
Fabrication of Fe₃O₄ Core-TiO₂/mesoSiO₂ and Fe₃O₄ Core-mesoSiO₂/TiO₂ Double Shell Nanoparticles for Methylene Blue Adsorption: Kinetic, Isotherms and Thermodynamic Characterization

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Keywords: magnetic core; silica shell; titania shell; water treatment; methylene blue; solvo-thermal process; adsorption



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Article

Fabrication of Fe₃O₄ Core-TiO₂/mesoSiO₂ and Fe₃O₄ Core-mesoSiO₂/TiO₂ Double Shell Nanoparticles for Methylene Blue Adsorption: Kinetic, Isotherms and Thermodynamic Characterization

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Abstract: Wastewater treatment for removal of dyes from industrial effluents prior to discharge into the water surfaces is necessary to achieve green and sustainable environment. The continuous production and processing of dyes resulted in severe negative impacts for the ecosystem. Herein, Fe₃O₄ core-TiO₂/mesoSiO₂ and Fe₃O₄ core-mesoSiO₂/TiO₂ double shell nanoparticles were prepared by first (R1) and second (R2) routes. The structure of the fabricated Fe₃O₄ is designed to achieve coating and protection of magnetic Fe₃O₄ core and to produce double shell around to enhance the efficiency for methylene removal by adsorption process. The reported adsorption capacities for R1-0.2, R1-0.4 and R2 samples were 46, 38 and 50 mg/g respectively which obtained after 80 min as equilibrium contact time at pH of 6, using methylene blue concentration of 50 ppm. The adsorption of methylene blue using the prepared Fe₃O₄core-meso SiO₂/TiO₂ double shell was analyzed by kinetic and isotherms models. In addition, the thermodynamic investigations are applied to assess the spontaneous nature of the process. The obtained results confirmed that the pseudo-second order model is well-fitted with the adsorption data as well as the Freundlich-isotherm assumption suggested multilayer adsorption mechanism. In addition, results of thermodynamic investigation indicated that the surfaces of Fe₃O₄ core-mesoSiO₂/TiO₂ and Fe₃O₄ core-TiO₂/mesoSiO₂ double shell exhibit spontaneous tendency to adsorb methylene blue from the aqueous solutions. These results will encourage the further application of Fe₃O₄ core-meso SiO₂/TiO₂ and Fe₃O₄ core-TiO₂/meso SiO₂ double shell for removal of broad range of contaminants from wastewater.

Keywords: magnetic Fe₃O₄; coating; wastewater purification; methylene blue; nanotechnology; adsorption-modeling

1. Introduction

The problems related to water pollution have become the most a global environmental issue during the recent decades [1–3]. These problems are owed to the excessive industrial-activities which cause continuous production of polluted liquid effluents. For example, there are many types of dyes are produced by huge amounts annually and applied in the textile fields. Part of these tremendous tones of dyes are contaminated with the discharge effluents [4,5]. These dyes are dispersed in various environmental components and cause hazard to human and animals. Furthermore, these pollutants resulted in bad esthetical view and cause significant damage to the water ecosystem [4,6,7]. Methylene blue (MB) dye is known as methylthionium chloride and classified as cationic dye [8]. The common industrial applications of methylene blue are painting and

paper industries, textiles fabrication, pesticides production, and pharmaceuticals products [9]. The water discharge from these industrial sections contains huge amounts of methylene blue dye which spread in the environment. the exposure to methylene blue cause negative impacts on human health such as vomiting, headache, cyanosis, jaundice, quadriplegia, shock, and others [10]. A large amount of dye $>7.0 \text{ mg kg}^{-1}$ causes mental disturbance, abdominal pain and nausea [11].

Currently, the most important methods for methylene blue removal is adsorption, biodegradation, chemical oxidation, photodegradation and membrane filtration. Among these treatment methods the adsorption process has showed a unique advantage such as low cost, easy performance and high removal efficiency [12–14]. The common adsorbent materials are zinc oxide, silica and silica derived materials, alumina and carbon. The broader materials categories as adsorbents include; fly ash, manganese oxide, nickel oxide and transition metal hydroxide which poses high potential for pollution remediation by adsorption [1,15]. However, the materials in the nano-size exhibit high surface area, fast dispersion in the adsorption medium leading to promised adsorption capacity compared to the traditional materials. The limitation of the nanomaterials that reduce their applicability in real field is the need for high speed centrifuge or nanofiltration to separate the adsorbent from the adsorption medium at the end of the treatment process [16,17]. To overcome this limitation, magmatic materials are introduced as adsorbents which enable high dispersion, porous structures as well as the possibility to be separated by external magnetic field [18]. Furthermore, the magnetic based nanomaterials can be prepared in a core-shell structure which allow easy functionalization with organic and/or inorganic species. The core-shell based nanomaterials open the space for tremendous adsorbent materials with amazing ability for adsorption and separation [19–21].

Different roots have been developed to prepare the core-shell based magnetic materials, however, the application of Fe_3O_4 nanoparticles as core is the most effective due to the superior magnetic properties [22–24]. The shell structure can be prepared by various coating of silica, carbon, polymer or titania to protect the magnetic core and enable various functionalization [25–27]. Salamat *et al.* have synthesized $\text{Fe}_3\text{O}_4(\text{np})@\text{TiO}_2$ shell structure for water treatment applications by photocatalytic-degradation of organic pollutants [28]. Shi *et al.* have prepared core-shell structure of $\text{Fe}_3\text{O}_4@\text{titanate}$ using the in-situ growth and hydrothermal assisted etching for application in wastewater treatment [29]. Zheng *et al.* have prepared $\text{Fe}_3\text{O}_4@\text{ZIF-8}$ as core-shell nanostructure and recommend them for removal of methylene blue with adsorption capacity of 20.2 mg g^{-1} [30]. Saini *et al.*, have applied the $\text{Fe}_3\text{O}_4@\text{Ag}/\text{SiO}_2$ as core-shell with excellent adsorption properties for removal of about 99.6% of methylene blue dye from aqueous solution of pH 7, and the adsorption mechanism was agreed with Langmuir isotherm assumption reporting with maximum monolayer adsorption-capacity (Q_{max}) of 128.5 mg/g [31]. Jaseela *et al.* have prepared inorganic – organic adsorbent including TiO_2 and PVA for selective adsorption of methylene blue with removal efficiency of 97.1% of MB. The adsorption kinetic was fitted with pseudo-second order-based model [32]. Zhan *et al.*, produced Fe_3O_4 -derived organic/inorganic hybrid-based adsorbent with various structured magnetic (np) by solvothermal and chemical-based co-precipitation method naming the products as S- Fe_3O_4 and C- Fe_3O_4 , respectively. The magnetic materials (S- Fe_3O_4 and C- Fe_3O_4) were further functionalized by dopamine (DA) and (3-aminopropyl) triethoxysilane (KH550) to produce at the end the core-shell $\text{Fe}_3\text{O}_4/\text{poly}(\text{DA} + \text{KH550})$ adsorbents. The application of these materials for methylene blue removal showed adsorption capacity higher than 400.00 mg g^{-1} , with well-fitting for the pseudo-second-order kinetic model and Langmuir isotherm model [33]. Schneider *et al.* have fabricated an adsorbent-composite from $\text{Fe}_3\text{O}_4@\text{SiO}_2@\text{carbon}$ for methylene blue removal [34]. Akbarbandari *et al.* have developed a bi-metallic and tri-metallic metal-organic frameworks (MOFs) supported on the magnetic activated carbon (MAC) were synthesized for methylene blue removal. The adsorption process was reported to follow the pseudo-second-order kinetic model and Langmuir isotherm model with maximum adsorption capacity of 66.51 and 71.43 mg/g for the bi-metallic and tri-metallic based magnetic nanocomposites, respectively [35]. However, the research are still continued to investigate the various roots for building magnetic core-shell based nanocomposites with porous structures and different shell combination of metal oxides to tune the properties of core shell

