressing a particular problem in order to offer an integrated optimization. By adopting an integrated approach and carefully considering the effects of various aspects of warehouse operations, the optimization has the ability to significantly improve performance. While failing to account for the impact of other operations can have a negative effect on the system. Therefore, it is imperative to conduct a comprehensive evaluation of the interdependent consequences of combining strategies to ensure optimal outcomes. In the context of a multi-picker system, for example, concentrating highly correlated items in one zone may lead to congestion issues if dedicated zones are not implemented. Similarly, assigning all correlated items closer to the depot in one zone may negatively affect staff utilization and increase idle time in dedicated-zone systems.

In this paper we introduce a new approach to minimizing travel distance in a distribution center's single-order, synchronized zone picking system. We present a model for implementing CSAS by taking into account the influence of achieved average order size as a key factor in minimizing travel distance. The mixed integer non-linear programming (MINLP) model specifically designed to offer multiple local optimal solutions by varying defined criteria. Additionally, we have developed a simulation-based model to evaluate the performance of various scenarios. Unlike other methods that rely on heuristic or meta-heuristic algorithms, we simplify the complexity of the MINLP problem and incorporate the integrated heuristic procedures within the MINLP solver to expedite the convergence. This approach reduces problem complexity and enables efficient exploration of the solution space. Furthermore, we have applied other techniques to simplify and optimize the convergence of the MINLP model. For instance, rather than optimizing travel distance by incorporating historical order demand of significant volume (order x item) to directly calculate the achieved average order size or total trips, we employed a correlation frequency matrix (item x item) and utilized the item picking frequency information available in that matrix. The simplified matrix not only provides significantly reduced memory usage, but also encompasses all the necessary information for minimizing total trips and influencing the average order size per zone indirectly. By employing this matrix, we were able to effectively minimize computational consumption while still achieving optimal outcomes. Those techniques have proven to be highly effective in expediting the convergence to achieve specific targets based on defined ratios, which can be extended to other optimization models such as resource allocations. The optimization model is designed to offer seamless integration with existing warehouse strategies. The model maximizes the overall zone correlation score while considering deviations from weighted centroids. To accurately measure deviations, we implemented two methods within our penalty term: Positive Centroid Deviation (PCD) and Negative Centroid Deviation (NCD). The model can achieve multiple local optimal solutions based on predefined zone ratios for correlation score and picking frequency. The main objective is to prioritize maximize the correlation score while minimizing the picking frequency for the zones farthest from the depot. This approach enables us to implement an item allocation strategy that increases the average order size for these distant zones. Conversely, we prioritize minimizing the correlation score and maximizing the picking frequency in the closest zones, resulting in frequent trips and shorter average order size. By considering the average order size as a key factor in our optimization model, we effectively minimize the travel distance and enhance operational efficiency. This ultimately leads to a significant reduction in overall travel time by decreasing the need for pickers in distant zones to frequently travel to the staging area. To evaluate the performance of our

approach, we conducted simulations to test various scenarios in terms of total travel distance achieved. The results demonstrate significant performance improvements, with reductions in travel distance of up to 36.75%, and a sustainable improvement of 33.59% reduction for recent data. This research contributes to the existing literature on order picking optimization and provides valuable insights into addressing the limitations associated with correlated strategies. By offering a simplified problem-specific approach, we aim to enhance order picking operations, improve efficiency, and shed light on the challenges involved in implementing such methodology.

The paper is structured into six sections to effectively address the research objectives. The Literature Review (Section 2) summarizes related work. The Problem Settings (Section 3) offers a comprehensive understanding of the research framework. The Methodology (Section 4) includes a Simulation Model (Section 4.1) and a Mathematical Programming Model (Section 4.2). The Optimization Result Analysis (Section 5) highlights the outcomes and performance of proposed CSAS. Finally, the Conclusion (Section 6) summarizes key findings.

2. Literature Review

Casella et al. (2023) examine the topic of order picking to highlight emerging trends. Their analysis covers storage allocation policies, and emphasizes the lack of research on correlated storage assignment. Islam and Uddin (2023) provide another review to summarize techniques for solving correlated storage location assignment problems (CSLAP) that mostly expressed as NP-hard integer programming models. The authors review 60 publications and categorize solution methods as heuristic, meta-heuristic, and data mining approaches. This assignment method is found to be more effective in reducing travel distance compared to other storage allocation systems, as indicated by several studies including Zhang et al. (2019) and Lee et al. (2020). According to the review, the objective functions in these studies aim to minimize total travel distance (Wutthisirisart et al., 2015; Diaz, 2016; Xie et al., 2018; Krishnamoorthy & Roy, 2019; Zhang et al., 2019; Jiang et al. 2021; Li et al., 2021; Yuan et al., 2021; Trindade et al., 2022), minimizing travel time (Mirzaei et al., 2021a, 2021b), and maximizing correlation between stock keeping units (SKUs) (Lee et al., 2020; Yang, 2022). De Koster et al. (2007) highlight the importance of zoning as an effective strategy for optimizing order picking processes. Zoning involves dividing the order picking area into specific zones and assigning dedicated pickers accordingly. The advantages of this approach include reduced travel distance for each picker, decreased traffic congestion, and enhanced familiarity with item locations. Two methods, progressive assembly (pick-and-pass) and synchronized picking, can be used to overcome the challenge of consolidating orders before shipping. Product properties such as size, weight, temperature requirements, and safety are considered for effective implementation of zoning. Mantel et al. (2007) introduces the Order Oriented Slotting (OOS) strategy, which aims to optimize item allocation for multi-item orders to minimize the travel distance. The authors classify slotting strategies into item-oriented such as the Cube per Order Index approach (COI), and order-oriented approaches such as OOS, with correlated storage lying in between. They note that OOS does not work well together with order batching and extensive zoning, and it performs best when an average order consists of a moderate number of SKUs to be picked. The author suggests implementing a method for storage assignment that is optimal for both frequent single-item orders and multi-item orders. Wutthisirisart et al. (2015) present a two-phased heuristic algorithm for relation-based item assignment to minimize the travel distance. The algorithm considers item correlation and order characteristics, such as order frequency and size, to allocate items. Zhang (2016) implements clustering-based algorithms using a correlation frequency matrix to optimize travel distance. Kuo et al. (2016) developed metaheuristic algorithms to implement the CSAS in a synchronized-zone order picking system. Their model minimizes the sum of item correlation frequencies across zones, aiming to reduce idle time and increase utilization rates by assigning highly correlated items to different zones, picked simultaneously by multi pickers. However, this approach increased workload and travel distance. The authors recommended further studies to balance the trade-off between utilization and workload. Diaz (2016) examines the impact of customer demand patterns and order clustering on warehouse order-picking operations. The author proposes a heuristic optimization approach that

considers physical restrictions, such as non-uniform density SKUs. Xie et al. (2018) presents a bi-level optimization model with grouping constraints. Experimental results validate the effectiveness of the model and the superiority of the tabu search method over random search. Krishnamoorthy & Roy (2019) introduce a storage assignment strategy that utilizes a top-k high utility itemset mining technique and a heuristic algorithm to assign items effectively. Zhang et al. (2019) present an integer programming model using heuristic and simulated annealing methods that considers item correlation. The study by Lee et al. (2020) introduces a correlated and traffic balanced storage assignment. It minimizes travel time and congestion by clustering items based on travel efficiency and traffic flow balance. Using multi-objective evolutionary algorithms, the authors identified clusters, followed by implementing an optimized assignment. In their case study, the model outperformed random, class-based, and correlated approaches. Jiang et al. (2021) implemented a storage strategy that allows product to be stored in multiple locations, taking into account their co-occurrence in orders. The problem is formulated as an integer programming model to minimize the weighted sum of distances between products. The paper by Li et al. (2021) introduces a heuristic method that utilizes data mining to optimize order picking distance. It focuses on grouping similar items and considering nonuniform product weights. Yuan et al. (2021) present an optimization approach for storage assignment in a Robotic Mobile Fulfillment System (RMFS). Their method improves order picking efficiency by reducing pod visits, optimizing travel distance, and mitigating system congestion. Mirzaei et al. (2021b) propose an integrated cluster allocation method that incorporates product affinity and product turnover information to assign related products to the same storage location. This approach reduces retrieval time by up to 40% compared to conventional storage policies. The authors (2021a) propose a comprehensive approach that considers turnover frequency, product correlation, and inventory dispersion strategies to minimize order picking travel time in automated systems. They develop a mathematical model and heuristic method to allocate products to clusters and zones effectively. The test demonstrates that correlated dispersed assignment results in shorter travel times for larger order sets compared to random, turnover frequency-based, correlated assignment strategies. Trindade et al. (2022) proposed a heuristic approach for optimizing the storage location assignment in multi-aisle warehouses through product clustering. Their method addresses challenges related to non-uniform products and incorporates additional allocation criteria. The results demonstrated a potential reduction of travel distance by up to 15%. Yang (2022) examines the impact of storage assignment and order batching policies on order picking in RMFS. The author proposes using order and item similarity to batch orders and assign storage locations. Numerical tests reveal that weighted support count-based storage allocation combined with correlation-based order batching yields optimal performance. Adaloudis (2023) examines different methods for optimizing the storage assignment of autonomous mobile robot systems. Three optimization approaches are developed: correlation-based heuristic, product characteristic-based clustering, and surrogate-based genetic algorithm. A simulation model is employed to evaluate their effectiveness, with the clustering method based on product characteristics showing the most significant improvement. The surrogate-based genetic algorithm also demonstrates solid performance, while the correlation-based heuristic has the lowest performance among the three methods.

