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Analysis of Phase Diagram of CaO-CoO_x-ErO_y and Crystal Structure of Perovskite (Ca_{3-x}Er_x)Co₂O_{6-z} Solid Solution

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Abstract: In this work, a series of compounds in the CaO-CoO_x-ErO_y ternary oxide system were synthesized in air at 885 °C using high temperature solid-phase synthesis method. Phase boundary of each solid solution region in the CaO-CoO_x-ErO_y system was determined by X-ray powder diffraction technique. The phase diagram of the CaO-CoO_x-ErO_y system at 885 °C includes three series of ternary oxide solid solutions : (Ca_{3-x}Er_x)Co₄O_{9-z} (0 ≤ x ≤ 0.9), (Ca_{3-x}Er_x)Co₂O_{6-z} (0 ≤ x ≤ 1.25) and (Er_{1-x}Ca_x)CoO_{3-z} (0 ≤ x ≤ 0.33). Four three-phase regions and five solid solution tie-line regions were obtained. The structure of perovskite solid solution (Ca_{3-x}Er_x)Co₂O_{6-z} has been analyzed by Rietveld refinements. With the increase of Er content, the cell parameters of (Ca_{3-x}Er_x)Co₂O_{6-z} exhibit an decreasing trend in *a* and *b* directions and an increasing trend in *c* direction. A brief comparison of the phase diagrams of the CaO-CoO_x-RO_y (R=La, Dy, and Er) systems in air at 885 °C is given.

Keywords: Phase diagram of CaO-CoO_x-ErO_y system; Thermoelectric oxide system; Perovskite and its derived structures; Structure for (Ca_{3-x}Er_x)Co₂O_{6-z}

1. Introduction

The increasing demand for energy in everyday life, coupled with concerns about climate change, has prompted the scientific community to explore materials for more efficient energy conversion and storage. Perovskite [1-3] is a kind of outstanding materials, including metal halides and perovskite oxides, which has a good development prospect as energy materials and can effectively replace traditional materials. In 1839, Russian geologist Lev Perovski discovered the structure of ABO₃. Because the perovskite structure was generated by the discovery of the special structure of CaTiO₃ in calcium titanate during the study of perovskite, the structure of ABO₃ is called the perovskite structure. The perovskite structure is also called the 113 structure because the proportion of the elements in ABO₃ is A:B:O=1:1:3. The spatial group of the standard perovskite structure is P m3m. In ABO₃, A is a alkaline earth metal or rare earth ion with a relatively large ionic radius, B is a transition metal ion with a relatively small ionic radius, and O is oxygen ion [4,5].

In recent years, perovskite-type thermoelectric materials have made breakthrough progress, but only a few of them have been found to have practical industrial applications due to the low efficiency. To measure the performance of thermoelectric materials the dimensionless figure of merit (*zT*), given by $zT = S^2 \sigma T / \kappa$ [6-8], where *S* is the Seebeck coefficient or thermopower, σ is the electrical conductivity ($\sigma = 1/\rho$, ρ is electrical resistivity), κ is the thermal conductivity, and *T* is the absolute temperature, has been used. However, due to the correlation of *S*, ρ and κ , it is a difficult task to optimize the *zT* value. High quality thermoelectric materials need to meet the following requirements: high electrical conductivity, high Seebeck coefficient, and low thermal conductivity.

Thermoelectric oxides have been considered as possible candidates for waste heat conversion applications because of their stability at high temperatures. Low-dimensional oxide thermoelectric materials, including chain oxides Ca₃Co₂O₆ [9-11] and layered oxides Ca₃Co₄O₉ [12-20], NaCo₂O₄ [21], Bi₂Sr₂Co₂O_x [22] and natural superlattices (Bi,A)OCuSe (A=Pb, Ba, Sr, Ca) [23], are considered as

candidates for waste heat conversion applications. Among them, the 2D mismatched layered oxide $\text{Ca}_3\text{Co}_4\text{O}_9$ exhibited the highest ZT value. Much work has been done to improve the thermoelectric properties of $\text{Ca}_3\text{Co}_4\text{O}_9$ by doping at Ca or Co sites [24-27].

