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Article

# Fractional-Order Load Frequency Control of An Interconnected Power System With Hydrogen Energy-Storage Unit

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**Abstract:** Modern power systems are confronted with a spread concern on the frequency stability issue due to the widespread integration of randomly fluctuating renewable resources. To address the above concern, this work introduces a load frequency control (LFC) scheme based on a hydrogen based energy-storage unit and a parameter tuning strategy for fractional-order proportional-integral-derivative (FOPID) controller. Firstly, a two-area interconnected power system (IPS) model, including thermal, hydro, solar, wind, gas power generator, and hydrogen based energy-storage unit, is established. Then, a FOPID controller is designed for this IPS model, and an improved gradient-based optimizer (IGBO) is developed to adaptively regulate the parameters of the FOPID controllers. Finally, the effectiveness of the offered LFC scheme are tested through load disturbance and renewable energy fluctuations test scenarios, and provides comparison and robustness analysis among different schemes. The test results validated that the offered LFC scheme can effectively suppress the frequency fluctuations of IPS and has excellent robustness.

**Keywords:** load frequency control; interconnected power system; fractional-order control; improved gradient-based optimizer; parameter tuning

## 1. Introduction

Development and application of renewable energy generation technology could be one critical enabler of the global transition to low-carbon emissions economies [1]. Nevertheless, solar energy, wind energy, tidal energy and other renewable energies have random and fluctuating characteristics, and renewable energy generators have almost no inertia contribution to power grids since these generators are isolated to the grids by power electronic converters [2,3]. As a result, the IPSs with a substantial integration of renewable energy generators always face the frequency stability issue, and a suitable design of LFC method is commonly required for these power systems.

Over the past few years, various intelligent control technologies such as model predictive control [4], sliding mode control [5], reinforcement learning [6], active disturbance rejection control [7], fuzzy logic control [8] have been utilized in the design of load frequency control (LFC). The LFC scheme developed by the above technologies are usually effective in different test scenarios, but the major challenge of employing these methods is their heavy reliance on model accuracy and engineering feasibility. While traditional proportional-integral-derivative (PID) controller based LFC design, in fact, remains the most extensively used approach in practice [9,10]. However, the interconnected structure and complicated module expressions of modern IPSs make the empirical parameter tuning methods become time consuming and ineffective when using PID controller based LFC scheme. Besides, by using traditional PID controller based LFC design and empirical parameter tuning methods, the robustness and dynamic properties of the system may also get worse in highly volatile renewable energy power generation facilities and highly flexible loads.

To address the above concerns, various parameter tuning and optimization techniques were developed for optimizing PID controller based LFC. These techniques include whale optimization

algorithm (WOA) [11], fuzzy rule (FL) [12], artificial neural network (ANN) [13], and gray wolf optimizer (GWO) [14]. According to these works, one can find that by introducing optimization strategies to regulate the parameters, the frequency stability of IPSs can be improved significantly. Nonetheless, traditional PID controllers only have three adjustable parameters, their parameter settings are limited, and their performance deteriorate with system nonlinearities and uncertainties. Therefore, FOPID controller is proposed. In comparison to PID controllers, the FOPID controller enhances the adjustable dimensionality of controller parameters by incorporating fractional differential and integral orders. Consequently, it exhibits superior robustness and anti-interference performance in response to variations in the controlled system parameters [15–17]. Recently, such controllers have also been used for LFC design. For example, in literature [18], a FOPID controller is used to mitigate the frequency fluctuation of a two-area IPS, and a gases brownian motion optimization (GBMO) is exploited to regulate the parameters of the controller. Literature [19] use a modified FOPID controller-based LFC scheme to enhance frequency regulation performance and the controller parameters are subsequently tuned using Jellyfish Search Optimizer (JSO). In literature [20], a FOPID controller based LFC scheme for IPS with renewable energy power plants is proposed and movable damped wave algorithm (MDWA) is employed to tune the FOPID controller parameters. Besides, the method based on an improved particle swarm optimization (IPSO) and a hybrid artificial gorilla troops optimizer and equilibrium optimizer (AGTOEO) for tuning FOPID controller parameters has also been used in LFC design, as those introduced in reference [21] and [22]. The findings from these studies validate that FOPID controllers demonstrate superior dynamic performance compared to traditional PID controllers in LFC applications.

In addition to designing control strategies, the integration of energy storage facilities has emerged as a prevalent supplementary method to enhance the frequency characteristics of IPSs with renewable resources [23,24]. Among various energy storage technologies such as pumped storage, flywheel energy storage and electrochemical energy storage, hydrogen energy storage exhibits significant advantages in energy storage capacity and economic feasibility [25–27]. Over the last decade, significant efforts have been devoted to the development and application of hydrogen energy-based techniques. Various research groups have explored the utilization of hydrogen energy storage units in contributing to the frequency regulation of conventional power systems primarily powered by thermal power plants [28,29]. Through an analysis of existing studies focused on enhancing system structures through the integration of energy storage units, it can be inferred that the incorporation of hydrogen-based energy storage units into integrated energy systems enables power systems to exhibit greater flexibility in responding to energy fluctuations and enhances the utilization of renewable energy sources.

In recent years, the gradient-based optimizer (GBO) has emerged as a promising solution for addressing optimization problems across diverse fields, primarily due to its simple yet powerful structure, ease of implementation, robust exploration capability, and ability to effectively evade local optima [30]. However, the GBO has some limitations when tackling large-scale and complex engineering problems, such as slow convergence speed and low precision in the later stages of the algorithm [31]. To address these challenges, this study proposes an improved GBO (IGBO) for obtaining optimal parameters for the FOPID controller in LFC issues within a two-area IPS integrated with hydrogen energy storage. Firstly, a FOPID controller-based LFC scheme is designed using the Oustaloup approximation algorithm. Subsequently, the IGBO algorithm is developed to adaptively regulate the FOPID controller parameters. Finally, a series of test scenarios are presented to test the effectiveness and superiority of the offered LFC method, along with an analysis of system robustness.

## 2. LFC model of a two-area IPS

In general, modern power systems are formed by multiple interconnecting areas, with each area consisting of a variety of different types of power sources and load units. In this study, we focus on an IPS model consisting of two areas, which is depicted in Figure 1.