Many authors follow a common approach in storage assignment policies by locating frequently accessed items near the depot. Buckow and Knust (2023) propose algorithms and optimization techniques to reduce travel distances in a high-bay warehouse with an automated storage and retrieval system (AS/RS) by rearrange the pallets based on their turnover rates within a limited reshuffling time. Yuan et al. (2023) present a three-stage method to optimize the storage allocation assignment of automated drug dispensing machines in smart pharmacies. The method considers the daily demand to enhance space utilization, drug grouping using the Jaccard similarity coefficient to preventing cross-machine picking, and allocation optimization based on demand frequency to reduce picking time. Other researchers have also addressed travel distance optimization by considering multiple problems simultaneously. Kim et al. (2020) present heuristic methods to optimize the item storage assignment to minimize travel distance for order pickers. The authors propose slot selection

and frequent itemset grouping strategies based on association rule mining. The paper also introduces a flexible routing policy to further enhance the efficiency of the system. Zhang et al. (2024) propose a joint optimization of item and pod storage assignment problems in robotic mobile fulfillment systems by considering the correlation frequency of items in purchase orders. Their main objective is to minimize the robots' travel distance and ensure workload balance to avoid congestion. Additionally, the authors developed a genetic algorithm to solve the mixed integer programming model. Wan et al. (2022) present an integrated optimization for order picking systems by addressing layout optimization, storage location assignment, and picker routing. The authors propose a three-dimensional design for a fishbone layout, aiming to minimize the average distance between storage locations and the depot. They also establish storage location assignment models based on turnover and correlation storage policies and employ the TSP to plan picker routing. In order to solve the multiobjective optimization model, the authors design a cooperative optimization algorithm (COA) that improves the average optimal travel distance by 9% with consistency. They conclude that the fishbone layout can reduce picking distance by 10-15% without considering aisle congestion. Bolaños-Zuñiga et al. (2020) propose a mathematical model to address the integrated Storage Location Assignment, Unique, Picker-Routing (SLAUPR) problem and minimize travel time. One crucial aspect of the SLAUPR model is the inclusion of precedence constraints. By considering these constraints, the model ensures that the picking sequence is optimized to handle heavier items while maintaining overall process efficiency. The authors highlight that this integrated optimization model distinguishes their work from previous research, which often focused on specific optimization factors or relied on heuristic methods. Computational experiments conducted for the case study demonstrate that the mathematical model produces optimal solutions for small and medium-sized instances but faces challenges with larger instances. Consequently, the paper suggests further research to tackle the problem's complexity and explore additional enhancements. A subsequent study conducted by Bolaños-Zuñiga et al. (2023) aimed to refine the SLAUPR model while addressing the computational challenges highlighted in the earlier case study involving 185 available storage locations (Bolaños-Zuñiga et al., 2020). The authors introduce two formulations: SLAUPR_V2, which incorporates valid inequalities, and SLAUPR_V3, which incorporates single commodity flow constraints to eliminate sub-tours. Additionally, the authors developed an adaptive multi-start heuristic (AMH) that utilizes an evaluation function defined by the demand frequency and weight of products. This AMH serves as an approximation method to improve computation time for larger instances. The experimental results demonstrated the effectiveness of the proposed algorithm and models, with an increased number of feasible and optimal solutions. The average time required to obtain the feasible solutions is reduced to 117 seconds. Moreover, the product allocations suggested by the proposed heuristic resulted in a significant improvement of over 40% in picking times.

The MINLP is a branch of mathematical optimization that involve continuous and integer variables, as well as non-linear relationships between these variables. Berthold (2014) emphasizes the necessity of MINLP models in addressing wide range of real-life applications, which possess inherent nonlinear characteristics. The author acknowledges the vital role of heuristic algorithms as integral components of advanced solvers for such problems. One of the commercial tools that includes solvers for MINLP problems is Lingo software. The specific details of how the solvers operate may vary depending on the version and specific settings used, including the option for the solver to decide. However, Lingo's solver takes a typical approach for solving MINLP problems that includes employing a branch-and-bound algorithm, which is a common technique used for solving MIP problems. During the branch-and-bound process, the solver may apply various heuristics to guide the search for feasible solutions and improve the efficiency of the algorithm (Lindo Systems Inc., 2020). Tahami and Fakhrafar (2022) highlight the advantages of combining heuristics with exact algorithms for solving optimization problems. They note that exact algorithms guarantee optimal solutions but can be limited by their problem-specific nature and high memory consumption. On the other hand, heuristics aim to find good approximate solutions in a reasonable amount of time, providing scalability and flexibility. The study also notes that most branch-and-bound approaches rely on heuristics for bounding, and many hybrid approaches are heuristic-based.

This paper builds upon previous work in order picking optimization and aims to contribute to the existing research by addressing gaps in the field. We propose a new approach that minimizes travel distance in a synchronized-zone, single-order picking system by considering the average order size as a key factor. We implemented the CSAS using a MINLP model that is solved by the Branch and Bound algorithm. In our study, we made several key findings and recommendations. Firstly, we propose optimizing item correlation across zone by offering flexibility in identifying multiple local optimal solutions based on predefined criteria. This approach aims to address different real-world case scenarios to fulfill their priorities in achieving balanced workload in terms of travel distance. Additionally, we address the problem of order splitting by decrease total trips to distant zones, while increasing frequently ordered smaller lists at closer zones. This is achieved by considering both the total zone correlation score and picking frequency to optimize the allocation of items. This approach effectively minimizes travel distance by prioritizing distant zones with larger average order sizes, thereby reducing order splitting and number of trips to the depot. Finally, we suggest implementing an optimal item ranking method for both single-item and multiple-item orders, taking into account the average order size of each item. By incorporating these strategies, the travel distance within the order picking system can be substantially minimized. This reduction will ultimately result in enhanced efficiency and productivity in warehouse operations.

3. Problem Settings

In this paper, we optimize the travel distance in a pharmaceutical distribution center's synchronized-zone, single-order picking system by implementing the CSAS based on an item correlation matrix constructed from 15 months of historical data. According to Goetschalckx and Ashayeri (1989), the complexity of an order picking system is influenced by both internal and external factors. Internal factors, such as information availability, warehouse dimensionality, routing, storage, batching, and zoning, contribute to this complexity. These factors can be categorized into two levels of decision-making as shown in Figure 1.

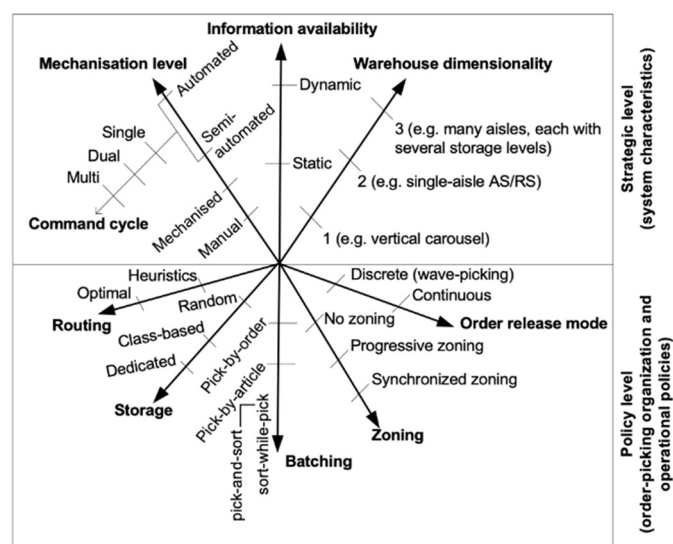


Figure 1. Complexity of the Order Picking System Based on the Dimensionality of Internal Factors as Presented by Goetschalckx and Ashayeri (1989).

At the policy level, several decisions greatly impact order picking performance. These decisions encompass five key areas: storage assignment strategy, zoning, routing, batching, and order release mode. Le-Duc (2005) defines these decisions as follows: Storage assignment strategy refers to the rules used to allocate products to specific storage locations, such as random, class-based, and dedicated storage assignments. Zoning involves dividing the order picking area into zones and assigning pickers to specific zones to reduce traffic congestion and travel distance, following either progressive or synchronized zoning approaches. Routing determines the sequence in which items

are picked, utilizing methods like s-shape, return, mid-point, largest gap, combined, and optimal routing. Batching involves either picking orders individually or combining multiple orders in one tour, with approaches such as sort-while-pick employed when order splitting is not allowed. If order splitting is possible, sorting is done after the picking process is complete (pick-and-sort). The order release mode consists of discrete (wave-picking) and continuous methods, where wave picking releases multiple orders with a common destination for picking in multiple warehouse areas. Typically, wave picking is combined with batch picking, and the next picking wave begins after the previous one is finished. The compatibility of these operational policies significantly affects the performance of the order picking system. Therefore, when considering the scope of an optimization problem, it is important to consider the combination of all related policies. This ensures that the proposed solution is applicable to similar systems and allows for further improvements in future related work. In this case study, the current order picking system relies on manual operations supported by a Warehouse Management System (WMS) and handheld devices, following a single-order method, synchronized zone picking policy (Figure 2), and return routing strategy (Figure 3).