Phase equilibrium diagrams which provide blue prints for processing and understanding phase relationships are important for designing and understanding materials properties, phase diagrams of the $\text{CaO-CoO}_x\text{-RO}_y$ (R=lanthanide) systems are of interest to the thermoelectric research community. Phase diagrams of $\text{CaO-CoO}_x\text{-RO}_y$ systems for R= La [28], Nd [29], Sm [30], Eu [31], Gd [32], Dy [33] and Ho [34] have been reported. In the $\text{CaO-CoO}_x\text{-RO}_y$ system, there are $\text{Ca}_3\text{Co}_4\text{O}_9$, $\text{Ca}_3\text{Co}_2\text{O}_6$ and RCoO_3 phases, all of which have perovskite or its derivative structure and have excellent thermoelectric properties.

In this study, we have established the phase compatibility relationships, crystal chemistry, and crystallography of selected compounds in the $\text{CaO-CoO}_x\text{-RO}_y$ systems at 885 °C (R=Er in this report), particularly to obtain subsolidus phase relationships in the vicinity of the $\text{Ca}_3\text{Co}_4\text{O}_9$ and $\text{Ca}_3\text{Co}_2\text{O}_6$ compounds. Possible formation of $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_4\text{O}_{9-z}$, $(\text{Er}_{1-x}\text{Ca}_x)\text{CoO}_{3-z}$ and $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_2\text{O}_{6-z}$ solid solutions and the effect of doping on the crystal structure are also discussed. In addition, the phase formation and phase relationships between $\text{CaO-CoO}_x\text{-LaO}_y$ [28], $\text{CaO-CoO}_x\text{-DyO}_y$ [33], and the $\text{CaO-CoO}_x\text{-ErO}_y$ systems are compared. These reference patterns will be included in the ICDD Powder Diffraction File (PDF [35]).

2. Materials and Methods

2.1. Sample preparation

The samples were prepared by high temperature solid-state synthesis technique. **Table 1** gives 52 samples prepared from stoichiometric mixtures of CaCO_3 , Co_3O_4 and Er_2O_3 (all with purity greater than 99%). The samples were mixed, pelletized, and sintered at 850 °C for 6 hours, its purpose is to calcinate CaCO_3 at high temperature and react CaCO_3 into CaO . The samples are ground repeatedly, the particles are small after grinding, and the samples are mixed evenly. They were then sintered at 885 °C for 6-9 days, with grinding, and the heat treatment process repeated until the powder X-ray diffraction pattern showed no further change.

Table 1. Fifty-two samples (mole fraction, %) prepared for the phase equilibria study of the $\text{CaO-CoO}_x\text{-ErO}_y$ system at 885 °C in air. In this table, Ca= CaO ; Co= $\frac{1}{3}\text{Co}_3\text{O}_4$; Er= $\frac{1}{2}\text{Er}_2\text{O}_3$.

Sample#	Ca	Co	Er
#01	0.05	0	0.95
#02	0.08	0	0.92
#03	0.1	0	0.9
#04	0.95	0	0.05
#05	0.98	0	0.02
#06	0.05	0.2	0.75
#07	0.2	0.2	0.6
#08	0.55	0.24	0.21
#09	0.65	0.25	0.1
#10	0	0.3333	0.6667
#11	0.3	0.3333	0.3667
#12	0.31	0.3333	0.3567
#13	0.32	0.3333	0.3467
#14	0.3333	0.3333	0.3334
#15	0.35	0.3333	0.3167

#16	0.39	0.3333	0.2767
#17	0.4	0.3333	0.2667
#18	0.42	0.3333	0.2467
#19	0.43	0.3333	0.2367
#20	0.45	0.3333	0.2167
#21	0.5	0.3333	0.1667
#22	0.55	0.3333	0.1167
#23	0.4	0.4	0.2
#24	0.5	0.4	0.1
#25	0.55	0.4	0.05
#26	0.6	0.4	0
#27	0.2	0.425	0.375
#28	0	0.5	0.5
#29	0.1	0.5	0.4
#30	0.15	0.5	0.35
#31	0.16	0.5	0.34
#32	0.17	0.5	0.33
#33	0.18	0.5	0.32
#34	0.19	0.5	0.31
#35	0.2	0.5	0.3
#36	0.21	0.5	0.29
#37	0.22	0.5	0.28
#38	0.25	0.5	0.25
#39	0.28	0.5	0.22
#40	0.3	0.5	0.2
#41	0.25	0.5714	0.1786
#42	0.26	0.5714	0.1686
#43	0.27	0.5714	0.1586
#44	0.28	0.5714	0.1486
#45	0.29	0.5714	0.1386
#46	0.295	0.5714	0.1336
#47	0.3	0.5714	0.1286
#48	0.3572	0.5714	0.0714
#49	0.4143	0.5714	0.0143
#50	0.4286	0.5714	0
#51	0.02	0.6	0.38
#52	0.2	0.65	0.15