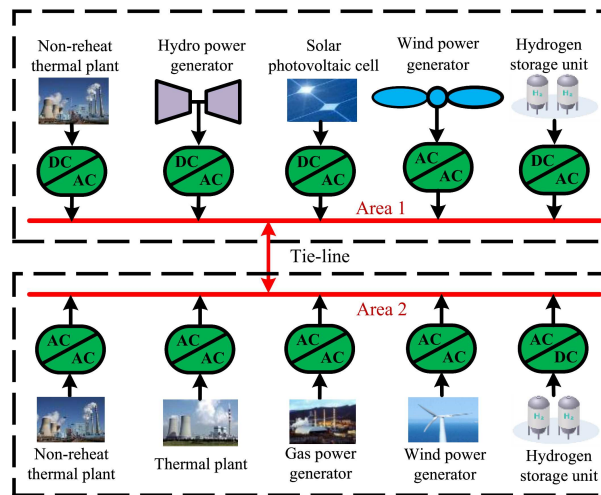


Figure 1. Structure of a two-area IPS.

In the two-area IPS, Area 1 comprises a non-reheat thermal plant, hydro power generator, solar photovoltaic cell, wind power generator, while Area 2 consists of a thermal plant, non-reheat thermal plant, gas power generator, and wind power generator. Furthermore, hydrogen storage units are incorporated in both areas to enhance system performance. The mathematical models for each unit can be described as follows:

### 2.1. Mathematical model of thermal power plant

In a thermal power plant, the primary components are a speed governor and a steam turbine. The transfer function for the governor and steam turbine can be governed as

$$G_G = \frac{1}{1 + sT_G} \quad (1)$$

$$G_T = \frac{1}{1 + sT_T} \quad (2)$$

where  $T_G$  and  $T_T$  denote the time constants of the governor and turbine, respectively.

The transfer function of a reheater can be governed by

$$G_R = \frac{1 + sK_r T_r}{1 + sT_r} \quad (3)$$

where  $K_r$  and  $T_r$  are the gain and time constants of the reheater, respectively.

### 2.2. Mathematical model of hydro power generator

The hydro power generator comprises a hydraulic turbine and a hydraulic governor, with its transfer function can be represented as

$$G_{HT} = \frac{1 - sT_W}{1 + 0.5sT_W} \quad (4)$$

$$G_{HG} = \frac{1 + sT_R}{(1 + sT_{GH})(1 + s(R_T/R)T_R)} \quad (5)$$

where  $T_W$  and  $T_{GH}$  represent the time constants of the turbine and the governor, respectively.  $T_R$  represent the reset time constant,  $R$  denotes the adjustment coefficient of hydro power generator, and  $R_T$  is the transient fall rate.

### 2.3. Mathematical model of solar photovoltaic cell

The power output of a solar photovoltaic cell is [21]

$$P_{PV} = \eta S \Phi \{1 - 0.005 (T_a + 25)\} \quad (6)$$

where the coefficient  $\eta$  represents the conversion efficiency of the photovoltaic unit. The coefficient  $S$  represents the surface area of the photovoltaic array,  $\Phi$  denotes the solar radiation on the photovoltaic array, and  $T_a$  denotes the working temperature. The mathematical model of photovoltaic system is

$$G_{PV} = \frac{K_{PV}}{1 + sT_{PV}} \quad (7)$$

where  $K_{PV}$  and  $T_{PV}$  are the gain and time constants of the photovoltaic unit, respectively.

### 2.4. Mathematical model of wind power generator

The modeling of wind power generators consists of two parts: a nonlinear model and a transfer function model. The former, as described in [21], does not contribute to frequency regulation. The power output of a wind power generator is

$$P_{WTG} = \frac{1}{2} \rho A_r C_p V_W^3 \quad (8)$$

where the coefficient  $\rho$  refers to air density, and  $A_r$  represents the swept area of blades. The coefficient  $C_p$  denotes the power coefficient,  $V_W$  denotes wind speed. The dynamic model of wind power generator is

$$G_W = \frac{K_{WTG}}{1 + sT_{WTG}} \quad (9)$$

where  $K_{WTG}$  and  $T_{WTG}$  represent the gain and time constants of the wind power generator, respectively.

The transfer function model focuses on the active standby of wind turbines and takes wind power as an active resource for frequency modulation [5], which can be mathematically expressed as

$$G_{wind} = \frac{1}{1 + sT_{pw2}} \frac{K_{pw1}(1 + sT_{pw1})}{1 + s} \frac{K_{pw2}}{1 + s} \quad (10)$$

where  $T_{pw1}$ ,  $T_{pw2}$ ,  $K_{pw1}$ , and  $K_{pw2}$  denote the time and gain constants of the wind power governor, respectively.

### 2.5. Mathematical model of gas power generator

The mathematical model of gas power generator can be stated as [32]

$$G_{GT} = \frac{1}{c_g + sb_g} \frac{1 + sX_c}{1 + sY_c} \frac{1 + sT_{cr}}{1 + sT_f} \frac{1}{1 + sT_{cd}} \quad (11)$$

where  $c_g$  and  $b_g$  represent the gain and time constants of the gas turbine, respectively.  $X_c$  and  $Y_c$  are complex parameters that reflect the impact of the gas turbine on the phase and amplitude of the input signal,  $T_{cr}$ ,  $T_f$  and  $T_{cd}$  are the time constants of the cooling system, fuel injection and entire gas power generator, respectively.

### 2.6. Mathematical model of hydrogen storage unit

The hydrogen storage system comprises an electrolyzer, a storage tank, and a hydrogen fuel cell. When surplus power is generated by the new energy generators within the system, the electrolyzer produces hydrogen, which is subsequently compressed and stored in the hydrogen storage tanks.

During periods of heightened load demand and electricity scarcity, the hydrogen fuel cell converts the chemical energy into electrical power to meet the system's load requirements. The mathematical model of the electrolyzer and the hydrogen fuel cell in the system can be represented as [28]

$$G_{\text{HAE}} = \frac{K_{\text{HAE}}}{1 + sT_{\text{HAE}}} \quad (12)$$

$$G_{\text{FC}} = \frac{K_{\text{FC}}}{1 + sT_{\text{FC}}} \quad (13)$$

where  $K_{\text{HAE}}$  and  $K_{\text{FC}}$  are the gain constants of the electrolyzer and the hydrogen fuel cell, respectively.  $T_{\text{HAE}}$  and  $T_{\text{FC}}$  represent the time constants of the electrolyzer and the hydrogen fuel cell, respectively.

Based on the mathematical models of each unit, as well as the hydrogen storage unit, an LFC model is constructed for the IPS consisting of two areas, as depicted in Figure 2.