materials and improve their performance as adsorbents. Therefore, this work aimed to investigate various routes for fabrication of Fe₃O₄core-meso SiO₂/TiO₂ double shell for methylene blue adsorption. In addition to study the kinetic, isotherms and thermodynamic properties for the adsorptive-removal of methylene blue.

2. Materials and Methods

All applied chemicals were in high purity analytical grade. Ferric chloride-hexahydrate (FeCl₃·6H₂O), sodium acetate, sodium citrate, ammonia solution, TBOT, TEOS and cetyltrimethylammonium bromide were obtained from Sigma-Aldrich (USA).

2.1. Synthesis of Fe₃O₄ magnetic core

Certain weight of FeCl₃·6H₂O was dissolved in a certain volume of ethylene glycol, and then calculated amount of sodium acetate, tri-sodium citrate and polyethylene glycol were added. The mixture was vigorously and continuously stirred to ensure complete mixing, and then transferred to an autoclave made from stainless-steel and lined with Teflon and heated to around 190 °C for certain time, At the end and after reaching the room temperature, the produced Fe₃O₄ magnetic core was washed three times with ethanol, and then dried at 60 °C in an oven for approximately 6 h [36].

2.2. Synthesis of Fe₃O₄core-meso SiO₂/TiO₂ double shell nanoparticles

2.2.1. Coating with mesoporous silica

Fe₃O₄ core magnetic nanoparticles is coated with mesoporous silica shell according to the following procedure, Fe₃O₄ was dispersed in H₂O/ethanol mixture ultrasonically and then exact volume from NH₄OH added. Thereafter, specific weight from cationic surfactant (cetyltrimethylammonium bromide) is added, followed by the addition TEOS [37].

2.2.2. Titania Coating

To make a layer of titania onto the magnetic nanocores, the procedure described in the work of Jianping *et al.*, [38] was applied. In details, the silica coated magnetic nanocores were dispersed in ethanol and mixed with ammonia solution under ultrasonic stirring. TBOT was then added slowly. The reaction allowed to continue 24 h under mechanical stirring. Thereafter, the formed Fe₃O₄core-SiO₂/TiO₂ double shell nanoparticles were separated from the mother solution, washed several times with de-ionized water, then with ethanol, dried, and finally calcined at 500 °C for 2 h to form Fe₃O₄core-meso SiO₂/TiO₂ double shell nanoparticles.

2.3. Synthesis of multifunctional Fe₃O₄core-TiO₂/meso SiO₂ double shell nanoparticles

For fabrication of Fe₃O₄core-TiO₂/meso SiO₂ double shell nanoparticles, the titania layer was coated onto magnetic Fe₃O₄ core nanoparticle surface, then a silica coating as a second layer is made, and the samples will finally be calcined. In details, the magnetic nanocores were dispersed in ethanol and mixed with ammonia solution under ultrasonic stirring. Then TBOT is then added slowly (0.2 and 0.4 mL). The reaction was allowed to continuous mechanical stirring for 24 h. Thereafter, the produced Fe₃O₄ core-TiO₂ shell was separated from the mother solution, washed several times with de-ionized water, then with ethanol, dried, and finally calcined at 500 °C for 2 h air condition. The final step for coating meso SiO₂ onto Fe₃O₄core-TiO₂ was applied according to the following procedure, Fe₃O₄@TiO₂ as a core was dispersed in H₂O ultrasonically and the exact volume from NH₄OH was added. Thereafter, the cationic surfactant (cetyltrimethylammonium bromide) solution is added, followed by the addition TEOS [38]. The reaction was allowed for mechanical stirring for 6h. The formed Fe₃O₄ core-TiO₂/mesoSiO₂ double shell nanoparticles was separated from mother solution, washed with ethanol and water. Finally calcining the sample at 500 °C for 2 h to form Fe₃O₄ core-TiO₂/meso SiO₂ double shell nanoparticles.

2.4. Adsorptive-removal study for methylene blue

To investigate the fabricated Fe₃O₄ core-meso SiO₂/TiO₂ double shell for methylene blue uptake, the batch process was applied. A certain weight of fabricated Fe₃O₄ core-meso SiO₂/TiO₂ double shell was taken in 50 mL tube and mixed with the 25 mL of 50 ppm methylene blue dye solution. the mixture was shaken for 80 min; then the phases were separated by external magnetic field. The concentration of the methylene blue dye was measured by the Uv-Visible. Blank samples without fabricated Fe₃O₄ core-meso SiO₂/TiO₂ double shell were conducted in all experiments. the adsorption capacity (qe) was calculated from the equation (1):

$$q_e = (C_0 - C_e) \cdot V/M, \quad (1)$$

where C₀ is the primary concentration of methylene blue solution, C_e is final methylene blue concentration, V represent the volume of the adsorption solution, and M is the adsorbent mass (g) (Fe₃O₄ core-meso SiO₂/TiO₂ double shell).