2.2. X-ray diffraction

X-ray powder diffraction (XRD) analysis of the samples has been carried out at room temperature using a Rigaku SmartLab diffractometer with Cu K α radiation (40 kV, 200 mA) and a graphite monochromator at the China University of Geosciences Beijing. A step scan mode was employed with a step width of $2\theta=0.02^\circ$ and a sampling time of 1 s in the range of $15\leq 2\theta\leq 70^\circ$. The

compositions in the CaO-CoO_x-ErO_y system were analyzed by using the Powder Diffraction File (PDF) [35].

2.3. Rietveld refinements

The structural changes of the samples in the solid solution region (Ca_{3-x}Er_x)Co₂O_{6-z} were analyzed by Rietveld refinements [36,37]. X-ray powder diffraction (XRD) analysis of these perovskite crystals has been carried out at room temperature using a Rigaku SmartLab diffractometer with Cu K_α radiation (40 kV, 200 mA) and a graphite monochromator as mentioned above. A step scan mode was employed with a step width of 2θ=0.02° and a sampling time of 1 s in the range of 15≤2θ≤120°.

3. Results

Figure 1 shows the phase diagram of the CaO-CoO_x-ErO_y system that was determined at 885 °C. The phase relations between the solid solution and other phases are represented by tie-lines. The phase diagram of CaO-CoO_x-ErO_y ternary system at 885°C has 5 two-phase zones, 4 three-phase zones, 8 two-phase contact lines and 3 solid solution zones. The phase diagram of CaO-CoO_x-ErO_y ternary system at 885°C shows three solid solution distinctions: (Ca_{3-x}Er_x)Co₄O_{9-z} (0≤x≤0.9), (Ca_{3-x}Er_x)Co₂O_{6-z} (0≤x≤1.25) and (Er_{1-x}Ca_x)CoO_{3-z} (0≤x≤0.33). The crystal chemistry and crystallography of the phases in binary and ternary oxide systems are discussed below.

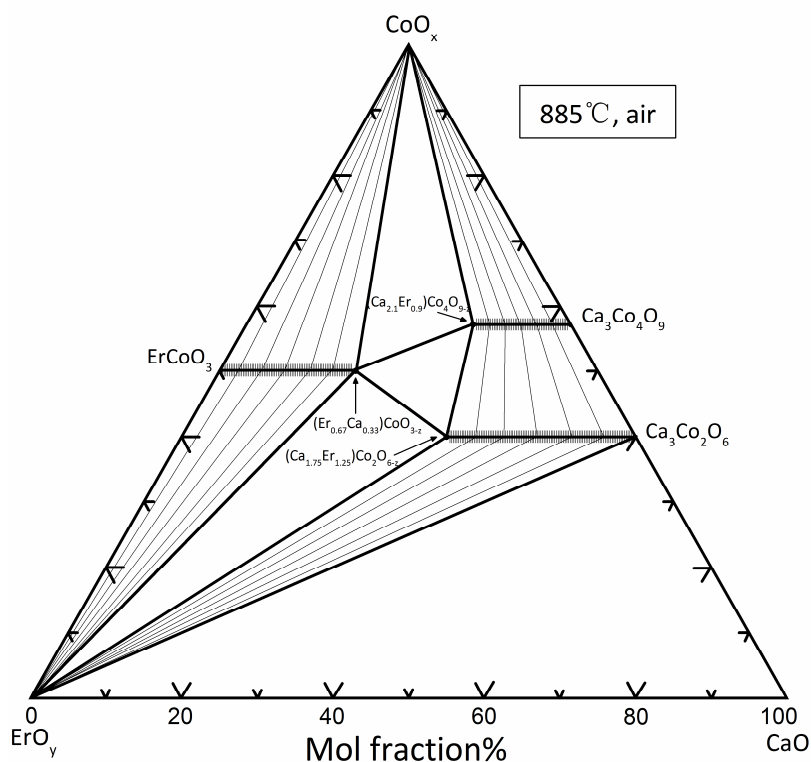


Figure 1. Phase diagram of the CaO-CoO_x-ErO_y system at 885°C in air, showing the limits of various solid solutions, and the tie-line relationships of various phases.