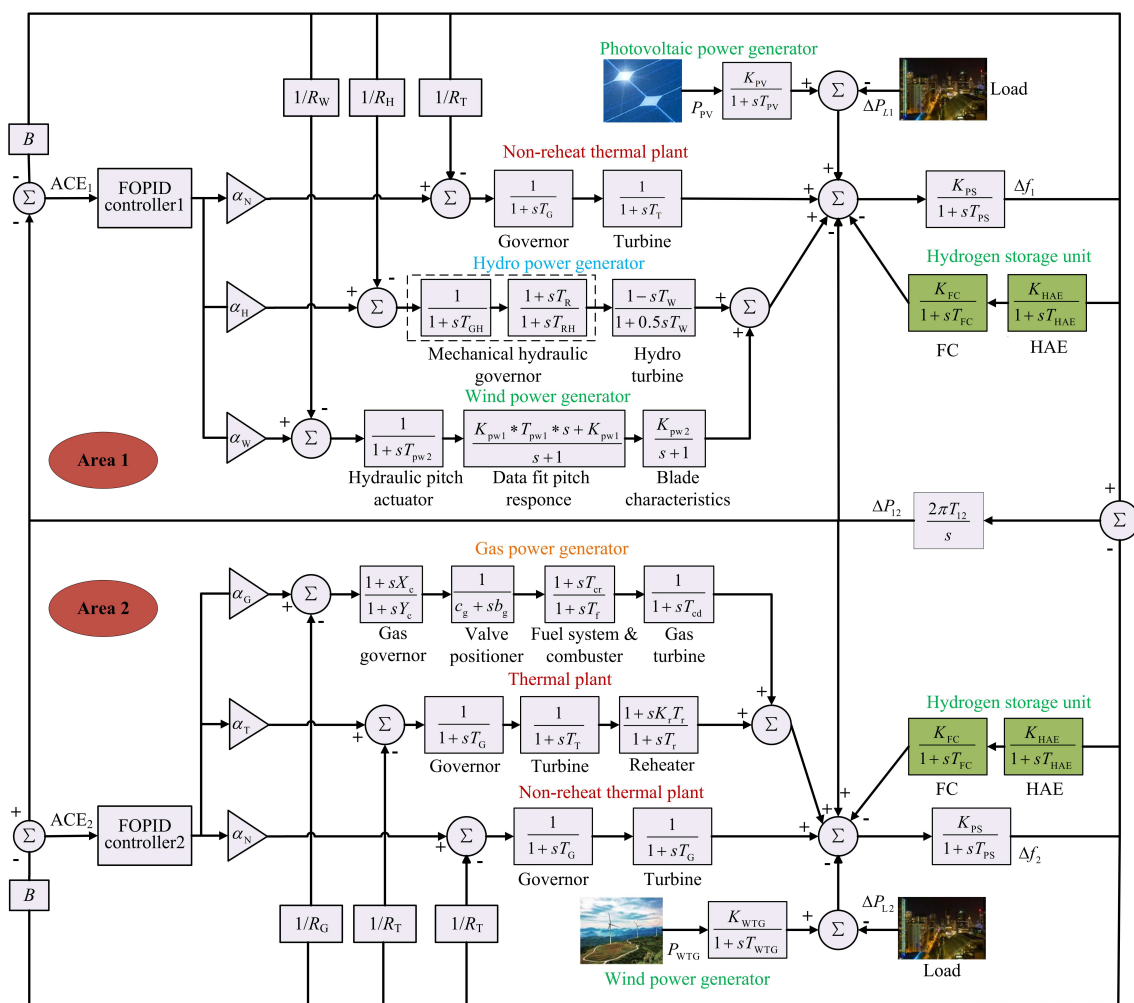


Figure 2. LFC model of a two-area IPS.

In Figure 2, the term  $B$  is the frequency offset coefficient,  $ACE_1$  and  $ACE_2$  represent the area control errors (ACE) for area 1 and area 2, respectively,  $R_T$  and  $R_H$  represent the governor constants of the thermal plants and the hydro power generator, respectively.  $R_G$  and  $R_W$  represent the governor parameters of gas power generator and wind power generator, respectively.  $\alpha_G$ ,  $\alpha_T$ ,  $\alpha_N$ ,  $\alpha_W$  and  $\alpha_H$  represent the power distribution ratio of gas, thermal, non-heat thermal, wind power and hydro power generators, respectively,  $\Delta P_{L1}$  and  $\Delta P_{L2}$  represent load disturbances in area 1 and area 2, respectively.  $K_{PS}$  and  $T_{PS}$  denote the gain and time constants of the IPS, respectively.  $T_{12}$  denotes the

synchronization coefficient of the tie line,  $\Delta f_1$  and  $\Delta f_2$  represent the frequency deviation of the area 1 and area 2, respectively.  $\Delta P_{12}$  denotes the power flow of tie line.

### 3. Design of FOPID controller based LFC

The LFC scheme in this study is based on a FOPID controller, which is two more parameters compared to the traditional PID controller. Basically, the transfer function of FOPID controller can be expressed by

$$G_C(s) = K_P + \frac{K_I}{s^\lambda} + K_D s^\mu \quad (14)$$

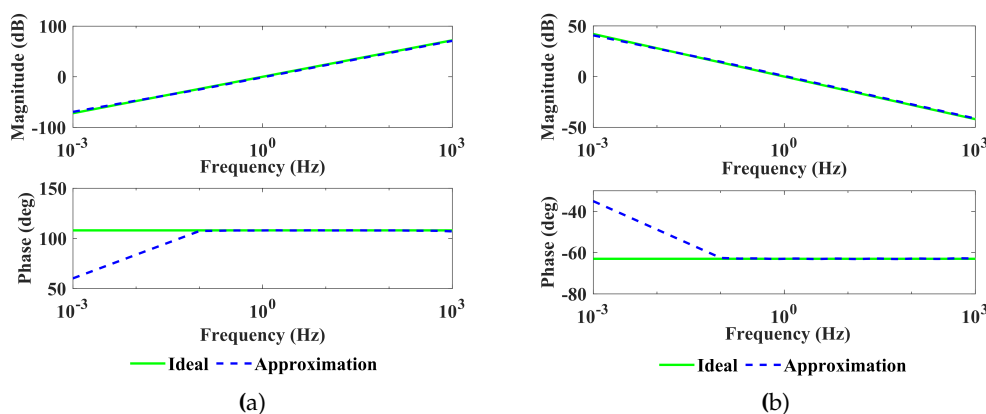
where  $K_P$ ,  $K_I$  and  $K_D$  represent the proportional coefficient, integral coefficient and differential coefficient, respectively. Additionally,  $1/s^\lambda$  and  $s^\mu$  denote the fractional integral operator and fractional differential operator, respectively. These ideal fractional-order operators cannot be implemented directly by integer order rational fractions. This study adopts an improved Oustaloup's approximation algorithm [33] to approximate the fractional-order operator within a predetermined frequency range by constructing a transfer function in the form of zeros and poles as follows:

$$G(s) = \left(\frac{d\omega_b}{b}\right)^\alpha \frac{ds^2 + b\omega_h s}{d(1-\alpha)s^2 + b\omega_h s + d\alpha} \prod_{k=-N_f}^{N_f} \frac{s + \omega'_k}{s + \omega_k} \quad (15)$$

$$\omega'_k = \omega_b \left(\sqrt{\frac{\omega_h}{\omega_b}}\right)^{\frac{k+N_f+0.5(1-\alpha)}{2N_f+1}} \quad (16)$$

$$\omega_k = \omega_b \left(\sqrt{\frac{\omega_h}{\omega_b}}\right)^{\frac{k+N_f+0.5(1+\alpha)}{2N_f+1}} \quad (17)$$

where  $\alpha$  represents the order of the fractional-order operator, and the coefficients  $b$  and  $d$  are preset coefficients with values of 9 and 10, respectively.  $N_f$  represents the order of the filter, which we set to 5 in this study.  $\omega_b$  and  $\omega_h$  represent the lower and upper limits of the predetermined frequency range, with values of 0.001 and 1000, respectively.  $\omega'_k$  and  $\omega_k$  represent the constructed zeros and poles of the transfer function, respectively. The comparison between the ideal fractional-order operators and approximate fractional-order operators is shown in Figure 3.



**Figure 3.** Comparison of ideal fractional-order operators and approximate fractional-order operators: (a) Derivative of order 1.2. (b) Integral of order 0.7.

As depicted in Figure 3, it can be observed that within the predetermined frequency range, the amplitude-frequency characteristic curves of the approximate fractional-order operator and the ideal fractional-order operator coincide with each other. Additionally, the phase-frequency characteristic curves of both operators fall within the preset phase error range throughout the predetermined

frequency range. The results of comparison confirm that the approximate fractional-order operators can be applied.

#### 4. Parameter tuning process based on IGBO

To ensure the two-area IPS in Figure 2 can swiftly recover frequency stability under load or renewable resources fluctuations, this paper proposes a parameter tuning strategy by an IGBO algorithm, which uses a combination of the gradient search mechanism (GSM) based on a sorting algorithm and the improved local escape operators (ILEO) based on chaotic mapping in the optimization process [34]. The objective fitness function is formulated using the integral of time multiplied absolute error (ITAE) criterion based on the ACE, which can be as

$$\min J_{ITAE} = \int_0^{T_{sim}} t (|\Delta f_1| + |\Delta f_2| + |\Delta P_{12}|) dt \quad (18)$$

where  $T_{sim}$  is the total duration of the optimization process. With the objective of minimizing  $J_{ITAE}$ , the IGBO algorithm is utilized to tune the parameters of the FOPID-based LFC controllers in the IPS. The specific update method for IGBO is as follows:

##### 4.1. Initialization

The IGBO algorithm initializes the parameters of the FOPID controller based on

$$X_n = Low + rand \times (Up - Low) \quad (19)$$

where  $n = 1, 2, \dots, N$ ,  $N$  corresponds to the total number of IGBO vectors.  $Low$  and  $Up$  denote the lower and upper bounds of the parameter space.  $rand$  denotes a randomly generated number within the range 0 to 1.

##### 4.2. Parameter update method based on GSM

GSM is used for global search in the parameter space, and its definition is as

$$GSM = randn \times \rho_1 \times \frac{2\Delta X \times X_n}{yp_n - yq_n + \varepsilon} \quad (20)$$

where  $randn$  represents a random number that follows a normal distribution, and  $\varepsilon$  represents a small number in the range of 0 to 0.1.  $\rho_1$  is a crucial parameter that determines the global exploration ability of the IGBO algorithm. To obtain a better solution for the FOPID controller parameters, a sorting algorithm is proposed to update the parameter  $\rho_1$ , which can be represented as

$$\rho_1 = \begin{cases} r1/N + 0.15 \times randn & \text{if } rand < 0.5 \\ n/N + 0.15 \times randn & \text{else} \end{cases} \quad (21)$$

where  $r1$  is a integer randomly selected from 1 to  $N$ . Furthermore, the GSM definition is represented by equation (22) for  $\Delta X$ , and  $yp_n$  and  $yq_n$  are represented by equation (25) and equation (26) respectively.

$$\Delta X = rand(1 : D) \times |step| \quad (22)$$

$$step = \frac{(X_{best} - X_{r1}^{it}) + \delta}{2} \quad (23)$$

$$\delta = 2 \times rand \times \left( \left| \frac{X_{r1}^{it} + X_{r2}^{it} + X_{r3}^{it} + X_{r4}^{it}}{4} - X_n^{it} \right| \right) \quad (24)$$

where  $rand(1 : D)$  is a  $D$ -dimensional random vector,  $D$  corresponds to the number of parameters of the FOPID controller to be optimized.  $step$  is determined by the optimal solution ( $X_{best}$ ) and the random selection vector ( $X_{r1}^{it}$ ) in the iterations.  $it$  is the current number of iteration within the range 1 to  $It_{max}$ ,  $It_{max}$  represents the maximum number of iterations. The variables  $r2$ ,  $r3$ , and  $r4$  represent distinct integers are randomly selected from 1 to  $N$ .

$$yp_n = rand \times \left( \frac{[Z_{n+1} + X_n]}{2} + rand \times \Delta X \right) \quad (25)$$

$$yq_n = rand \times \left( \frac{[Z_{n+1} + X_n]}{2} - rand \times \Delta X \right) \quad (26)$$

$$Z_{n+1} = X_n - randn \times \frac{2\Delta X \times X_n}{X_{worst} - X_{best} + \varepsilon} + DM \quad (27)$$

$$DM = rand \times \rho_2 \times (X_{best} - X_n^{it}) \quad (28)$$

where  $X_{worst}$  represents the worst vector during the iterations.  $DM$  is the direction of movement, guiding the individual vector towards a more optimal solution. The update method for parameter  $\rho_2$  is the same as  $\rho_1$ .