The procedures for the adsorption of methylene blue onto Fe₃O₄ core-meso SiO₂/TiO₂ double shell were repeated to investigate the most important factors such as pH, contact time, methylene blue dye concentration and temperature, which significantly affecting the uptake of methylene blue onto fabricated Fe₃O₄ core-meso SiO₂/TiO₂ double shell.

3. Results and discussion

3.1. Characterization of Fe₃O₄ core-double shell

Multi-procedures have been applied to prepared Fe₃O₄ core-meso SiO₂/TiO₂ double shell with alternative sequence of titania and silica. In the first stage, the homogenous spherical magnetic noncore (Fe₃O₄) is obtained via solvo-thermal process which resulted in separated particle with average size between 50 nm and 100 nm (Figure 1). The obtained magnetic nanocore is applied to fabricate Fe₃O₄ core-meso SiO₂/TiO₂ double shell or Fe₃O₄ core-TiO₂/meso SiO₂ double shell.

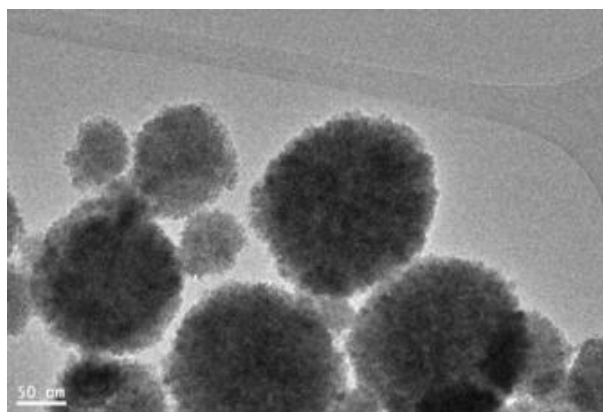


Figure 1. TEM images of Fe₃O₄ nanocores prepared by solvothermal method.

To fabricate Fe₃O₄@TiO₂@m-SiO₂, Fe₃O₄ nanoparticles using the first route. The nanoparticles were firstly coated with TiO₂ shell then secondly with mesoporous silica shell then finally calcination process is conducted to crystallize TiO₂ shell and to remove surfactant from silica shell to transform it to mesoporous one. TiO₂ coating into Fe₃O₄ nanoparticles was conducted by Stöber-modified approach where citrate modified Fe₃O₄ nanoparticles are dispersed in ethanol solution then ammonium hydroxide and titanium butoxide is added to the above mixture where the coating process are conducted at 45 °C for 20h. Mesoporous silica step was conducted onto TiO₂ coated Fe₃O₄ by using Stöber approach through adding cationic surfactant (Cetyl trimethylammonium bromide (CTAB)). Finally, the calcination process was conducted to ensure the crystallization of TiO₂ shell and to remove CTAB to get mesoporous silica shell. TEM observation (Figure 2a) showed the formation of ~ 25 nm of TiO₂ layer around Fe₃O₄ nanocores. TEM image (Figure 2b) revealed the

$\text{Fe}_3\text{O}_4@\text{TiO}_2@m\text{-SiO}_2$ structure was formed with shell thickness of 20 nm. In route R1, two different samples $\text{Fe}@Ti@m\text{-Si-0.2(R1-0.2)}$ and $\text{Fe}@Ti@m\text{-Si-0.4(R1-0.4)}$ we synthesized with adding 0.2 and 0.4 mL of TEOS, respectively. The thickness of shell layer was 20 and 45 nm for R1-0.2 and R2-0.4 sample, respectively.

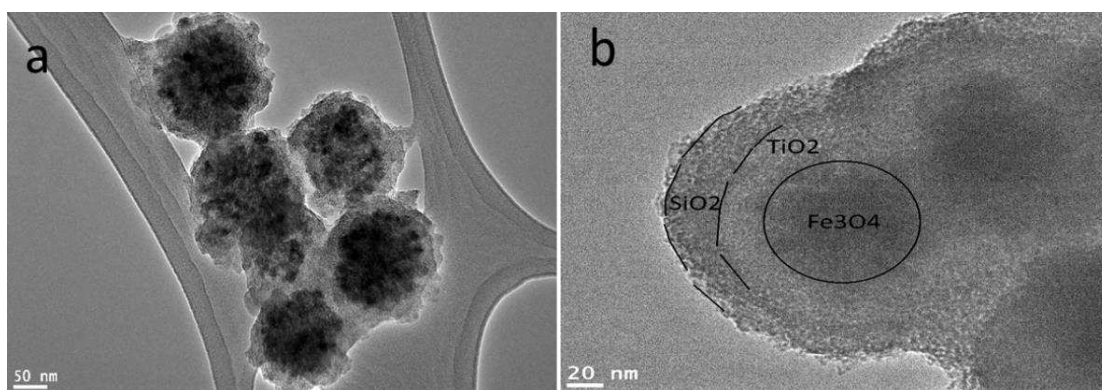


Figure 2. TEM image of (a) titania coated Fe_3O_4 nanocores and (b) $\text{Fe}_3\text{O}_4@\text{TiO}_2@m\text{-SiO}_2$ by first route (R1).

To fabricate Fe_3O_4 core-meso $\text{SiO}_2/\text{TiO}_2$ double shell using second route (sample R2), the magnetic nano-cores were subjected first to mesoporous silica coating, then to the formation of the second shell by TiO_2 coating. To achieve uniform formation of $\text{Fe}_3\text{O}_4@m\text{esoSiO}_2$, Stöber method in the presence of cationic surfactant was applied to form mesoporous silica layer around the magnetic nano-cores followed by titania coating as showed in Figure 3. The mesoporous silica layer is about 20 nm (Figure 3a). The second step to coat TiO_2 on the fabricated Fe_3O_4 core-meso SiO_2 , was achieved by hydrolysis of titanium butoxide which successfully formed a uniform 20 nm layer of TiO_2 (Figure 3b) to finally form the Fe_3O_4 core-meso $\text{SiO}_2/\text{TiO}_2$ double shell (Figure 3). Finally calcine Fe_3O_4 core-meso $\text{SiO}_2/\text{TiO}_2$ double shell sample at 550 °C was performed to crystallize TiO_2 layer and to remove surfactant in one single step.