3.1. Binary oxide systems

3.1.1. CaO-CoO_x

Binary CaO-CoO_x oxide systems have been studied extensively. In this system, two single-phase structures have been identified: Ca₃Co₂O₆ (Co:Ca=40:60) and Ca₃Co₄O₉ (Co:Ca=57.14:42.86) [12,24]. Both Ca₃Co₂O₆ and Ca₃Co₄O₉ have perovskite-derived structures. It is also confirmed that there are only two single-phase Ca₃Co₂O₆ and Ca₃Co₄O₉ in the binary system under the current high temperature solid-phase synthesis conditions.

$\text{Ca}_3\text{Co}_4\text{O}_9$ is a mismatched layered oxide with two monocline subsystems, with the same a , c , but different b values. There are two different Co-O layers stacked regularly along the direction of the c -axis, one of which is CoO_2 layer, CoO_2 layer has a CdI_2 -type structure, CoO_2 layer can be regarded as Co ion in the center, there are six O ions around the central Co ion, the center of the octahedron is Co ion, the apex of the octahedron is O ion. Adjacent octahedrons are connected in the form of common edges; The other layer is Ca_2CoO_3 , formed from Ca-Co-O, which has a halite structure. CoO_2 layer can provide charge carriers (holes) needed for conducting electricity, and Co ions in CoO_2 layer include Co^{3+} and Co^{4+} , located at the adjacent O^{2-} midpoint. There is strong interaction between adjacent positive ions. The change of valence of Co ion makes it easy to shift from the center of the octahedron, resulting in the difference in the length of Co-O bond. The bonding mode between ions in Ca_2CoO_3 layer is ionic bond, and there is no change of valence, so Ca_2CoO_3 layer does not conduct electricity, and the presence of Ca_2CoO_3 reduces the thermal conductivity of the material. Higher conductivity σ and lower thermal conductivity κ will make the material have higher thermoelectric value. Therefore, the phase exhibits strong anisotropic thermoelectric properties in the ab plane [33].

$\text{Ca}_3\text{Co}_2\text{O}_6$ ($R\bar{3}c$, $a=9.0793$ (7) Å, $c=10.381$ (1) Å) is a member of the $n=1$ of the perovskite-derived series $\text{A}_{n+2}\text{B}_n\text{B}'\text{O}_{3n+3}$, where the A positions are alkaline earth metals, such as Ca, Sr and Ba, and the B and B' positions are usually transition metal elements. In $\text{Ca}_3\text{Co}_2\text{O}_6$, the A site is the Ca ion, the B site is the Co ion in the center of the octahedron, and the B' site is the Co ion in the center of the distorted trigonal prism [34]. **Figure 2** shows the structure of $\text{Ca}_3\text{Co}_2\text{O}_6$. $\text{Ca}_3\text{Co}_2\text{O}_6$ has a one-dimensional Co-O chain structure. This unique structure makes $\text{Ca}_3\text{Co}_2\text{O}_6$ obtain excellent thermoelectric properties, magnetic properties and chemical stability. $\text{Ca}_3\text{Co}_2\text{O}_6$ is suitable for use in moderate and relatively harsh environmental conditions. The Seebeck coefficient of $\text{Ca}_3\text{Co}_2\text{O}_6$ increases with the increase of temperature, the conductivity of $\text{Ca}_3\text{Co}_2\text{O}_6$ is semiconductor, and the thermal conductivity of $\text{Ca}_3\text{Co}_2\text{O}_6$ is relatively low. Therefore, $\text{Ca}_3\text{Co}_2\text{O}_6$ is a kind of high efficient thermoelectric material with potential to be developed.