According to GSM, the IGBO generates two solutions with different capabilities using equation (29) and equation (30) respectively.

$$X1_n^{it} = X_n^{it} - randn \times \rho_1 \times \frac{2\Delta X \times X_n^{it}}{yp_n - yq_n + \varepsilon} + rand \times \rho_2 \times (X_{best} - X_n^{it}) \quad (29)$$

$$X2_n^{it} = X_{best} - randn \times \rho_1 \times \frac{2\Delta X \times X_n^{it}}{yp_n - yq_n + \varepsilon} + rand \times \rho_2 \times (X_{r1}^{it} - X_{r2}^{it}) \quad (30)$$

where equation (29) is beneficial for global search and equation (30) is beneficial for local exploitation. Therefore, based on the solutions  $X1_n^{it}$  and  $X2_n^{it}$ , the IGBO generates the next solution ( $X_n^{it+1}$ ) is defined as

$$X_{n,j}^{it+1} = \begin{cases} \begin{cases} X1_{n,j}^{it} & \text{if } rand_2 < 0.5 \\ X2_{n,j}^{it} & \text{if } rand_2 \geq 0.5 \end{cases} & \text{if } rand_1 < P_{cr} \\ X_{n,j}^{it} & \text{if } rand_1 \geq P_{cr} \end{cases} \quad j = 1 \text{ to } D \quad (31)$$

where  $rand_1$  and  $rand_2$  are two different random numbers,  $P_{cr}$  is the crossover probability, and its update method is the same as  $\rho_1$ .

#### 4.3. ILEO

The ILEO is used in IGBO to avoid algorithms falling into local optimality. The generation method of ILEO vector solution can be expressed as

$$X_{ILEO}^{it+1} = \begin{cases} X_n^{it+1} + \rho_1 (X_{best2} + X_k^{it}) + \rho_2 (X_{r1}^{it} - X_{r2}^{it}) & \text{if } rand < \frac{(1-it)/It_{max}}{2} \\ X_{best} + \rho_1 (X_{best2} + X_k^{it}) + \rho_2 (X_{r1}^{it} - X_{r2}^{it}) & \text{else} \end{cases} \quad (32)$$

where  $X_{best2}$  is the second best solution.  $X_k^{it}$  represents a solution that is randomly selected from 1 to  $N$ . Therefore, the next generation solutions generated by the IGBO can be represented as

$$X_n^{it+1} = \begin{cases} X_{ILEO}^{it+1} & \text{if } rand < LC \\ X_n^{it+1} & \text{else} \end{cases} \quad (33)$$

where the term  $LC$  denotes a chaotic logistic map, and its update method is  $LC = 4LC(1 - LC)$ , and the initial  $LC$  is 0.67. The IGBO optimizes the parameters of two FOPID controllers in the following parameter space.

$$\begin{cases} K_{Pi}^{Low} \leq K_{Pi} \leq K_{Pi}^{Up} \\ K_{Ii}^{Low} \leq K_{Ii} \leq K_{Ii}^{Up} \\ K_{Di}^{Low} \leq K_{Di} \leq K_{Di}^{Up} \\ \lambda_i^{Low} \leq \lambda_i \leq \lambda_i^{Up} \\ \mu_i^{Low} \leq \mu_i \leq \mu_i^{Up} \end{cases} \quad (34)$$

where  $i = 1, 2$  indicates area 1 and area 2, respectively. The parameter tuning process based on IGBO is depicted in Figure 4.

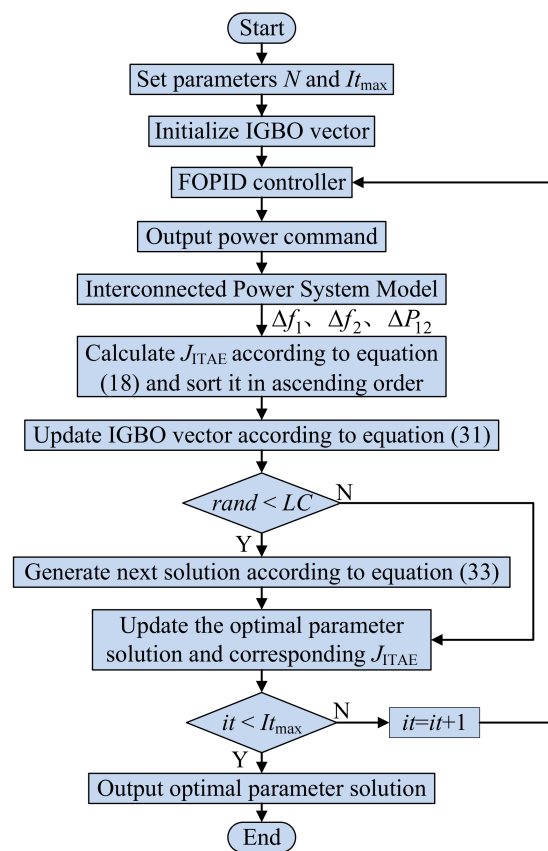


Figure 4. Parameter tuning process based on IGBO algorithm.

## 5. Validation and comparison

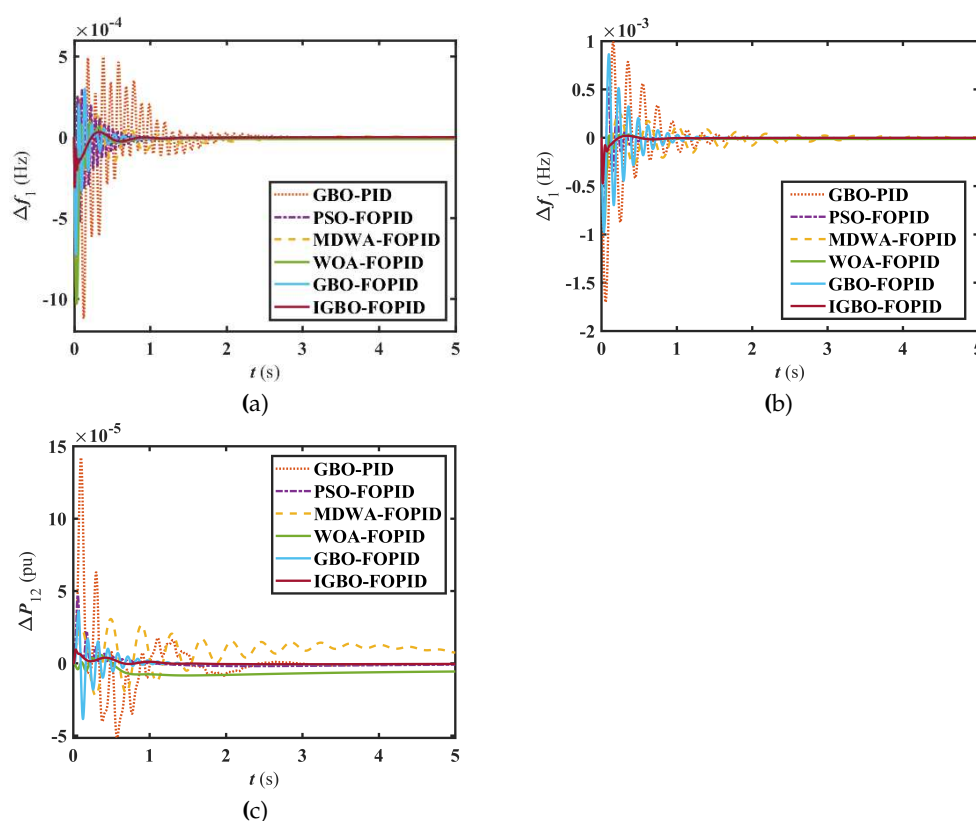
In this section, a two-area IPS LFC model is constructed according to Figure 2, and the system parameter settings are depicted in Appendix A. The proposed LFC scheme is initially tested using step load disturbance scenarios. Subsequently, its performance is validated under scenarios involving random fluctuations of photovoltaic and wind power. Furthermore, the robustness of the IPS is evaluated by varying the inertia constant. To test the effectiveness of the offered LFC scheme (IGBO-FOPID) in this study, its control performance is compared with existing LFC methods, including the FOPID controller regulated through WOA (WOA-FOPID), MDWA (MDWA-FOPID), PSO (PSO-FOPID), and GBO tuned PID/FOPID controllers (GBO-PID/FOPID). The maximum number of iterations,  $It_{max}$ , for each control scheme algorithm is set to 30, and  $N$  is set to 50. Table 1 lists the controller parameters obtained by different LFC schemes.