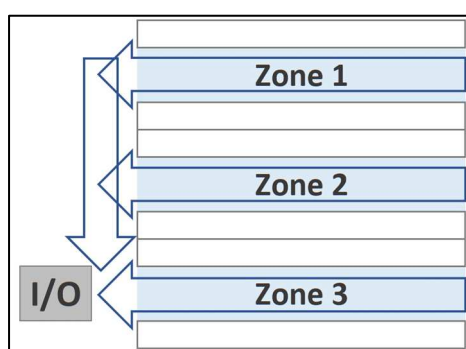


Figure 2. Zone Strategy.

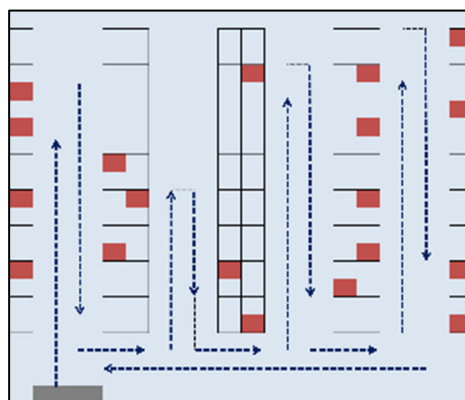


Figure 3. Return Routing.

The existing storage assignment approach combines class-based and random assignments, fast-moving (148) items are stored randomly in a block area closer to the depot, while slow-moving (211) items are placed further away (Figure 4). In order to optimize the storage allocation, the CSAS has been implemented along with the existing class-based method, replacing the random storage approach. To achieve this optimization, a MINLP model has been developed to minimize travel distance for each classed-based single-block storage area with a conventional layout (Block A & B). The model employs the solver's integrated heuristics algorithms to better explore the solution space. To make the problem more manageable, each block in the warehouse has its own model using a simplified data-driven approach, in addition to following an efficient method that indirectly impacts the travel distance without calculating the actual distance from the depot. The model takes into account the number of items allocated in each zone and incorporates other defined criteria for

balancing resource utilizations in terms of distance. By considering these constraints, the storage allocation is optimized according to the actual framework of the order picking system.

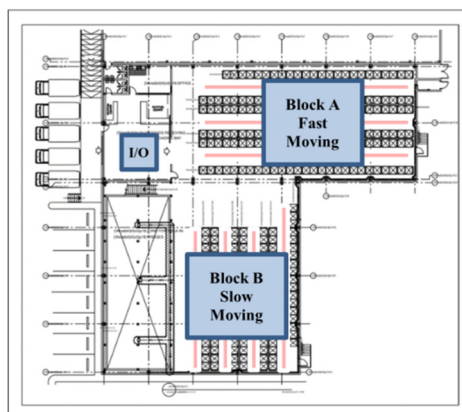


Figure 4. The Distribution Center Layout.

Additionally, a simulation model has been developed using FlexSim to evaluate the performance of the proposed item storage assignment. This simulation model was designed to offer maximum flexibility by allowing the testing of various historical data sets and experimenting with different arrangements for item storage assignment.

4. Methodology

Designing an MINLP model to converge to optimal solution is challenging, especially when implementing precise constraints. This is primarily due to the presence of non-convexity, which leads to multiple local optimal solutions. Additionally, the complexity introduced by integer variables and nonlinear functions, along with the difficulties in satisfying constraints using approximation techniques. Moreover, the impracticality of exploring the entire search space due to high dimensionality which add to the computational demands of MINLP problems, making it harder to attain globally optimal solutions. To improve the efficiency of solving MINLP problems, several strategies can be employed. These include problem reformulation, variable fixing, decomposition techniques, preprocessing, and model simplification methods. Problem reformulation involves transforming the original MINLP problem into a more manageable form, such as a MILP problem or a convex optimization problem. By reformulating the problem, we can take advantage of existing algorithms and solvers that are better suited for faster computational times. Variable fixing is another useful strategy that involves identifying variables with known values and fixing them at those values. This reduces the search space and eliminates unnecessary computations. Decomposition techniques involve breaking down the MINLP problem into smaller subproblems, which can be solved independently. This allows for parallelization and the use of specialized solvers for each subproblem, leading to faster convergence. Preprocessing and model simplification techniques enhance solver efficiency through the analysis of the problem structure and the elimination of redundancy. This reduces complexity and removes unnecessary constraints or variables, resulting in a more streamlined and tractable problem that improve solver performance. By employing these strategies, we can enhance computation speed, reduce complexity, and improve efficiency when solving MINLP problems.

This paper introduces optimization techniques for storage allocation, incorporating the concept of weighted centroids as targets for each zone. By utilizing correlation score ratios and frequency ratios as coefficients, we have the ability to effectively influence the distribution of items among zones by satisfying specific criteria that directly impact the average order size. The incorporation of these weighted centroids is instrumental in driving convergence towards preferred outcomes and effectively addressing diverse scenarios. Consequently, this technique offers exceptional flexibility and adaptability, making it highly suitable for testing and validating different correlated storage

arrangement. Additionally, we follow an efficient methodology by breaking down the process into sub-problems and employing separate models for the class-based blocks, A and B. Furthermore, we utilize the Branch-and-Bound algorithm, which is employed by Lingo's MINLP Solver, to narrow down the search for the local optimal solution. This algorithm reduces computational complexity and improves overall efficiency by partitioning the solution space and bounding the objective function value in each partition. To further enhance memory consumption, we import the correlation frequency matrix (item x item) directly into our model, eliminating the need to generate it from the order history data during runtime. This matrix allows us to evaluate different arrangements and assign items to zones based on defined correlation score and picking frequency. Unlike traditional methods that solely aim to maximize the total correlation score, our approach considers the impact of average order size. We control the distribution of items by defining the ratios of total correlation score and total picking frequency at each zone as key factors in optimizing the travel distance. Instead of relying on iterative processes and extensive calculations using a large volume of order history records to estimate the average order size, which can render the model infeasible, we incorporate the total picking frequency by summing the diagonal values available in the matrix for all items that are correlating with themselves. This significantly simplifies the process without compromising the model's accuracy. By evaluating the performance in terms of travel distance achieved for different ratios of these key factors, we highlight the impact of the average size of newly generated orders or sub-orders across zones. This average is influenced by the proposed item allocation to zones within the model. It negatively correlates with the total picking frequency and positively correlates with the total correlation score. Therefore, higher ratio of correlation score and lower ratio of picking frequency indicate larger average order size. In this case study, we prioritize the placement of items based on these factors. Contrary to traditional methods that allocate items of higher correlation closer to the depot, we strategically place items that collectively achieve higher average order size in distant zones to minimize travel distance. This optimization approach ensures workload distribution based on distance, reducing the need for pickers assigned to further zones to frequently travel to drop items at the staging area. As a result, overall travel time for pickers is reduced, leading to improved efficiency. In mathematical modeling, we propose the utilization of the Positive Deviation (PD) measurement as an effective penalty for achieving a target in maximizing problems. This approach penalizes positive deviations and quantifies negative ones within feasible solutions. It facilitates rapid convergence towards maximizing the objective function to reach a specific target, while penalizing any deviation beyond that target. Similarly, the Negative Deviation (ND) measurement is an effective method for targets in minimizing problems. We use formulas for these measurements rather than functions or logical conditions to facilitate better convergence. The ND and PD are calculated to determine deviations from targeted weighted averages, referred to as centroids. These measurements quantify each state and guide the solver towards reaching targets rather than strictly penalizing all deviations. By incorporating both PD and ND in our penalty terms, we are able to achieve targeted centroids that exhibit a positive correlation. By utilizing the ND, we prevent the centroid from decreasing below the target and allow it to increase, while by utilizing the PD we discourage the centroid from increasing above the target and permit it to decrease. This approach yields better results by driving the convergence towards finding a local optimal solution that maximizes specific centroids while simultaneously minimizes others to distribute items that satisfies these specific criteria, which is opposing to their correlated relationship. By implementing ND and PD, we observed a significant improvement in convergence speed – approximately 3.5 times faster compared to using absolute deviation. The solving time is further influenced by the penalty parameter, which determines the balance between accuracy in achieving targets and allowing for deviations to maximize the overall correlation score. A higher penalty parameter promotes more accuracy, but requires more time to converge to the local optimal solution. Balancing this trade-off allows us to control the extent to which the deviation is permitted in maximizing the total score while still aiming for the desired ratios per zone. The main objective of the MINLP model is to propose item assignments across zones without explicitly ranking them within each zone. However, our research paper investigates different ranking methods and reveals that those based on the average order size

of items within each zone have shown better results in optimizing travel distance. By prioritizing frequently ordered items that are less dependent on other items, the item ranking methods effectively minimize travel distance, resulting in a more efficient item storage assignment. We integrate all these strategies with the objective of minimizing memory consumption and computation time to achieve better optimization results. By doing so, we are able to achieve multiple local optimal solutions based on desired ratios in an average solving time of 14 minutes. To evaluate the effectiveness of our approach, we conducted a simulation-based model of the order picking system to compare the total travel distance achieved using our methodology against the current system statistics. The results demonstrated a remarkable improvement in performance, with reductions in travel distance of up to 36.75%. To further validate our approach, we also evaluated the results of recent historical order data to test the sustainability of the optimization. The results showed significant reductions of up to 33.59%. To sum up our methodology, we follow a systematic approach consisting of several steps (Figure 5).