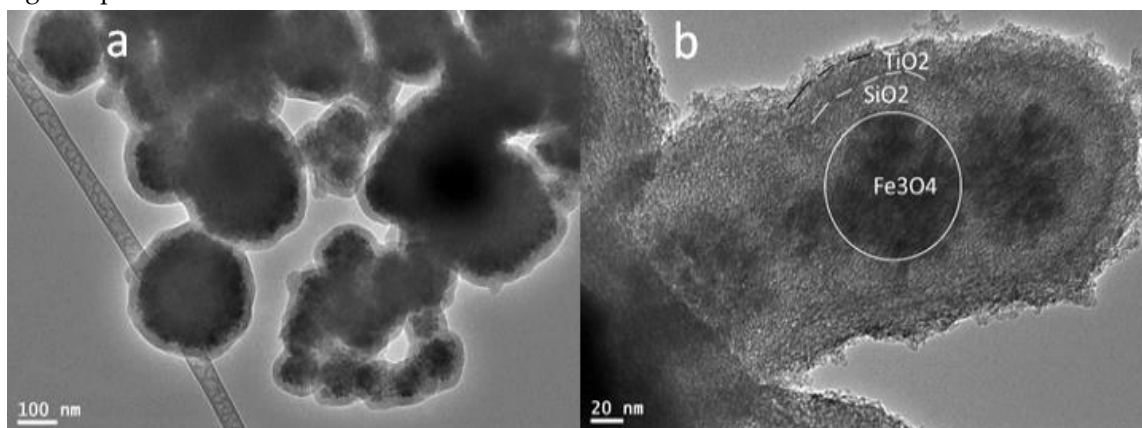


Figure 3. TEM image of (a) single shell mesoporous silica coated Fe_3O_4 nanocores and (b) double shell $\text{Fe}_3\text{O}_4@m\text{-SiO}_2@\text{TiO}_2$ by second route (R2).

N_2 adsorption-desorption isotherm was conducted for core-double shell nanoparticles prepared by route1 (at 0.2 and 0.4 ml TEOS) and route 2 at 77 K and presented in Figure 4. The prepared core-double shell derived nanoparticles even by route 1 or route 2 exhibited porous structure with type IV isotherm. It is clear that nanoparticles prepared by route 1 where silica shell is outer layer had higher surface area as well as larger pore volume (Table 1 and Figure 4A) when compared with nanoparticles prepared with route 2 where TiO_2 shell is the outer one. Moreover, these results can be explained based on porous character of silica shell compared with crystalline dense character of TiO_2 one. However, changing the silica content caused as slight increment in the surface area and pore

volume of the formed sample. Moreover, the pore size was much bigger in case of the core-double shell nanoparticles prepared by route 1 than samples of route 2 (Table 1 and Figure 4B).

Table 1. textural properties for magnetic cores-double shell prepared by route 1 and 2.

Sample	BET S. A. m ² /g	Pore volume cm ³ /g	Pore size A ^o
Fe@Ti@m-Si-0.2(R1-0.2)	1133.28	0.74	25.79
Fe@Ti@m-Si-0.4(R1-0.4)	1207.49	0.88	29.86
Fe@m-Si@Ti (R2)	52.27	0.03	24.02

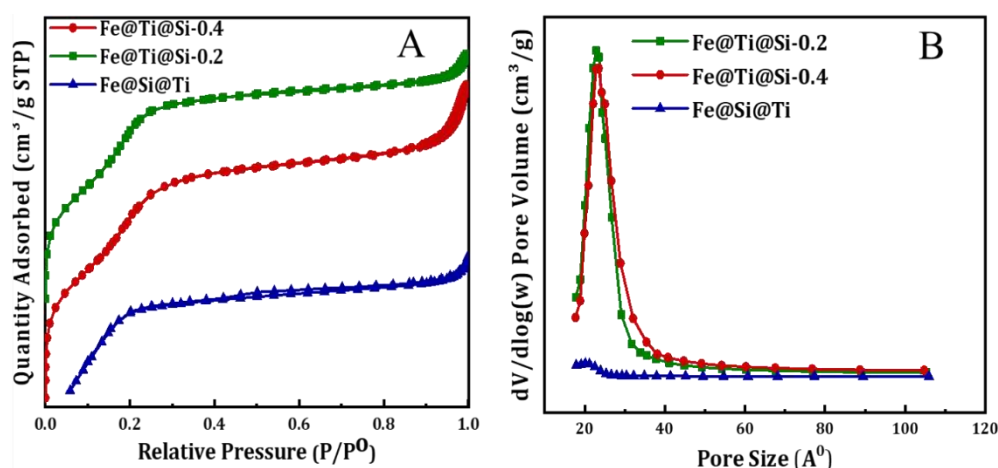


Figure 4. (A) N₂ sorption isotherm and (B) pore size distribution of calcined Fe₃O₄@TiO₂@m-SiO₂ at TEOS amount of 0.2, 0.4 mL prepared by route 1 (R1) and calcined Fe₃O₄@m-SiO₂@TiO₂ prepared by route 2 (R2).

FTIR measurements core-double shell nanoparticles prepared by route1 (at 0.2 and 0.4 ml TEOS) and route 2 (Figure 5). Si-O peak can be seen formed at 1050-1250 cm⁻¹. The Fe-O-Si peak that refer for chemical binding between Fe₃O₄ and silica, cannot be seen in the FTIR spectrum because it appears at around 584 cm⁻¹ and therefore overlaps with the Fe-O vibration of magnetite nanoparticles. The peaks at 1632 cm⁻¹ and 3425 cm⁻¹ corresponding to the vibration of hydroxyl groups (-OH) on the surface of Fe₃O₄ nanoparticles. The peak at 970 cm⁻¹ can be attributed to Ti-O-Si bond while the shoulder at 1400 cm⁻¹ can be due to band to Ti-O-Ti vibration.

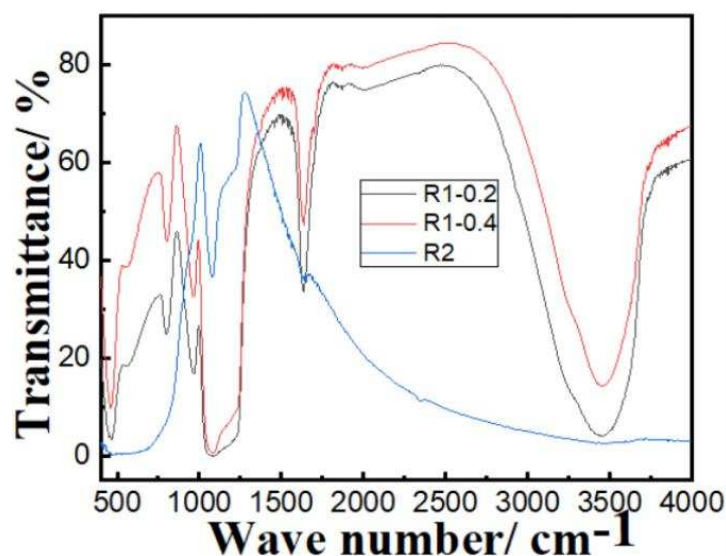


Figure 5. FTIR spectra of calcined Fe₃O₄@TiO₂@m-SiO₂ at TEOS amount of 0.2 and 0.4 mL prepared by route 1 (R1) and calcined Fe₃O₄@m-SiO₂@TiO₂ prepared by route 2 (R2).