**Table 1.** Parameters of two FOPID controllers obtained by different LFC schemes.

LFC scheme	$K_{P1}$	$K_{I1}$	$K_{D1}$	$\lambda_1$	$\mu_1$	$K_{P2}$	$K_{I2}$	$K_{D2}$	$\lambda_2$	$\mu_2$
GBO-PID	68.22	385.33	25.42	-	-	61.77	430.56	16.58	-	-
WOA-FOPID	54.38	308.42	10.66	0.41	1.19	305.22	525.31	12.62	1.17	1.32
MDWA-FOPID	516.76	327.85	4.89	2	1.81	622.30	25.11	3.43	2	1.89
PSO-FOPID	583.84	513.51	31.38	0.97	1.19	461.51	512.46	22.13	1.15	1.21
GBO-FOPID	385.42	519.77	15.98	1.09	1.23	695.18	683.66	16.16	1.12	1.24
IGBO-FOPID	545.39	642.31	11.48	1.02	1.62	697.38	698.66	22.18	1.04	1.47

### 5.1. Step load disturbance test scenarios

In this scenario, the output of renewable energy units is not considered. At 0s, 0.01 pu step disturbance signals are introduced to area 1 and area 2 at the same time. In simulation, the performances of six different LFC schemes are compared, in which GBO-PID, PSO-FOPID, MDWA-FOPID, WOA-FOPID, GBO-FOPID and IGBO-FOPID based LFC are used. The response of the IPS under step load disturbance with different LFC schemes are depicted in Figure 5.



**Figure 5.** Response curves of the IPS under step load disturbance scenarios: (a) frequency deviation in area 1, (b) frequency deviation in area 2, (c) tie line power.

The results presented in Figure 5 demonstrate the superiority of the FOPID controller-based LFC scheme over the PID controller-based LFC scheme. Implementation of the FOPID controller leads to a considerable enhancement in system frequency modulation performance. Specifically, the FOPID controller-based LFC scheme effectively reduces the frequency deviation overshoot and minimizes frequency fluctuation range within the system. Furthermore, the proposed IGBO-optimized FOPID controller outperforms FOPID controllers optimized using PSO, MDWA, WOA, and GBO algorithms. Notably, the IGBO-FOPID controller-based LFC scheme yields lower overshoot, as well as shorter settling time to achieve system stability. These outcomes affirm that the IGBO-FOPID controller-based LFC scheme significantly enhances the frequency response capability of the IPS.

To further evaluate the superiority of the proposed LFC scheme, Table 2 lists some key performance indicators of the IPS with different LFC schemes, such as maximum undershoot (US), maximum overshoot (OS), integral squared error (ISE), integral time multiplied squared error (ITSE), integral absolute error (IAE), and ITAE of  $\Delta f_1/\Delta f_2/\Delta P_{tie12}$ .

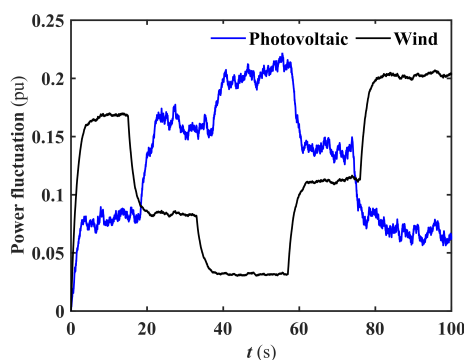
**Table 2.** Maximum US/Maximum OS/ ISE/ITSE/IAE/ITAE of system response under step load disturbance scenarios.

LFC scheme	Maximum US			Maximum OS			ISE	ITSE	IAE	ITAE
	$\Delta f_1$	$\Delta f_2$	$\Delta P_{tie12}$	$\Delta f_1$	$\Delta f_2$	$\Delta P_{tie12}$				
GBO-PID	-1.10e-3	-1.70e-3	-5.15e-5	4.97e-4	9.94e-4	1.42e-4	4.86e-7	1.10e-7	8.54e-4	4.27e-4
WOA-FOPID	-1e-2	-9.55e-4	-8.37e-6	9.34e-5	3.45e-5	5.91e-6	7.79e-8	7.75e-9	2.82e-4	4.12e-4
MDWA-FOPID	-3.71e-4	-4.86e-4	-2.22e-5	1.34e-4	2.64e-4	3.07e-5	4.80e-8	2.08e-8	4.02e-4	4.47e-4
PSO-FOPID	-5.62e-4	-9.19e-4	-1.89e-5	2.95e-4	5.23e-4	4.74e-5	6.86e-8	7.33e-9	2.31e-4	8.28e-5
GBO-FOPID	-7.24e-4	-9.76e-4	-3.85e-5	2.98e-4	8.64e-4	3.60e-5	1.20e-7	1.66e-8	3.05e-4	9.93e-5
IGBO-FOPID	-3.09e-4	-4.72e-4	-6.21e-7	3.21e-5	2.06e-5	9.51e-6	9.79e-9	6.87e-10	8.76e-5	4.89e-5

The comparison in Table 2 showcases that the IGBO-optimized FOPID controller achieves superior values of maximum US, maximum OS, ISE, ITSE, IAE, and ITAE compared to other LFC schemes. This further illustrate that the offered controller outperforms those based on PSO, MDWA, WOA, and GBO optimized PID/FOPID controllers.