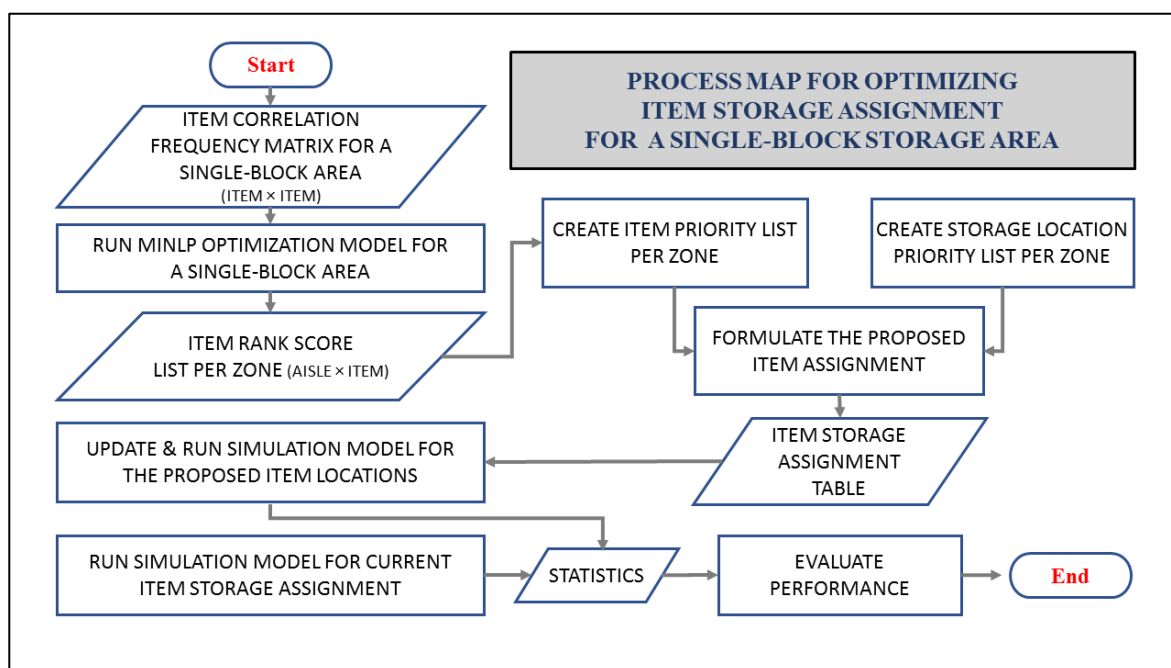


Figure 5. Process Map.

We begin by constructing a simulation model and developing a mathematical programming model. Followed by formulating a storage location priority list and implement CSAS based on our optimization model utilizing an item ranking method that is optimal for both single-item and multi-item orders. Through this process, we optimize the total travel distance and achieve desired workload balance among pickers in terms of distance versus frequency of trips.

4.1. Simulation Model

A simulation model was developed using FlexSim software to evaluate the performance of the order picking system under different scenarios. The model captured workload distribution, resource utilization, and travel distance performance. The first step in modeling involved building a virtual environment that closely represents the system's layout. This is done by scaling the 3D model based on the distribution center's floor plan to provide accurate travel distance statistics and precise placement of objects. The model includes a total of 13 racks, one transporter assigned at each of the 7 zones\aisles, a queue for the depot\staging area, navigation networks, and a storage system to retrieve and assign items by slot address (Figure 6).

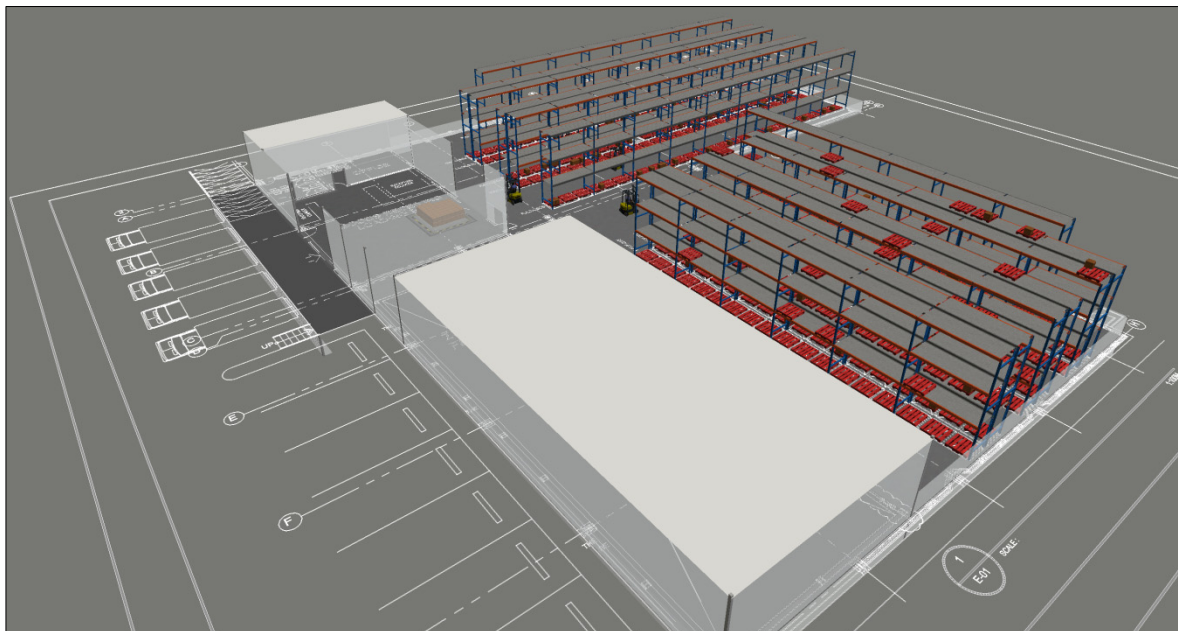


Figure 6. 3D Simulation Model.

In order to capture the idle time caused by the picker's waiting time after completing the picking task for the day, we define a "zero" speed value for loading and unloading activities in the simulation model. Furthermore, we made the assumption that the volume of item picking would not interrupt the trip due to any capacity constraints. This allowed us to accurately reflect the optimization performance of the proposed item storage assignment. An essential step in designing our model is generating dynamic global tables from primary ones during the simulation runtime in order to incorporate the dynamic aspects of the system and enable experimentations (Figure 7). These tables contain order volumes, trip-related information, and item locations based on proposed item storage assignments.

Address Table

	Block_Sequence	Block	Address	Aisle	Rack	Bay	Slot	Level
1		1 A	A01.002.0A1		1	1	2	1
2		2 A	A01.002.0A2		1	1	2	2
3		3 A	A01.002.0A3		1	1	2	3
4		4 A	A01.003.0A1		1	1	3	1
5		5 A	A01.003.0A2		1	1	3	2
6		6 A	A01.003.0A3		1	1	3	3
7		7 A	A01.004.0A1		1	1	4	1
8		8 A	A01.004.0A2		1	1	4	2

ItemPermutation Table

	ItemCode	Block	Block_Sequence
1	6017 A		1
2	3007 A		2
3	12253 A		3
4	22119 A		4
5	12133 A		5
6	12402 A		6
7	3384 A		7
8	3058 A		8

OrderHistory Table

	Day	OrderNo	ItemCode	Qty
1		1	851840	1377
2		1	851841	3058
3		1	851841	22064
4		1	851841	19324
5		1	851841	13045
6		1	851841	3252
7		1	851841	26055
8		1	851841	6068
9		1	851841	19158
10		1	851841	12233

Figure 7. Primary Global Tables.

Another essential component is the design includes the creation of the process flow logic of the picking system that was defined by composing and coding the activity blocks within the simulation model (Figure 8).