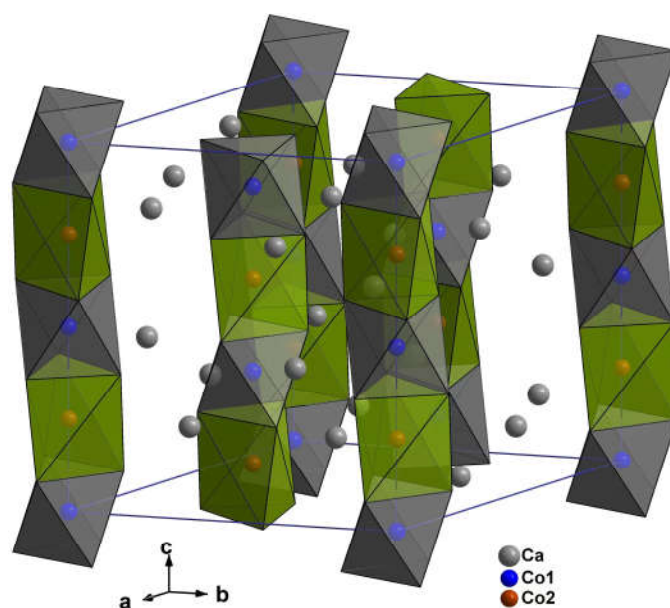


Figure 2. Crystal structure of $\text{Ca}_3\text{Co}_2\text{O}_6$ showing the linear chain characteristics of Co-O octahedron and Co-O prism, each $\text{Co}_2\text{O}_6^{6-}$ chain is surrounded by six other chains. These $\text{Co}_2\text{O}_6^{6-}$ chains are separated by octa-coordinated Ca^{2+} ions.

3.1.2. CaO-ErO_y

Five samples were prepared in the CaO-ErO_y binary system to determine the phases form. There is no single phase in the CaO-ErO_y binary system, indicating that there is no solid solution near CaO and Er₂O₃, that is, there is no solid solution zone in the CaO-ErO_y binary system.

3.1.3. CoO_x-ErO_y

At 885 °C, the only phase found in the ErO_x-CoO_y system is the ErCoO₃ phase, which has the Pnma space group perovskite structure. In the CoO_x-LaO_y binary system of the CaO-CoO_x-LaO_y [28] phase diagram, La₂CoO₄ phase was determined, but in this study the Er₂CoO₄ phase could not be prepared under the present conditions.

3.2. Ternary oxide systems

Three series of ternary solid solutions were found at 885 °C, which were (Ca_{3-x}Er_x)Co₄O_{9-z} (0 ≤ x ≤ 0.9), (Ca_{3-x}Er_x)Co₂O_{6-z} (0 ≤ x ≤ 1.25) and (Er_{1-x}Ca_x)CoO_{3-z} (0 ≤ x ≤ 0.33). We found the solid solution region (Ca_{3-x}Er_x)Co₄O_{9-z} near Ca₃Co₄O₉ and the solid solution region (Er_{1-x}Ca_x)CoO_{3-z} near ErCoO₃ are close to the previously reported range in the other CaO-RO_x-CoO_y systems. The solution region (Ca_{3-x}Er_x)Co₂O_{6-z} was found near Ca₃Co₂O₆, while the solid solution of other lanthanides did not occur at (Ca,R)₃Co₂O₆. Different from the CaO-CoO_x-RO_y (R=Eu, Gd, Sm) systems as reported previously, the solid solution region of (Er_{2-x}Ca_x)CoO_{4-z} did not exist in the CaO-CoO_x-ErO_y system at 885 °C. The phase relationship of each solid solution zone will be discussed in detail below.

3.2.1. (Ca_{3-x}Er_x)Co₄O_{9-z}

Ca₃Co₄O₉ was found in CaO-CoO_x boundary binary system, which is a mismatched layered oxide. Ca₃Co₄O₉ has the perovskite-derived structure. Ca₃Co₄O₉ is a good thermoelectric material and has a splendid prospect in the field of energy. The solid solution region (Ca_{3-x}Er_x)Co₄O_{9-z} forms with the addition of doping element Er. Ten samples were selected near Ca₃Co₄O₉ to explore the boundary of the solid solution region (Ca_{3-x}Er_x)Co₄O_{9-z}, with the dopant of Er, the content of x in the solid solution (Ca_{3-x}Er_x)Co₄O_{9-z} was found to be from 0 to 0.9.