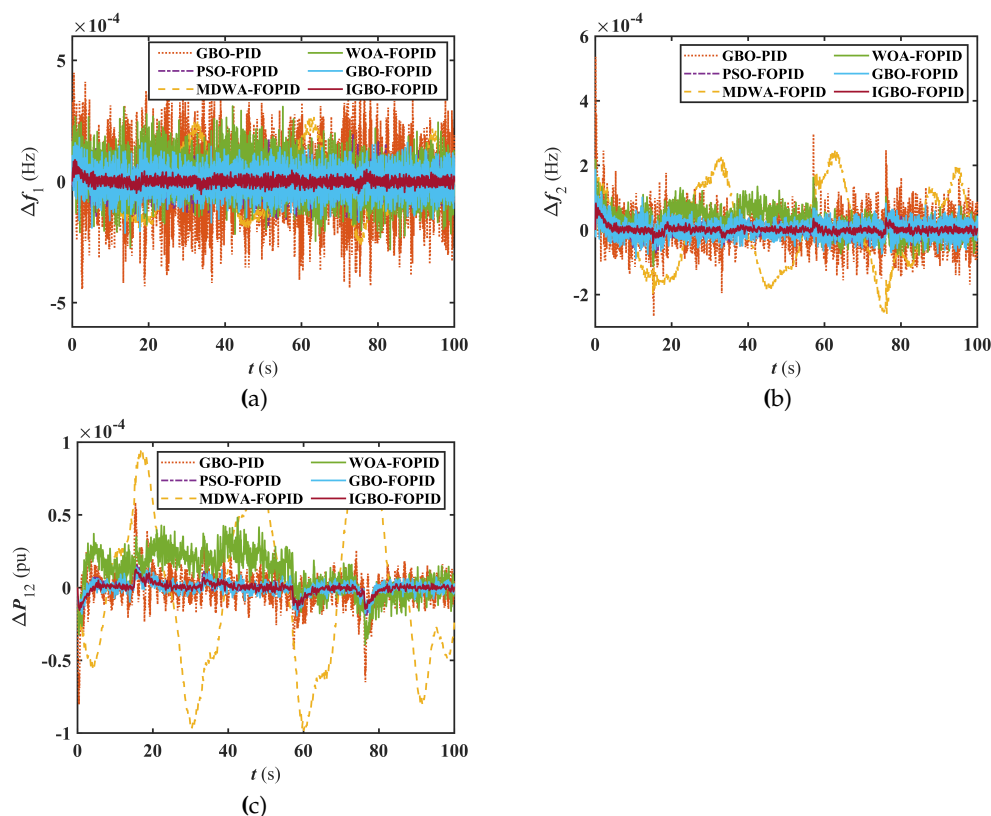
## 5.2. Photovoltaic and wind power random fluctuation test scenarios

The effectiveness of the IGBO-FOPID based LFC scheme is verified under the scenario of random power output from renewable energy sources. The output fluctuations of photovoltaic power and wind power, as described in literature [21], are utilized in this section. The fluctuations are visualized in Figure 6.



**Figure 6.** Photovoltaic and wind power fluctuation curves.

Keep the control parameters in Table 1 unchanged and use different LFC scheme for simulation. The response of IPS under random fluctuations in photovoltaic and wind power using different LFC schemes are shown in Figure 7. The maximum US/maximum OS/ISE/ITSE/IAE/ITAE of  $\Delta f_1/\Delta f_2/\Delta P_{tie12}$  results are displayed in Table 3.



**Figure 7.** Response curves of the IPS under photovoltaic and wind power random fluctuation scenarios: (a) frequency deviation in area 1, (b) frequency deviation in area 2, (c) tie line power.

**Table 3.** Maximum US/Maximum OS/ ISE/ITSE/IAE/ITAE of system response under photovoltaic and wind power random fluctuation scenarios.

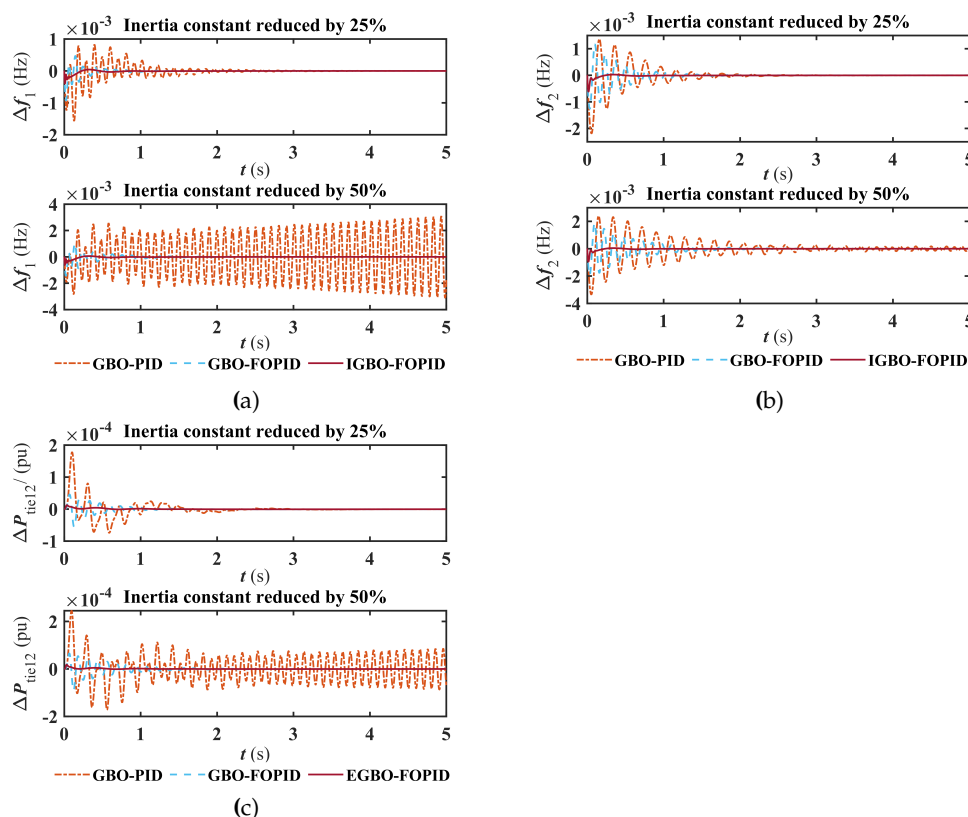
LFC scheme	Maximum US			Maximum OS			ISE	ITSE	IAE	ITAE
	$\Delta f_1$	$\Delta f_2$	$\Delta P_{tie12}$	$\Delta f_1$	$\Delta f_2$	$\Delta P_{tie12}$				
GBO-PID	-4.45e-4	-2.67e-4	-8.04e-5	4.49e-4	5.36e-4	5.84e-5	2.14e-6	9.95e-5	1.58e-2	0.77
PSO-FOPID	-1.83e-4	-7.30e-5	-2.45e-5	1.96e-4	1.68e-4	1.63e-5	3.90e-7	1.88e-5	6.58e-3	0.32
MDWA-FOPID	-2.61e-4	-2.59e-4	-9.84e-5	2.67e-4	2.49e-4	9.43e-5	3.35e-6	1.68e-4	2.62e-2	1.31
WOA-FOPID	-2.81e-4	-1.12e-4	-3.91e-5	3.11e-4	2.17e-4	4.82e-5	1.45e-6	5.87e-5	1.51e-2	0.69
GBO-FOPID	-2.13e-4	-8.77e-5	-1.94e-5	1.81e-4	1.87e-4	1.39e-5	4.99e-7	2.36e-5	8.12e-3	0.39
IGBO-FOPID	-5.27e-5	-4.07e-5	-1.55e-5	8.96e-5	8.25e-5	1.25e-5	5.25e-8	1.91e-6	2.55e-3	0.11