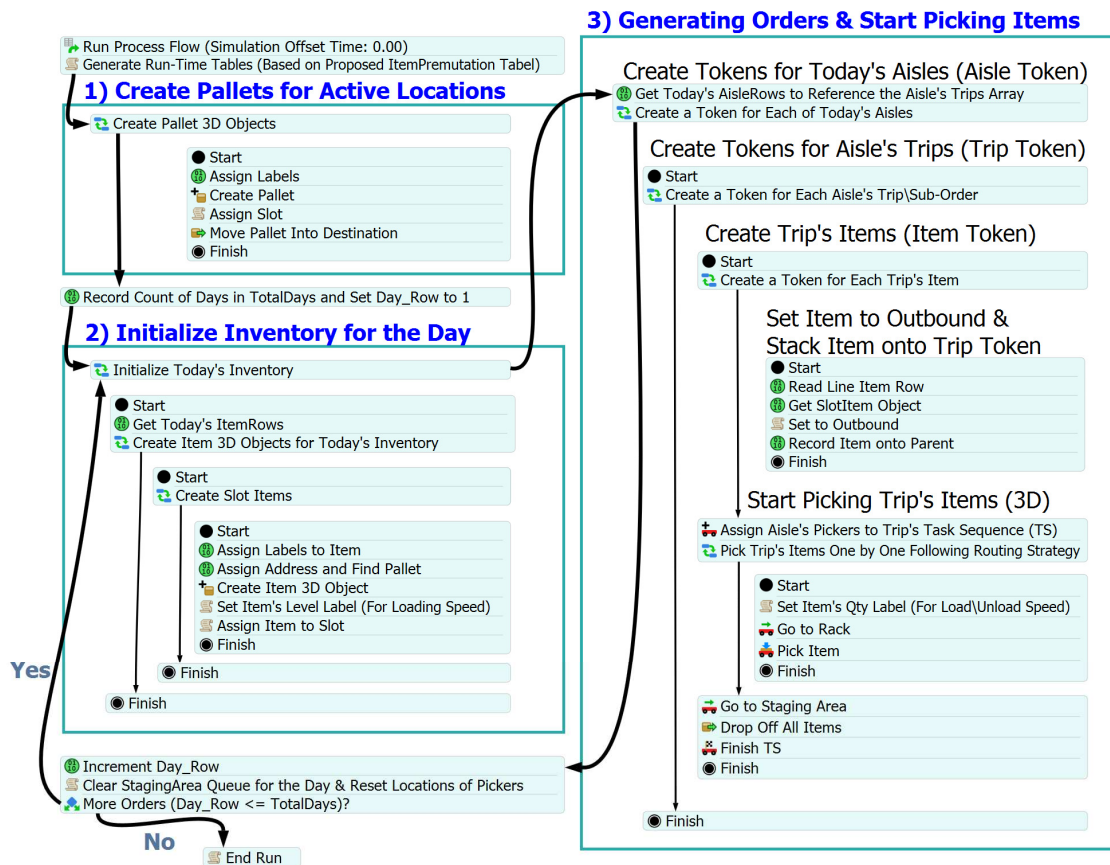


Figure 8. Process Flow Logic.

These activity blocks represent the sequence of actions and tasks performed in the system such as generating dynamic tables, assigning picking lists to pickers, finding item addresses, and terminating the simulation process. Accurately modeling the process flow enables the simulation of activities based on the dependencies of the model components. Finally, a statistics dashboard was constructed within the simulation model to measure and evaluate the performance of the picking system. The dashboard captures key performance indicators such as total travel distance and resource utilization (Figure 9).

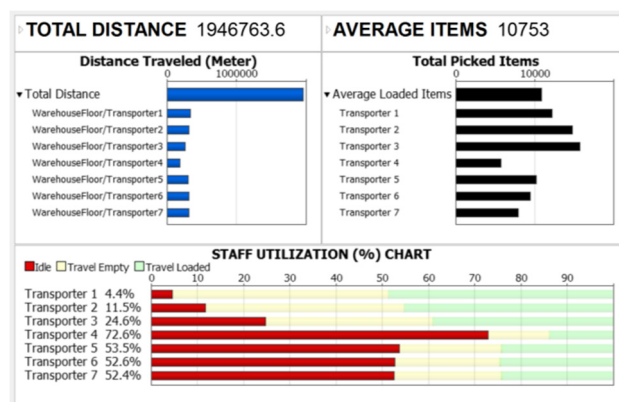


Figure 9. Simulation-Based Statistics (Current).

4.2. Mathematical Programming Model

There are various ways to convey a problem statement and its solution when presenting an optimization model. The common approach is to express the problem using simplified math

equations to provide a concise representation. However, in this section, we start with presenting the code in Lingo's mathematical modeling language. This approach offers several advantages in terms of readability, usability, and the understanding of the potential impact of the problem formulation on the solver's performance. This allows us to include annotations, which can provide additional explanations as presented in "Model E: Lingo Optimization Code (Block A)". A MINLP model is created for each single-block to maintaining the current class-based storage blocks for fast-moving and slow-moving items while implement the proposed CSAS. The optimization aims to maximize the total zone correlation score while penalizing deviations from weighted averages, referred to as centroids in this model. By defining centroids from achieved total correlation score and total picking frequency based on ratios, we can conduct scenario analysis to examine their influence on travel distance optimization. To better measure deviation from centroids and refine the objective function, we have introduced the utilization of PD and ND as a more effective alternative penalty terms for achieving targets. These measures aim to address the positive or negative sources of deviation, particularly to prohibit it from increasing beyond or below a target. The purpose of this approach is to quantify the feasible solution to allow for better comparison against other states while approaching the target from the opposite side of deviation. By incorporating deviation penalty terms, we can expedite convergence towards maximizing the objective function that ultimately lead to higher total correlation score in addition to achieving specific targets.

```

MODEL:

SETS:

    ITEMS;

    AISLES / 1..3 /: SLOTS, D_SIGN_R, D_SIGN_P, CORR_SCORE_RATIO, PICKING_RATIO, R_CENTROID_COEF,
    P_CENTROID_COEF, R_CENTROID, P_CENTROID, R_D, P_D, TOTAL_ZONE_CORR_SCORE, TOTAL_ZONE_PICKING_COUNT;

    IXI (ITEMS, ITEMS): CORR_FREQ_MATRIX;

    AXI (AISLES, ITEMS): AISLE_SELECTED_ITEMS, AISLE_ITEM_SCORE;

ENDSETS

DATA:

    !IMPORT CORRELATION FREQUENCY MATRIX AND ITEMS ARRAY;

    ITEMS, CORR_FREQ_MATRIX= @OLE('C:\...\Block_A_Lingo_Optimization_ItemMatrix.xlsx', 'ITEMS', 'ITEM_ITEM');

    !EXPORT RANKING SCORE (SUM OF CORRELATION SCORE AND PICKING FREQUENCY);

    @OLE('C:\...\Block_A_Lingo_Optimization_ItemMatrix.xlsx', 'AISLE_ITEM_RANK')= @WRITEFOR(AXI(K,A):

    @SUM(ITEMS(B): CORR_FREQ_MATRIX(A,B) * AISLE_SELECTED_ITEMS(K,A) * AISLE_SELECTED_ITEMS(K,B) ));

    D_SIGN_R = -1 -1 -1; !NCD FOR CORRELATION CENTROIDS;

    D_SIGN_P = +1 +1 +1; !PCD FOR PICKING FREQUENCY CENTROIDS;

    CORR_SCORE_RATIO = 3 2 1; !DEFINE CORRELATION SCORE RATIOS;

    PICKING_RATIO = 1 2 3; !DEFINE PICKING RATIOS;

    T_RATIO_UNITS = 6;

    SLOTS = 45 49 54; !AVAILABLE SLOTS AT ZONE 1, 2, 3;

    T_SLOTS = 148; !TOTAL NUMBER OF STORAGE SLOTS;

    N_AISLES = 3; !TOTAL NUMBER OF ZONES;

    t=10; !PENALTY PARAMETER;

ENDDATA

    !OBJECTIVE FUNCTION;

```

```

MAX = @SUM(AISLES(K): TOTAL_ZONE_CORR_SCORE(K) + ( ( ( R_D(K)/(t* R_D(K)+1) ) - 1 ) * R_D(K) ) +
( ( (P_D(K)/(t*P_D(K)+1) ) - 1 ) * (P_D(K) * (TOTAL_SCORE /TOTAL_PICKS) ) ) ) );

!ASSIGN SCORES TO ITEMS BY SUMMING ONLY FREQUENCIES OF ITEMS NEXT IN ORDER;
@FOR(AISLES(K): @FOR (ITEMS(A): AISLE_ITEM_SCORE(K,A) = @SUM(ITEMS(B) | B #GT# A: CORR_FREQ_MATRIX(A,B)*
AISLE_SELECTED_ITEMS(K,A) * AISLE_SELECTED_ITEMS(K,B) ));
@FOR (AISLES(K): TOTAL_ZONE_CORR_SCORE(K) = @SUM(ITEMS(I): AISLE_ITEM_SCORE(K,I) ));
TOTAL_SCORE = @SUM(AISLES(K): TOTAL_ZONE_CORR_SCORE(K));

!CALCULATE COEFFICIENTS FOR CORRELATION CENTROIDS ACCORDING TO SLOT RATIO & CORR_SCORE_RATIO;
@FOR (AISLES(K): R_CENTROID_COEF(K) = ( (SLOTS(K)/T_SLOTS) + (CORR_SCORE_RATIO(K)/T_RATIO_UNITS) )/2 );
!CREATE TARGET CORRELATION SCORE CENTROIDS BASED ON COEFFICIENTS;
@FOR (AISLES(K): R_CENTROID(K) = TOTAL_SCORE * R_CENTROID_COEF(K) );

!CENTROID DEVIATION FOR CORRELATION:
( |X-CENTROID| + (D_SIGN_R * (X-CENTROID)) ) /2;
@FOR (AISLES(K): R_D(K) = ( @ABS( TOTAL_ZONE_CORR_SCORE(K) - R_CENTROID(K) ) +
(D_SIGN_R(K) * (TOTAL_ZONE_CORR_SCORE(K) - R_CENTROID(K) ) ) ) /2 );

!SUM PICKING FREQUENCIES FOR SELECTED ITEMS PER ZONE;
@FOR(AISLES(K): TOTAL_ZONE_PICKING_COUNT(K) =
@SUM(ITEMS(A): AISLE_SELECTED_ITEMS(K,A) * CORR_FREQ_MATRIX(A,A));
TOTAL_PICKS = @SUM (AISLES(K): TOTAL_ZONE_PICKING_COUNT(K));

!CALCULATE COEFFICIENTS FOR PICKING CENTROIDS ACCORDING TO SLOT RATIO & PICKING_RATIO;
@FOR (AISLES(K): P_CENTROID_COEF(K) = ( ( (SLOTS(K)/T_SLOTS) + (PICKING_RATIO(K)/T_RATIO_UNITS) )/2 );
!CREATE TARGET PICKING FREQUENCY CENTROIDS BASED ON COEFFICIENTS;
@FOR (AISLES(K): P_CENTROID(K) = TOTAL_PICKS * P_CENTROID_COEF(K) );

!CENTROID DEVIATION FOR PICKING FREQUENCY:
( |X-CENTROID| + (D_SIGN_P * (X-CENTROID)) ) /2;
@FOR (AISLES(K): P_D(K) = ( @ABS(TOTAL_ZONE_PICKING_COUNT(K) - P_CENTROID(K) ) + (D_SIGN_P(K) *
(TOTAL_ZONE_PICKING_COUNT(K) - P_CENTROID(K) ) ) ) /2 );

@FOR (AXI(K,I): @BIN(AISLE_SELECTED_ITEMS(K,I)); !CONSTRAINT: BINARY VARIABLE;
@FOR(ITEMS(I): @SUM(AISLES(K): AISLE_SELECTED_ITEMS(K,I) ) = 1 ); !CONSTRAINT: ITEMS ASSIGNED TO ONE ZONE;
@FOR (AISLES(K): @SUM(ITEMS(I): AISLE_SELECTED_ITEMS(K,I) ) = SLOTS(K)); !CONSTRAINT: TOTAL ITEMS ASSIGNED
= AVAILABLE SLOTS;