3.2. Adsorptive-remediation investigation

Methylene blue is extensively used in the industrial section for dyeing and painting, resulting huge amount of colored discharge and produce many negative environmental impacts [39–41]. Herein, three adsorbent materials including the core double shell structures from R1-0.2, R1-0.4 and R2 are applied for methylene blue dyes by adsorptive-removal. The effect of the pH of the medium is investigated by varying the pH of the methylene blue sample solution from 2 to 7 (Figure 6). In the strong acidic medium the adsorption capacities for methylene blue removal using R1-0.2, R1-0.4 and R2 were in the lowest values, then increased with increasing the pH reaching its maximum value between pH 6 and 7. The lower adsorption capacity at strong pH medium may be owed to the protonation of the adsorbent surfaces [42,43].

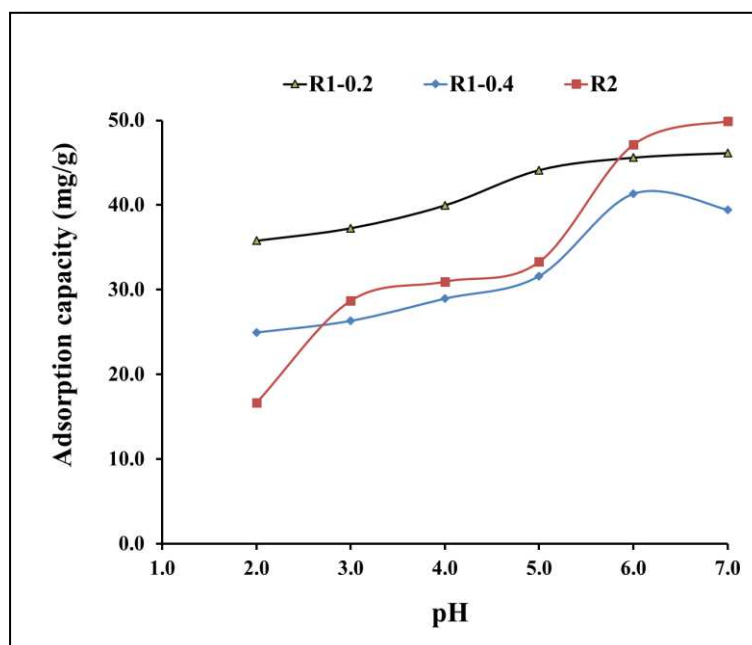


Figure 6. pH investigation for methylene blue adsorption onto R1-0.2, R1-0.4 and R2.

The effect of contact time on the de-colorization of dyes from aqueous solution by adsorption is investigated to assess the rate and efficiency of the process [44,45]. The effect of time is studied from 5 min to 180 min and the adsorption capacities for R1-0.2, R1-0.4 and R2 for methylene blue uptake are presented in Figure 7. The adsorption capacities after 1 min were 11, 9 and 15 for R1-0.2, R1-0.4 and R2, respectively, then increased till reach the equilibrium at 80 min recording adsorption capacity of 46, 38 and 50 mg/g. By increasing time from 80 min to 180 min, there are no noticeable improvement in the adsorption capacities were detected due to the occurrence of the steady state.

The rate of the mass transfer of methylene blue during adsorption process onto R1-0.2, R1-0.4 and R2 was studied by applying the kinetic models of pseudo first order and pseudo second order [46,47] as presented in Figures 8 and 9, respectively. From the data correlation, the pseudo second order kinetic model was found to be more comfortable for describing the rate of the adsorption process. The pseudo-first-order equation of Lagergren, is generally expressed in the integrated form of Equation (2):

$$\log(q_e - q_t) = \log q_e - k_1 t / 2.303 \quad (2)$$

By plotting $\log(q_e - q_t)$ versus time t , (Figure 8), The pseudo-first-order rate constant, k_1 , is calculated and reported in Table 2. In addition, the pseudo-second-order kinetic rate equation is expressed in the integrated form of Equation (3):

$$t/qt = 1/Kq_e^2 + 1/q_e \cdot t \quad (3)$$

where t is the time (min), and q_e (mg/g) and q_{e2} (mg/g) is the quantity of methylene blue adsorbed at equilibrium onto fabricated R1-0.2, R1-0.4 and R2 samples at pH 6 and 25 °C. Figure 9 present the plotting of t/qt versus t . the q_e and k parameters is calculated using the slope and intercept, respectively, according to second-order kinetic model equation (3).

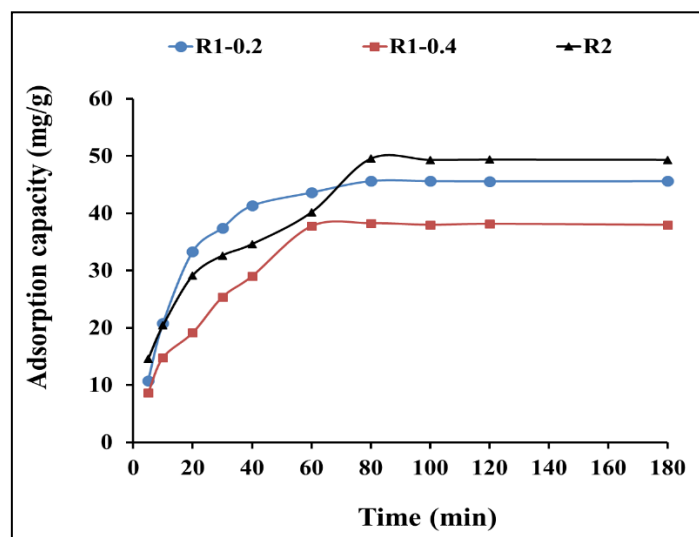


Figure 7. Time investigation for methylene blue adsorption onto R1-0.2, R1-0.4 and R2.