In Figure 7, one can find that the effectiveness of the offered IGBO-FOPID-based LFC scheme in regulating the IPS under scenarios involving random fluctuations in photovoltaic and wind power. Notably, the system incorporating the IGBO-FOPID-based LFC scheme exhibits smaller frequency fluctuations in two areas when compared to other LFC schemes. Additionally, the comparison presented in Table 3 reveals that the IPS performance with the IGBO-FOPID-based LFC scheme outperforms that of other LFC schemes in terms of maximum US, maximum OS, and various performance indicators. These findings highlight the superior anti-jamming capabilities of the proposed LFC scheme compared to other control methods. Thus, the proposed scheme is highly suitable for multi-source IPS applications incorporating renewable energy sources.

### 5.3. Robustness analysis

To evaluate the robustness of the IPS with an IGBO optimized FOPID controller, this section tests the dynamic responsiveness of the system when the system's own inertia constant is reduced by 25%

and 50%. System parameters are shown in the Appendix B. Leave the controller parameters in Table 1 remained unchanged, GBO-PID, GBO-FOPID and IGBO-FOPID based LFC schemes were tested, with the results presented in Figure 8.



**Figure 8.** Response curves of the IPS for different inertia constants: (a) frequency deviation in area 1, (b) frequency deviation in area 2, (c) tie line power.

In Figure 8, one can find that when the inertia constant of the IPS changes, the IPS with the proposed LFC scheme has the best frequency stability compared with those with the traditional GBO-PID based LFC scheme and the GBO-FOPID based LFC scheme, which further confirms that by using the proposed control scheme, the robustness and rapidness of the IPS can be improved.

## 6. Conclusion

This paper presents an LFC scheme based on optimal parameter optimization and tuning of FOPID controllers to address frequency fluctuation issues in an IPS involving renewable energy generation units. The introduction of FOPID controller increases the adjustable dimension of the system's load frequency controller parameters, allowing for greater flexibility. By utilizing an IGBO algorithm to tune the FOPID controller parameters, lower system frequency deviation performance indicators can be obtained. The proposed LFC scheme can effectively mitigate system frequency fluctuations, reduce the frequency fluctuation range, and exhibit excellent robustness.

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### Appendix A. Data of the two-area IPS.

Thermal power plant:  $T_G=0.08(s)$ ,  $T_T=0.3(s)$ ,  $R_T=2(\text{Hz/pu})$ ,  $T_r=10(s)$ ,  $K_r=0.5$ .

Photovoltaic power generator:  $K_{PV}=1(\text{Hz/pu})$ ,  $T_{PV}=1.8(s)$ .

Hydro power generator:  $T_R=5(s)$ ,  $T_{RH}=0.513(s)$ ,  $T_{GH}=48.7(s)$ ,  $T_W=0.5(s)$ ,  $R_H=2.4(\text{Hz/pu})$ .

Wind power generator:  $K_{WTG}=1(\text{Hz/pu})$ ,  $T_{WTG}=1.5(s)$ .  $T_{pw2}=0.041(s)$ ,  $T_{pw1}=6(s)$ ,  $K_{pw1}=1(\text{Hz/pu})$ ,  $K_{pw2}=1.75(\text{Hz/pu})$ ,  $R_W=2(\text{Hz/pu})$ .

Gas power generator:  $c_g=1(s)$ ,  $b_g=0.049(s)$ ,  $X_c=0.6(s)$ ,  $Y_c=1.1(s)$ ,  $R_G=2.4(\text{Hz/pu})$ ,  $T_{cr}=0.01(s)$ ,  $T_i=0.239(s)$ ,  $T_{cd}=0.2(s)$ .

Hydrogen storage unit:  $K_{HAE}=0.002(\text{Hz/pu})$ ,  $T_{HAE}=0.5(s)$ ,  $K_{FC}=0.01(\text{Hz/pu})$ ,  $T_{FC}=4(s)$ .

IPS:  $B=0.425(\text{pu/Hz})$ ,  $T_{12}=0.087(\text{pu/rad})$ ,  $T_{PS}=20(s)$ ,  $K_{PS}=100(\text{Hz/pu})$ .

### Appendix B. Data of the two-area IPS when the inertia changes.

Inertia reduced by 25%:  $B=0.319(\text{pu/Hz})$ ,  $T_{PS}=16(s)$ ,  $R_W=2.5(\text{Hz/pu})$ ,  $R_T=2.5(\text{Hz/pu})$ ,  $R_N=2.5(\text{Hz/pu})$ ,  $R_G=2.5(\text{Hz/pu})$ ,  $R_H=3(\text{Hz/pu})$ .

Inertia reduced by 50%:  $B=0.213(\text{pu/Hz})$ ,  $T_{PS}=10(s)$ ,  $R_W=3(\text{Hz/pu})$ ,  $R_T=3(\text{Hz/pu})$ ,  $R_N=3(\text{Hz/pu})$ ,  $R_G=3(\text{Hz/pu})$ ,  $R_H=3.6(\text{Hz/pu})$ .

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