```

MODEL E: LINGO OPTIMIZATION CODE (BLOCK A)

In mathematical programming models, the positive or negative deviation is commonly defined through logical conditions, or employing functions that determine the maximum or minimum value between the deviation result and the zero value since, to the best of our knowledge, there is no standard formula available to measure this deviation. However, when dealing with optimization

problems, the solvers translate the formulation into a mathematical representation. Therefore, to facilitate the calculation of these deviations and promote better convergence, we have employed the following simple formulas that enable the quantification of positive centroid deviation (PCD) and negative centroid deviation (NCD) for achieved score (x) and a targeted centroid (C):

$$PCD(x, C) = \frac{|x - C| + (x - C)}{2} \quad (1)$$

$$NCD(x, C) = \frac{|x - C| - (x - C)}{2} \quad (2)$$

To further refine our model, we incorporate a derivative-based deviation penalty term (P) that penalizes the deviations for each zone. The penalty parameter (t) adjusts the weight of the penalty term, striking a balance between maximizing the total correlation score and enforcing the desired weighted centroids per zone. We calculate the penalty (P) as a function of D , where (D) represents the PCD or NCD and (t) denotes the penalty parameter as presented in equation [3]:

$$P(D) = D \cdot \left(\frac{D}{t \cdot D + 1} - 1 \right) \quad (3)$$

By setting (t) to 10, the penalty approaches $(-\frac{9}{10} D)$ for larger deviations, resulting in higher accuracy for targeted ratios compared to setting (t) to 2, and the model converges in less solving time compared to using the absolute deviation measure. On the other hand, if we set (t) to 2, the solving time decreases and the objective function achieves higher correlation scores as the penalty term approaches $(-\frac{1}{2} D)$ due to reduced penalization. Although it may seem that the term $(\frac{D}{t \cdot D + 1} - 1)$ can be replaced by a fixed percentage, it actually plays a crucial role in expediting convergence. For instance, when solving one of the proposed scenarios in Model B with (t) set to 2, the solving time is 10 minutes and 53 seconds. However, replacing the term with $(-\frac{1}{2})$ increases the solving time to 27 minutes and 5 seconds, which is 2.5 times slower. It's important to note that both solutions are identical, but the difference in solving time demonstrates the formulation impact of the penalty term on the solver's performance. Overall, incorporating the penalty term with an appropriate penalty parameter allows us to fine-tune the model's performance, achieving targets while optimizing solving time.

In this section, we introduce Model E, which has been developed to assess the effectiveness of implementing CSAS in optimizing travel distance within an order picking system that utilizes a zoning strategy. The model incorporates weighting coefficients to guide convergence towards targeted correlation scores and picking frequencies. By adjusting the ratios of targeted centroids, the model enables customization of item correlation distribution across zones, effectively balancing workload according to different desired customizations. The primary objective of the model is to achieve various local optimal solutions based on these defined coefficients, maximizing item correlation per zone and consequently increasing the average order size. To further increase the average order size in distant zones, we propose reducing the total picking frequency of items in these zones. This can be achieved by prioritizing the placement of items that collectively exhibit higher correlation and lower picking frequency in distant zones. Such approach effectively reduces travel distance by minimizing the need for frequent travel to the depot, thereby optimizing the picker's travel distance. In the result section, we present several scenarios to analyze the model's performance by testing different parameter configurations. For instance, in a system with three zones where the first zone is the furthest from the depot, setting the correlation score ratio for the coefficients to 3:2:1 and the picking frequency ratio to 1:2:3, as in scenario fourteen, enables the model to find a local optimal solution that satisfies these criteria. This leads to larger average order sizes in distant zones, ultimately minimizing travel distance. To quantify deviations from the targeted centroids, the presented models employ penalization using either the PCD or the NCD. In Model E, NCD is applied for all correlation centroids, while PCD is applied for all picking frequency centroids. This arrangement allows correlation scores to surpass the defined centroids, but restricts picking frequency centroids from exceeding their targets. However, it's important to note that setting extreme

ratios and unattainable centroids may render this configuration unachievable. In such cases, when extreme targets are set, the model penalizes multiple targets and leans towards maximizing the total correlation score.

Here is the mathematical representation of Model B, D, and E:

$$\text{MAXIMIZE } Z = \sum_{k=1}^n C_k + X_k + Y_k \quad (4)$$

Subject to:

$$S_{ak} \in \{0,1\}, \quad \forall 1 \leq a \leq m, 1 \leq k \leq n \quad (5)$$

$$\sum_{k=1}^n S_{ak} = 1, \quad \forall 1 \leq a \leq m \quad (6)$$

$$\sum_{a=1}^m S_{ak} = L_k, \quad \forall 1 \leq k \leq n \quad (7)$$

L_k defined as the total available slots in zone k .

where:

$$C_k = \sum_{a=1}^m \sum_{a < b \leq m} (T_{ab} \cdot S_{ak} \cdot S_{bk}), \quad \forall 1 \leq k \leq n \quad (8)$$

T_{ab} is defined as the correlation frequency for item a and b .

$$S_{ak} = \begin{cases} 1, & \text{if item } a \text{ is selected in zone } k \\ 0, & \text{otherwise} \end{cases} \quad (9)$$

$$X_k = \left(R_k \cdot \left(\frac{R_k}{t \cdot R_k + 1} - 1 \right) \right), \quad \forall 1 \leq k \leq n \quad (10)$$

$$Y_k = \left(F_k \cdot \left(\frac{F_k}{t \cdot F_k + 1} - 1 \right) \cdot \left(\frac{\sum_{k=1}^n (C_k)}{\sum_{k=1}^n (P_k)} \right) \right), \quad \forall 1 \leq k \leq n \quad (11)$$

t is the penalty parameter set to a value of 10 in Model (E).

R_k is defined as the deviation from correlation centroid (CC_k) given achieved correlation score (C_k) and defined type of deviation i_k that is calculated by equation [12] for zone k :

$$R_k = \frac{|C_k - CC_k| + (i_k \cdot (C_k - CC_k))}{2} \quad (12)$$

$$i_k = \begin{cases} -1, & \text{if NCD is implemented for } CC_k \text{ in zone } k \\ +1, & \text{if PCD is implemented for } CC_k \text{ in zone } k \end{cases} \quad (13)$$

$$CC_k = \left(\sum_{k=1}^n C_k \right) \cdot e_k \quad (14)$$

e_k is defined as the weighting coefficient for correlation centroid (CC_k) for zone k .

F_k is defined as the deviation from picking centroid (PC_k) given achieved picking frequency (P_k) and defined type of deviation j_k that is calculated by equation [15] for zone k :

$$F_k = \frac{|P_k - PC_k| + (j_k \cdot (P_k - PC_k))}{2} \tag{15}$$

$$P_k = \sum_{a=1}^m (T_{aa} \cdot S_{ak}), \quad \forall 1 \leq k \leq n \tag{16}$$

T_{aa} is defined as the picking frequency for item a

$$j_k = \begin{cases} -1, & \text{if NCD is implemented for } PC_k \text{ in zone } k \\ +1, & \text{if PCD is implemented for } PC_k \text{ in zone } k' \end{cases} \tag{17}$$

$$PC_k = \left(\sum_{k=1}^n P_k \right) \cdot h_k \tag{18}$$

h_k is defined as the weighting coefficient for picking centroid (PC_k) for zone k

The objective function in equation [4] aims to maximize the sum of item correlation score (C_k) for each zone (k), while considering deviation penalty terms (X_k) and (Y_k), calculated using equations [10] and [11] respectively. For every zone (k), the deviations (R_k) and (F_k) in the penalty terms are calculated by equations [12] and [15] for the achieved item correlation score (C_k) and the picking frequency (P_k). These penalty terms account for the zone's correlation centroid (CC_k) and picking centroid (PC_k), based on the deviation types (i_k) and (j_k) that are defined for each zone. These terms are formulated using acceleration convergence technique, with a penalty parameter (t) set to 10 in Model E, resulting in approximately 90% penalization for each deviation. The decision variables (S_{ak}) in equation [5] are binary constraints representing the assignment of each item (a) to a zone (k) as in equation [9]. We ensure that the sum of (S_{ak}) for all zones (k) is equal to 1 for every item (a), restricting each item to be located in only one zone. This constraint is expressed in equation [6]. Furthermore, the sum of (S_{ak}) for all items is constrained by the value of L_k for each zone (k), as indicated in equation [7]. It should be noted that in the "E" model, the exported result for "Aisle_Item_Rank" is a combination of the item's correlation score and its picking frequency. This approach, referred to as method A, which was used initially for item ranking within zones. However, the presented results in Table 1 for scenarios under Model E demonstrate the incorporation of method C. This method takes into account the average order size that is calculated from the order history data. Furthermore, an acceleration technique, which was previously used by Kuo et al. (2016) in their model, is incorporated in this model. This technique involves calculating the item correlation only once for two correlated items, resulting in a more efficient computation process. As a result, the total zone correlation score achieved in the model represents half of the actual zone correlation score, as shown in Table 1. In this paper, however, the item correlation used in formulas for item ranking is defined as the sum of correlation frequencies for all items located in that particular zone.