3.2.2. (Ca_{3-x}Er_x)Co₂O_{6-z}

Ca₃Co₂O₆ was found in the CaO-CoO_x boundary binary system, the corresponding Co content is 40 at.%. Ca₃Co₂O₆ has the perovskite-derived structure. Ca₃Co₂O₆ is a good thermoelectric material and has a splendid prospect in the field of energy. The solid solution region (Ca_{3-x}Er_x)Co₂O_{6-z} forms with the addition of doping element Er, the solid solution formation appears for (Ca_{3-x}Er_x)Co₂O_{6-z}, with the value of x ranging from 0 to 1.25. The XRD patterns of the sample with 40 at.% Co content and results of MDI Jade show the peak shift systematically with the Er content. As shown in **Figure 3**, the peaks shift with the amount of Er content in (Ca_{3-x}Er_x)Co₂O_{6-z}, but the directions of peak shiftings are not the same. In **Figure 3**, it is seen that the crystal plane (113) moves towards a low angle direction, while the crystal plane (300) moves toward a high angle direction, probably due to anisotropic expansion of the unit cell.

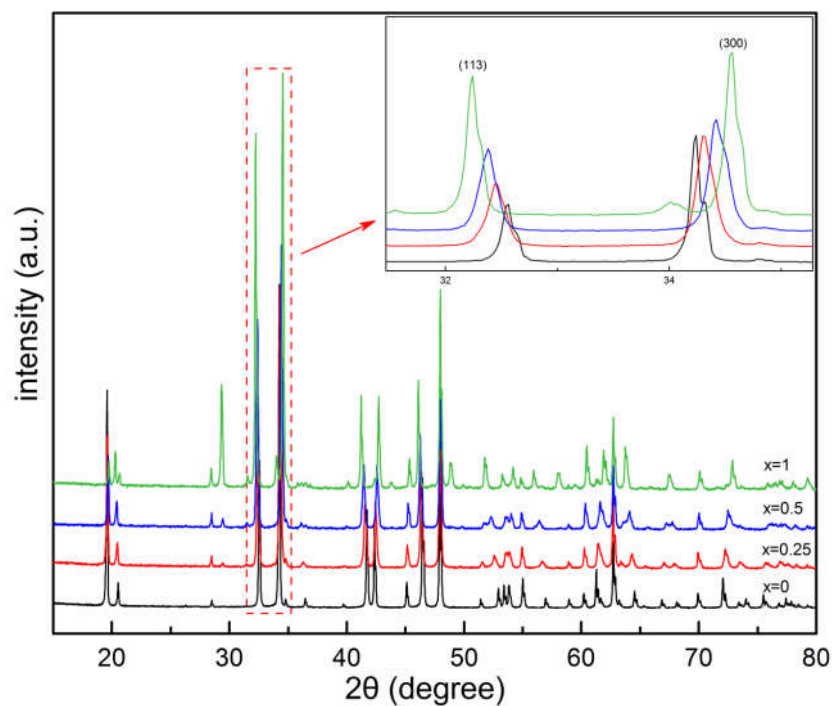


Figure 3. XRD patterns of $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_2\text{O}_{6-z}$ ($x=0, 0.25, 0.5, 1$).

At 885°C, solid solution was found near $\text{Ca}_3\text{Co}_2\text{O}_6$. The samples $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_2\text{O}_{6-z}$ ($x=0, 0.25, 0.5, 1$) were slowly scanned with XRD followed by Rietveld finishing. The diffraction patterns were analyzed by the Rietveld refinement technique using the Fullprof program. **Figure 4** shows the refinement results of $(\text{Ca}_2\text{Er}_1)\text{Co}_2\text{O}_{6-z}$ and $\text{Ca}_3\text{Co}_2\text{O}_6$, respectively, with χ^2 of 2.47 and 2.22.