Table 2 shows the calculated parameters values and the linear regression correlation coefficient values. The pseudo second-order kinetic rate equation model fitting was much better than for the pseudo-first-order one. The obtained results confirm the assumption related to the second-order kinetic model including fast adsorption process. In addition, the adsorption dynamic is dependent on the migration of the methylene blue molecules to the surface of the fabricated Fe_3O_4 core-meso SiO_2/TiO_2 double shell adsorbent and finally, migration of the methylene blue molecules to the entire pores of the fabricated Fe_3O_4 core-meso SiO_2/TiO_2 double shell adsorbent [48,49].

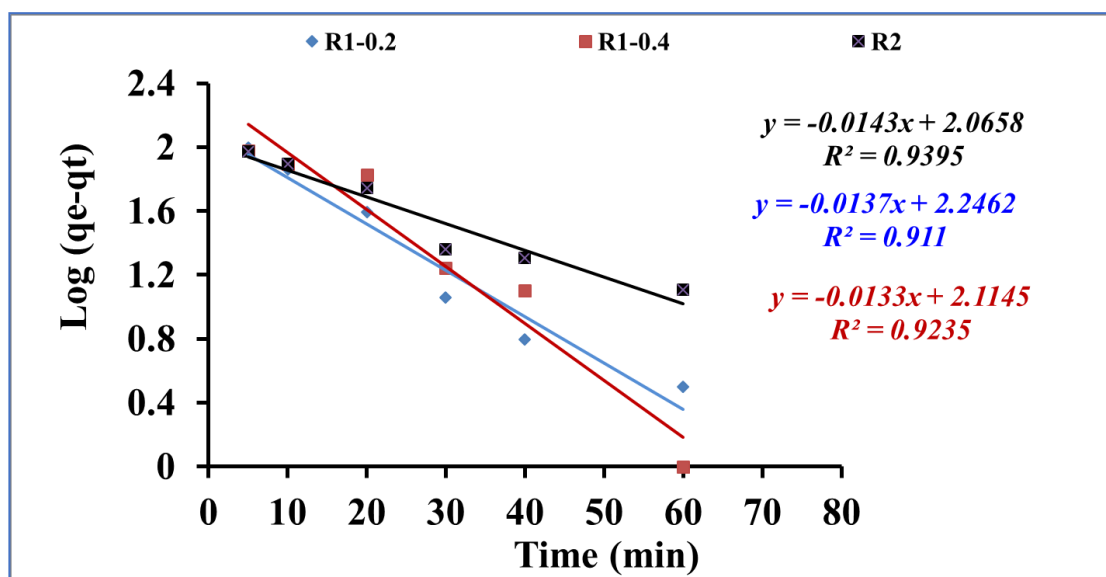


Figure 8. Pseudo first order kinetic model for methylene blue adsorption onto using R1-0.2, R1-0.4 and R2.

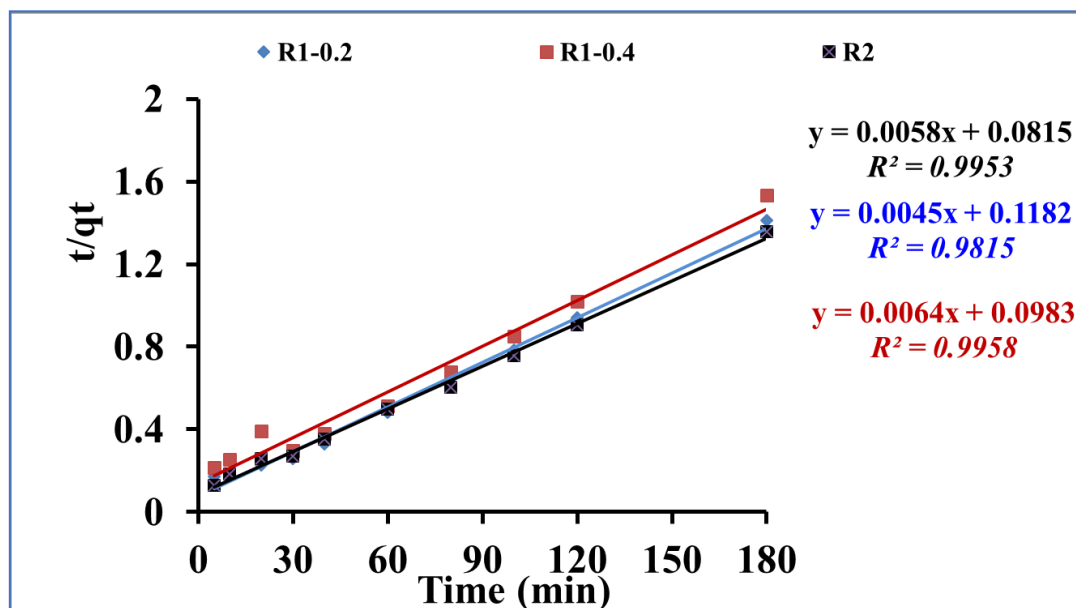


Figure 9. Pseudo second order kinetic model for methylene blue adsorption onto using R1-0.2, R1-0.4 and R2.

Table 2. Kinetic constant parameters obtained for methylene blue adsorption onto using R1-0.2, R1-0.4 and R2.

	Pseudo-First-Order				Pseudo-Second-Order		
	q_e, exp (mg/g)	$K_1 (\text{min}^{-1})$	$q_e, \text{cal} (\text{mg/g})$	R^2	$k_2 (\text{g/mg} \cdot \text{min})$	$q_e, \text{cal} (\text{mg/g})$	R^2
R1 -0.2	128	0.031	176.27	0.91	$1.71 \cdot 10^{-4}$	222.22	0.98
R1-0.4	118	0.03	130.16	0.93	$4.16 \cdot 10^{-4}$	156.25	0.99
R2	133	0.032	116.35	0.92	$4.12 \cdot 10^{-4}$	172.41	0.99

3.3. Isotherms Study

The investigation of the effect of concentration of methylene blue at constant temperature (isotherms) on the adsorption capacity using fabricated R1-0.2, R1-0.4 and R2 samples is applied to assess the distribution methylene blue as adsorbate within the liquid sample solution and the solid fabricated Fe_3O_4 core-meso $\text{SiO}_2/\text{TiO}_2$ double shell adsorbent at the equilibrium [50–53]. The Langmuir equation (4) was used to model the adsorption data for methylene blue uptake onto fabricated Fe_3O_4 core-meso $\text{SiO}_2/\text{TiO}_2$ double shell adsorbent (R1-0.2, R1-0.4 and R2 samples) [54]:

$$C_e/Q_e = 1/(q_{\text{max}} \cdot b) + C_e/q_{\text{max}}, \quad (4)$$

where C_e is the concentration of methylene blue (mg/L) at equilibrium, Q_e is the quantity of methylene blue adsorbed (mg/g), and q_{max} and b is Langmuir model constants (Figure 10). The correlation coefficients, R^2 , for adsorption data for methylene blue adsorption onto fabricated R1-0.2, R1-0.4 and R2 samples were low, indicating that the adsorption data was not fitted by the Langmuir isotherm.