Table 1. Optimization Result (Branch and Bound Solver Type).

#	MODEL	RANK	BLOCK	SOLVING TIME	ZONE	SCORE RATIO	PICKING RATIO	SLOT RATIO	SCORE WEIGHTING COEFFICIENT	PICKING WEIGHTING COEFFICIENT	SCORE ACHIEVED	AVERAGE SCORE	PICKING ACHIEVED	AVERAGE PICKING	SCORE CENTROID	PICKING CENTROID	SCORE CENTROID'S ABSOLUTE DEVIATION	PICKING CENTROID'S ABSOLUTE DEVIATION	PENALTY	OBJECTIVE FUNCTION	DISTANCE	%	DISTANCE (NEW DATA)	%
1	A	A	A	00:46:34	1	55	10	45	0.43	0.20	38,817	30,258	13,539	14,123	38,762.52	8,559.68	54.476	4,979.317	(10,830.23)	79,942.77	1,283,018.00	34.09%	392,416.40	31.97%
					2	30	30	49	0.32	0.32	28,481		13,287		28,642.56	13,369.14	161.561	82.137						
					3	15	60	54	0.26	0.48	23,475		15,543		23,367.91	20,440.18	107.086	4,897.180						
					100	100	148			90,773	42,369	90,773	42,369	323.123	9,958.634									
2	B	A	A	00:10:53	1	55	10	45	0.43	0.20	41,300	31,529	13,908	14,123	40,391.63	8,559.68	908.368	5,348.317	(6,478.33)	88,109.67	1,276,568.10	34.43%	391,744.60	32.09%
					2	30	30	49	0.32	0.32	29,953		13,245		29,846.35	13,369.14	106.651	-						
					3	15	60	54	0.26	0.48	23,335		15,216		24,350.02	20,440.18	-	-						
					100	100	148			94,588	42,369	94,588	42,369	1,015.019	5,348.317									
					1	15	10	45	0.23	0.20	15,955	34,055	11,238	14,123	23,193.99	8,559.68	-	2,678.317						
					2	30	30	49	0.32	0.32	32,341		14,149		32,236.88	13,369.14	104.116	779.863						
					3	55	60	54	0.46	0.48	53,868		16,982		46,733.13	20,440.18	7,134.873	-						
100	100	148			102,164	42,369	102,164	42,369	7,238.989	3,458.180														
3				00:10:00	1	15	10	45	0.23	0.20	15,955	34,055	11,238	14,123	23,193.99	8,559.68	-	2,678.317	(7,789.69)	94,374.31	1,294,600.40	33.50%	402,337.70	30.25%
					2	30	30	49	0.32	0.32	32,341		14,149		32,236.88	13,369.14	104.116	779.863						
					3	55	60	54	0.46	0.48	53,868		16,982		46,733.13	20,440.18	7,134.873	-						
					100	100	148			102,164	42,369	102,164	42,369	7,238.989	3,458.180									

showcases the performance on fitted data as well as recent data. By validating the optimization process against both datasets, we can determine the effectiveness and sustainability of the model.

SCENARIO #	MATHEMATICAL MODEL					ITEM RANKING METHOD
	MODEL	CORRELATION DEVIATION	PICKING DEVIATION	PENALTY TERM	PENALTY PARAMETER (t)	
01	A	Absolute Centroid Deviation (ACD)	Absolute Centroid Deviation (ACD)	Penalize (-)	2	A
02-07	B	Positive Centroid Deviation (PCD)	Positive Centroid Deviation (PCD)			
08-09	C	Positive Mean Deviation (PMD)	-	Incentivize (+)		
10-12	D	Positive Centroid Deviation (PCD)	Positive Centroid Deviation (PCD)	Penalize (-)	10	B
13-16	E	Negative Centroid Deviation (NCD)	Positive Centroid Deviation (PCD)			C

Figure 10. Summary of Scenarios.

The results demonstrate the performance achieved for these various scenarios in terms of travel distance (simulation results), optimization solving time, and the influence of defined ratios for achieved total picking frequency and total score on the travel distance optimization. The mathematical model suggests assignments for items within zones without explicitly prioritizing them. However, our research paper explores different approaches to ranking items. The following list represents the ranking methods that we implemented within our scenarios:

- Ranking Method A is the sum of item correlation (C_{ka}) and item picking frequency (P_{ka}) for item (a) in a particular zone (k):

$$R_{ka} = C_{ka} + P_{ka} \quad (19)$$

- Ranking Method B involves calculating equation [20] for ranking an item (a) in a particular zone (k):

$$R_{ka} = \frac{(P_{ka})^2}{C_{ka} + P_{ka}} \quad (20)$$

- Ranking Method C for an item (a) involves calculating equation [21] for all orders (w) in the order history binary matrix (O_{wb}) to determine the order size in the newly generated suborders with the optimization selection (S_{bk}) of all items denoted by (b) in a particular zone (k):

$$R_{ka} = \sum_{w=1}^i \left(\frac{1}{\sum_{b=1}^m (O_{wa} \cdot O_{wb} \cdot S_{ak} \cdot S_{bk})} \right), \quad O_{wa}, O_{wb}, S_{ak}, S_{bk} \in \{0,1\} \quad (21)$$

It's important to note that method B for item ranking takes a similar approach as method C in optimizing item placement by using an efficient calculation in terms of computation time. Both methods determine the item rank based on frequency and item order size. It's worth noting that the value resulting from dividing the sum of total item correlation score and item frequency of picking by item frequency of picking is equivalent to the item average order size as presented in equation [22]:

$$\text{Item Average Order Size}_{ka} = \frac{C_{ka} + P_{ka}}{P_{ka}} \quad (22)$$

Therefore, the ranking formula used for method B can be seamlessly integrated into optimization models and provides an efficient alternative to the optimal item ranking approach employed by method C. By prioritizing frequently requested items with little to no correlation with other items, the item ranking for method B and C places them closer to the depot, thereby minimizing travel distance. This strategy proves advantageous compared to scenarios where these items are placed further away, beyond other correlated items with the same total picking frequency. For example, let's consider 100 orders of size one for item A and 100 orders of size three for items B, C, and D. Moving item A further from slot number one to slot number four would increase the distance by 300 distance units (assuming one slot equals one distance unit). On the other hand, moving items B, C, and D closer by one slot would collectively decrease the distance by 100 distance units because these items are picked together for each order in one trip. Hence, item A must be prioritized over other items of higher average order size unless they achieve higher picking frequency that compensates for the difference, specifically ≥ 300 orders for B, C, and D. Therefore, calculating item ranking based on the average order size proves to be more effective in optimizing item placement. In the following specifications, we provide details for all models in Figure 10:

- Model A: Scenario no. one (Block A) implements Absolute Centroid Deviation (ACD) to penalize the objective function with a penalty parameter (t) of 2, and item ranking method A. In order to compare the performance result with scenario no. two (Model B – Block A), the optimization for this scenario was combined with the optimization selection of items for scenario no. seven (Model B – Block B)
- Model B: The scenarios under this model implement PCD to penalize the objective function for all centroids, using a penalty parameter (t) of 2, and item ranking method A. This model includes a set of 6 scenarios with variations of ratios as shown in Table 1. Scenario no. two achieved better result in terms of travel distance optimization compared to other scenarios under the same model. It has the same ratios as scenario no. one (Model A). In comparison, the results in Table 1 demonstrate that scenario no. two is 4.5 times faster in terms of solving time, achieved higher total correlation scores, and slightly better travel distance optimization. All scenarios (Block A) in this model are combined with the optimization selection of items for scenario no. seven (Model B – Block B).
- Model C: This model utilizes Positive Mean Deviation (PMD) for the correlation score centroids to incentivize the objective function and maximize the total correlation. The penalty term's sign is reversed, and the model does not impose any restrictions through ratios. The centroids in this model represent the mean, and the item ranking method A is used. Two scenarios are presented in Table 1 for Block A and Block B. The performance result presented for scenario no. eight (Block A) represents the combination of both. It is worth noting that scenario no. two (Model B) outperforms scenario no. eight in terms of travel distance optimization, despite the decrease in the overall item correlation achieved. This can be attributed to the process of order splitting that is resulting in a greater number of trips when the optimization of item assignment is solely based on item correlation frequency.
- Model D: This model applies PCD to penalize the objective function with a penalty parameter (t) of 10, and item ranking method A. Compared to scenario no. two (Model B), which utilizes a penalty parameter of 2, scenario no. ten achieves a slightly better travel distance optimization and closer results to the targeted centroids. However, it is slower and achieves a lower total correlation score. The results for scenario no. ten are combined with the optimization selection

of items for scenario no. seven (Model B - Block B). Additionally, scenarios no. eleven (item ranking method B) and no. twelve (item ranking method C) outperform scenario no. ten in terms of travel distance optimization.

- Model E: The scenarios under this model combines NCD for correlation score centroids and PCD for picking frequency centroids to penalize the objective function with a penalty parameter (t) of 10, and item ranking method C. The results for the four scenarios (Model E - Block A) that implement different defined ratios are combined with the optimization selection of items for scenario no. seven (Model B - Block B). This model aims to better guide the convergence toward the targeted centroids for correlation scores and picking frequency, which are positively correlated. While the correlation scores can increase beyond the targeted centroids by penalizing only negative deviations, the picking frequency can be distributed across zones to minimize the total deviation by avoiding exceeding the defined targeted centroids. Despite our attempt to implement the model with the same ratios as scenario no. one to compare the results, the optimization process did not reach a local optimal solution within several hours before terminating the process. However, a feasible solution was obtained within few minutes. Finding the local optimal solution for these ratios appears to be challenging in this model. However, the feasible solution, which was not included in results, closely achieved the targets for correlation scores.

Among the evaluated scenarios, scenario no. fifteen in model "E" stands out with a remarkable reduction of 36.75% compared to the current system, as in Figure 11. The choice of correlation score and picking frequency ratios in this scenario are specifically defined to optimize the travel distance for a system of three zones. This is achieved by prioritizing higher average order sizes in distant zones resulting in fewer trips for zones located farther away from the depot.

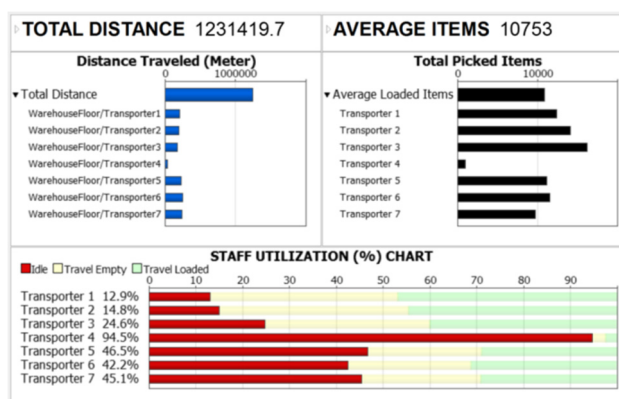


Figure 11. Simulation-based Statistics for Scenario no. 15.

This scenario utilizes correlation score ratios of 2:1.5:1, which means that 44.44% of the high-correlation items are located in the first zone (furthest zone), 33.33% on moderately correlated items, and 22.22% on low-correlation items. In addition, the picking frequency ratios of 1:1.5:2 is implemented to determine the priority of item selection based on their frequency. This ratio implies that 22.22% of the emphasis is on low-frequency items are located in the first zone (furthest zone), 33.33% on moderately frequent items, and a significant 44.44% on high-frequency items. It is important to highlight that the weighting coefficients for these ratios have been appropriately adjusted based on the item slots available for each zone to moderate targets accordingly, as presented in Lingo's code (Model E – Block A). By combining these ratios, model "E" aims to achieve several objectives. Firstly, it encourages larger average order size by prioritizing high-correlated items to low-frequency items in distant zones. This reduces the number of required trips, resulting in improved efficiency. Secondly, the model seeks to increase the number of trips for items with low correlation in the closest zones to the depot. This strategy helps in minimizing order splitting and optimizing the overall picking process in terms of travel distance. To evaluate scenario no. fifteen, we analyzed a recent order history spanning 148 days, which resulted in a reduction percentage of

33.59%. This indicates that the model has been effective in achieving sustainability. It is important to note that while the correlation score can dynamically increase to achieve the desired targets, the total picking frequency for all items remains constant. Furthermore, the model has shown solid results and provided insights for optimizing the travel distance; however, it is still considered in the experimental stage. The ratios proposed in this case study may not be optimal for scenarios with imbalanced slot distributions across zones. For instance, the ratios presented for scenario no. seven (Model B - Block B) specifically address the shortage of available slots in zone no. four, which is the closest to the depot. Despite attempts to optimize travel distance by using ratios such as 1:2:3:4 for the correlation score and 4:3:2:1 for the picking frequency, the results did not surpass the selected ratios presented in Table 1 for scenario no. seven. This was the case even after considering slot availability and adjusting the weighting coefficients for all zones. This because attempting to assign correlated items in zone no. four, which only has approximately a third of the available slots compared to any other zone in block B, would cause order splitting and additional trips to other zones. On the other hand, reducing the correlation score to the minimum value and increasing picking frequency for zone no. four allowed for larger average order sizes in distant zones that had enough slots to accommodate different combinations of correlated items that are frequently found in customer orders. Ultimately, this approach reduced the overall number of trips required. Therefore, it is recommended to place the most frequently ordered single-items in the zones closest to the depot, especially when there are fewer available slots.

6. Conclusion

In this paper, we employ a methodology to demonstrate that maximizing the correlation among items to optimize the storage assignment is not the only factor in order to minimize the travel distance. We have successfully implemented the CSAS by adopting an approach that aligns with the zoning system and incorporating an item ranking method that accommodates both single-item and multi-item orders within each zone. Our approach highlights the importance of considering the average order size based on distance from depot as a crucial factor, surpassing the sole reliance on maximizing the total item correlation per zone. By doing so, we are able to achieve better results in terms of travel distance optimization by minimizing trips in distant zones and decreasing order splitting. Additionally, our methodology offers flexibility to customize the assignment of correlated items based on real-world scenarios, ensuring adaptability and practicality in diverse operational contexts. It is crucial to acknowledge the challenges associated with achieving specific item distribution based on correlation and frequency. We initially attempted to incorporate distance-based soft constraints in our MINLP model to prioritize the placement of high-correlation to lower picking frequency items in distant zones. This involved assigning lower reward factors for placing such items for nearby zones in the objective function, while increasing the reward for their placement in distant zones. However, the model overcompensates and does not converge according to our targets. Furthermore, in our proposed model, defining ratios posed initial difficulties in achieving the desired outcome, particularly when dealing with extreme reverse ratios. That was mainly due to the positive correlation between the correlation score and picking frequency, coupled with the preference for maximizing the total correlation score rather than enforcing desired weighted centroids per zone. To address these challenges, we have implemented PCD and NCD penalty terms. These penalties aim to address the positive or negative sources of deviation, particularly to prohibit it from increasing beyond or below a target. It is important to note that the solution obtained by the solver is highly dependent on various configurations, such as type of derivatives used and other selected heuristic procedures. As a result, the solutions can vary in terms of solving time and the achieved objective function.

In this study, we evaluate sixteen scenarios under five optimization models (Models A to E) for implementing the CSAS. Our models are evaluated based on factors such as travel distance, total correlation score, and item picking frequency in order to optimize the order picking process. Scenario no. fifteen found to be the most effective, achieving a reduction of 36.75% compared to the current system. It prioritizes high-correlation items and low-frequency items in distant zones, promoting

larger order sizes and reducing travel distance for these zones in contrast to closer ones. The presented results validate the effectiveness of the optimization models using both fitted and new datasets. The proposed approach for implementing the CSAS minimizes the travel distance by penalizing the objective function with the use of PCD and NCD penalty terms and a parameter of 10, ranking items based on their average order size using method C, and finally prioritizing higher ratios of correlation score to picking frequency for distant zones. For ranking items within zones, method C is found to be the most optimal. However, method B, which also considers the item average order size, is more efficient in terms of computation time. Both methods can be applied as a direct approach for optimizing the travel distance in a single-zone order picking system. Therefore, we recommend further research to test this proposed approach, providing insights into its advantages in terms of computational efficiency and optimality for both single and batch order picking systems. Additionally, we recommend further analysis for optimizing the travel distance using different datasets to address scenarios with imbalanced slot distributions across zones in a multi-zone system. Our proposed model considers the impact of higher correlation scores to lower picking frequencies while aiming to achieve larger average order sizes in order to prioritize the placement of these items in distant zones. This methodology is achieved by explicitly defining ratios of the proposed targets. With additional analysis to investigate imbalanced slot distribution using different datasets, this model can be improved to incorporate dynamic convergence techniques without the explicit need to define these ratio. The model could be developed to dynamically adjust the weighted centroids, taking into account their respective impacts on selecting items that collectively achieve larger order sizes, while considering the slot availability ratio at each zone to minimize order splitting. By adjusting the weights of the coefficients during the optimization process based on each case scenario, the model can adapt to different conditions and find an optimal solution for different datasets. It is also recommended to develop a model that follows a direct approach in evaluating the impact of order splitting while assigning correlated items across zones. Overall, this paper provides recommendations for optimizing order picking operations and highlights effective strategies for item placement. By adopting these strategies, the order fulfillment can be enhanced, leading to improved efficiency and cost savings. Furthermore, the techniques employed in our approach have the potential to be applied in various areas such as distributing resources, algorithms and mathematical models.

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