The Freundlich model assume the adsorption process occur as multi-layers of adsorbate molecules (methylene blue) onto the surface of adsorbent (Fe_3O_4 core-meso $\text{SiO}_2/\text{TiO}_2$ double shell). The obtained data for adsorption data for methylene blue adsorption onto fabricated R1-0.2, R1-0.4 and R2 samples were subjected to Freundlich equation [55] (Equation (5)):

$$\text{Log } q_e = \text{log } K_f + 1/n \text{ log } C_e, \quad (5)$$

where C_e is the concentration of methylene blue (mg/L) at equilibrium, Q_e is the quantity of methylene blue adsorbed (mg/g). K_F (mg/g) is the Freundlich constant for the adsorbent capacity and n is related to the favorable nature of the adsorption process. Figure 11 shows the plotting of $\log q_e$ and $\log C_e$. From Freundlich equation and Figure 11 the slope and intercept indicate $1/n$ and $\log K_F$, respectively.

The adsorption of methylene blue using Fe_3O_4 core-meso SiO_2/TiO_2 double shell (R1-0.2, R1-0.4 and R2 samples) showed agreement with Freundlich model ($R^2 > 0.9$) for the tested range of concentrations used in this study, suggesting multilayer adsorption process.

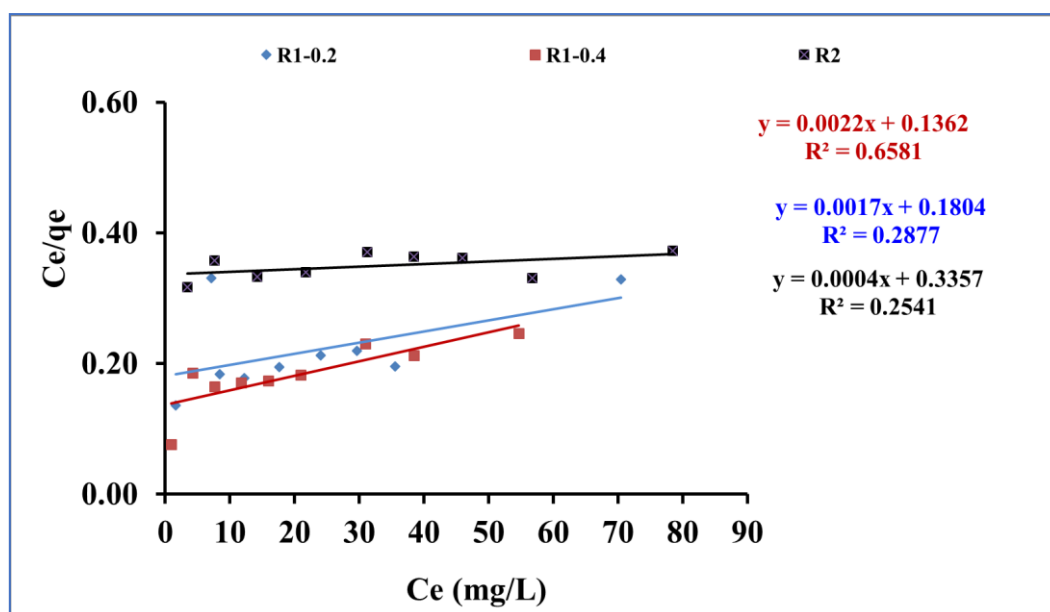


Figure 10. Langmuir for methylene blue adsorption onto using R1-0.2, R1-0.4 and R2.

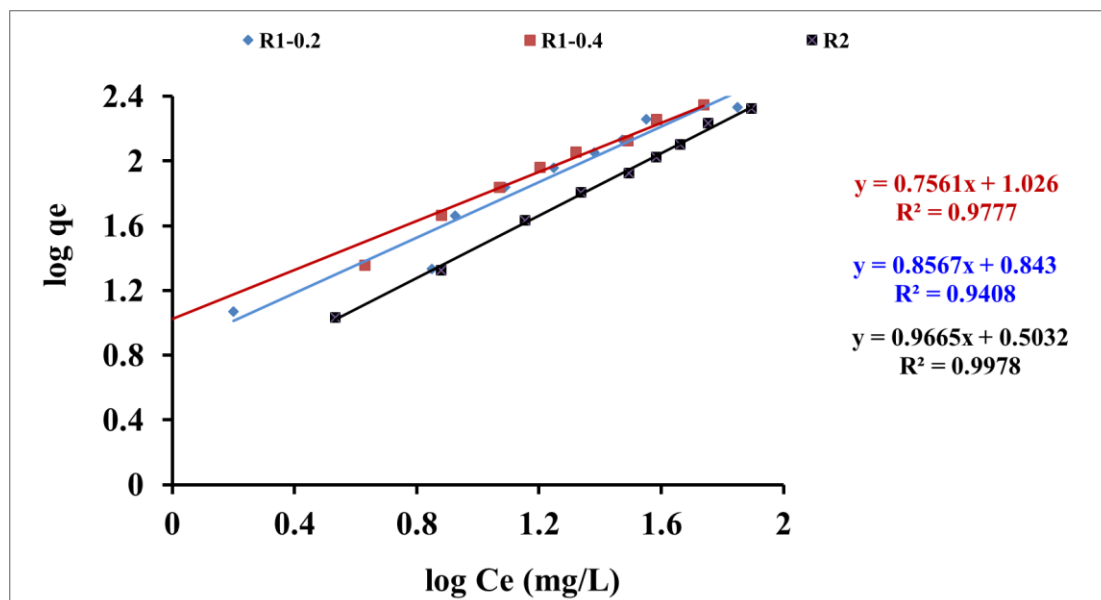


Figure 11. Freundlich isotherm for methylene blue adsorption onto using R1-0.2, R1-0.4 and R2.

Table 3. Langmuir and Freundlich parameters for methylene blue adsorption onto using R1-0.2, R1-0.4 and R2.

	Langmuir Constants				Freundlich Constants		
	K_L	b	Q_{max}	R^2	K_F	n	R^2
R1-0.2	5.54	9.4×10^{-3}	588.2	0.28	6.96	1.16	0.94
R1-0.4	7.34	0.016	454.5	0.65	10.61	1.32	0.97
R2	2.97	1.19×10^{-3}	2500	0.25	3.18	1.03	0.99

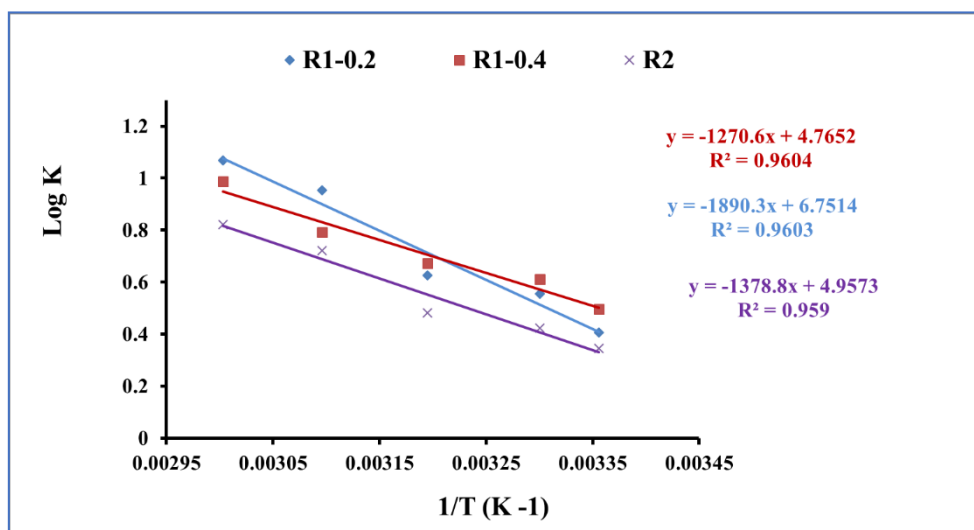
3.4. Thermodynamic Studies

Adsorption process is strongly influenced by temperature of the adsorption medium [56–58]. The temperature effect has been studied to evaluate the nature of the adsorption process of methylene blue onto fabricated Fe₃O₄ core-meso SiO₂/TiO₂ double shell. The thermodynamic parameters, including; the Gibbs free energy (ΔG°), enthalpy (ΔH°), and entropy (ΔS°) of the adsorption process of methylene blue onto fabricated R1-0.2, R1-0.4 and R2 samples are evaluated from Equations (6) and (7):

$$\log K_d = \Delta S^\circ / 2.303R - \Delta H^\circ / 2.303RT \quad (6)$$

$$\Delta G^\circ = -RT \ln K_d, \quad (7)$$

where K_d is refer to equilibrium partition constant which is calculated as the ratio between sorption capacity of Fe₃O₄ core-meso SiO₂/TiO₂ double shell (q_e) and methylene blue equilibrium concentration (C_e), R represent the gas-constant (8.314 J/mol K), and T is the temperature in Kelvin (K). From Equation (6), the plot of $\log K_d$ and $1/T$ (Figure 12), enable the calculation of ΔH° and ΔS° values.

**Figure 12.** Thermodynamic parameters for methylene blue adsorption onto using R1-0.2, R1-0.4 and R2.

Gibbs free energy (ΔG°), enthalpy (ΔH°), and entropy (ΔS°) are presented in Table 4. ΔG° was obtained as negative values in the range (-2.3 to -6.8 kJ/mol) for R1-0.2, (-2.8 to -6.3 kJ/mol) for R1-0.4, and (-2.0 to -5.2 kJ/mol) for R2. In addition, the ΔH° and ΔS° values were found in the range of 26.4 to 36.19 kJ.mol⁻¹ and 94.9 to 126.3 Jmol⁻¹ K⁻¹, respectively. The calculated thermodynamic parameters indicated that the adsorption process of methylene blue onto fabricated R1-0.2, R1-0.4

and R2 samples is spontaneous with physical in nature endothermic. Furthermore, the adsorption process of methylene blue increases the degree of freedom during adsorption interaction process [59,60].

Table 4. Thermodynamic parameters for methylene blue adsorption onto using R1-0.2, R1-0.4 and R2.

	Temperature T(K)	Thermodynamic Parameters		
		ΔG° (kJ/mol)	ΔS° (J/mol/K)	ΔH° (kJ/mol)
R1-0.2	273	-2.3		
	278	-3.2		
	288	-3.7	129.3	36.19
	298	-5.9		
	308	-6.8		
R1-0.4	273	-2.8		
	278	-3.5		
	288	-4.0	91.2	24.33
	298	-4.9		
	308	-6.3		
R2	273	-2.0		
	278	-2.5		
	288	-2.9	94.9	26.40
	298	-4.5		
	308	-5.2		

4. Conclusions

Multistep fabrication processes have been investigated to fabricate Fe₃O₄ core-TiO₂/mesoSiO₂ and Fe₃O₄ core-mesoSiO₂/TiO₂ double shell nanoparticles were prepared by first (R1) and second (R2) routes as magnetic materials for adsorption of methylene blue. The TEM examination showed the successful formation of magnetic core-double shell structure including silica layer and titania layer of 20 nm thickness. The prepared magnetic core-double shell nanoparticles exhibit surface area of 1133, 1207, and 52.27 m²/g for R1-0.2, R1-0.4 and R2 samples, respectively. The removal of methylene blue was operated at pH 6 with contact time of 80 min to reach the steady state with adsorption capacity of 46, 38 and 50 mg/g for R1-0.2, R1-0.4 and R2, respectively. Upon Applying the kinetic models, the pseudo-second-order kinetic model was well fitted with adsorption data for removal of methylene blue onto fabricated Fe₃O₄ core-TiO₂/mesoSiO₂ and Fe₃O₄ core-mesoSiO₂/TiO₂ double shell nanoparticles (R1-0.2, R1-0.4 and R2 samples). The Freundlich isotherm showed good correlation with adsorption data suggesting a multilayer adsorption. The thermodynamic parameters confirm that the adsorption process of methylene blue onto fabricated magnetic core-double shell structure is spontaneous and physical in nature.

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