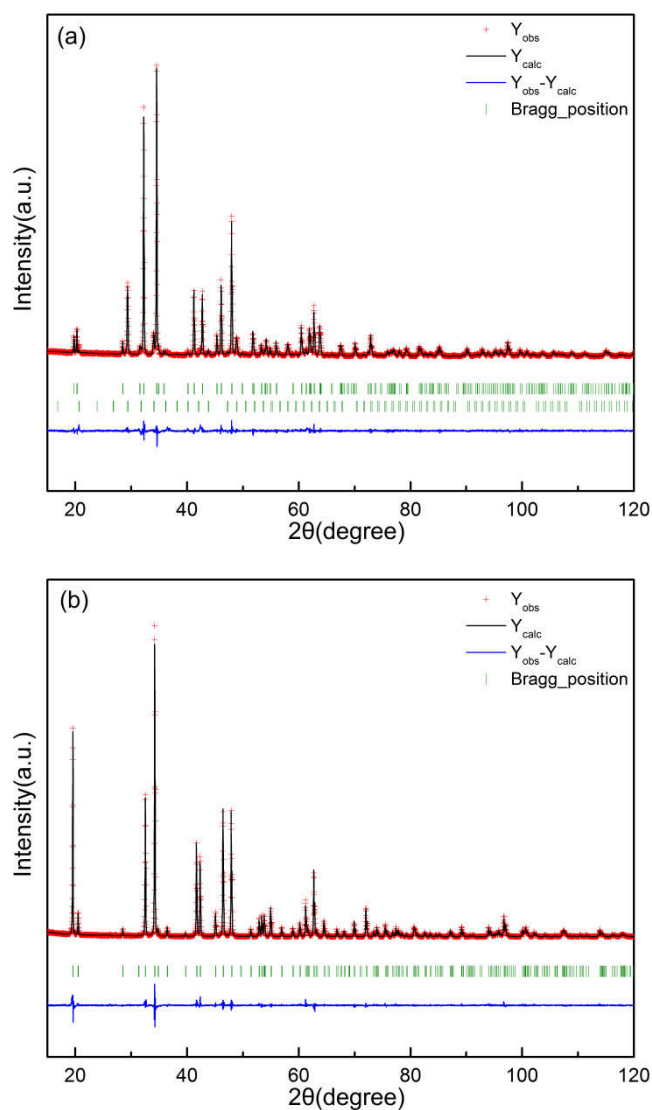


Figure 4. Rietveld analysis results for (a) $(\text{Ca}_2\text{Er}_1)\text{Co}_2\text{O}_{6-z}$ and (b) $\text{Ca}_3\text{Co}_2\text{O}_6$. Y_{obs} represents the experimental spectrum, Y_{calc} represents the calculated spectrum, the short vertical line below the diffraction spectrum represents the Bragg diffraction peak position of the corresponding phase, and $Y_{\text{obs}} - Y_{\text{calc}}$ represents the difference between the experimental spectrum and the calculated spectrum.

Table 2 and **Table 3** provide the refinement parameters and the atomic coordinates of $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_2\text{O}_{6-z}$ ($x=0, 0.25, 0.5, 1$), respectively. **Figure 5** shows the changes of cell parameters of $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_2\text{O}_{6-z}$ ($x=0, 0.25, 0.5, 1$). With the increase of x , a and b become smaller and c becomes larger, confirming the previous conjecture.

Table 2. Refinement parameters of $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_2\text{O}_{6-z}$ ($x=0, 0.25, 0.5, 1$). The bracketed values represent standard deviations.

x	a&b (Å)	c (Å)	Rwp	χ^2
0	9.07628(8)	10.38005(12)	11.0	2.22
0.25	9.05344(21)	10.44059(28)	10.8	3.53
0.5	9.02907(22)	10.50383(28)	9.57	3.43
1	8.98770(12)	10.58704(17)	6.79	2.47

Table 3. Atomic coordinates and displacement parameters for $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_2\text{O}_{6-z}$. The bracketed values represent standard deviation. The numerical error of B_{iso} obtained by XRD is relatively large, so the neutron diffraction B_{iso} [38] is used in the finishing.

	x	y	z	B_{iso} [38]
$\text{Ca}_3\text{Co}_2\text{O}_6$				
Ca	0.36986(2)	0	0.25	0.39
Co1	0	0	0	0.37
Co2	0	0	0.25	0.48
O	0.17804(6)	0.02561(8)	0.11402(5)	0.53
$(\text{Ca}_{2.75}\text{Er}_{0.25})\text{Co}_2\text{O}_{6-z}$				
Ca/Er	0.36834(3)	0	0.25	0.39
Co1	0	0	0	0.37
Co2	0	0	0.25	0.48
O	0.17787(11)	0.02463(13)	0.11268(7)	0.53
$(\text{Ca}_{2.5}\text{Er}_{0.5})\text{Co}_2\text{O}_{6-z}$				
Ca/Er	0.36773(3)	0	0.25	0.39
Co1	0	0	0	0.37
Co2	0	0	0.25	0.48
O	0.17959(12)	0.02464(14)	0.11238(8)	0.53
$(\text{Ca}_2\text{Er}_1)\text{Co}_2\text{O}_{6-z}$				
Ca/Er	0.36688(2)	0	0.25	0.39
Co1	0	0	0	0.37
Co2	0	0	0.25	0.48
O	0.18265(12)	0.02475(13)	0.11010(7)	0.53

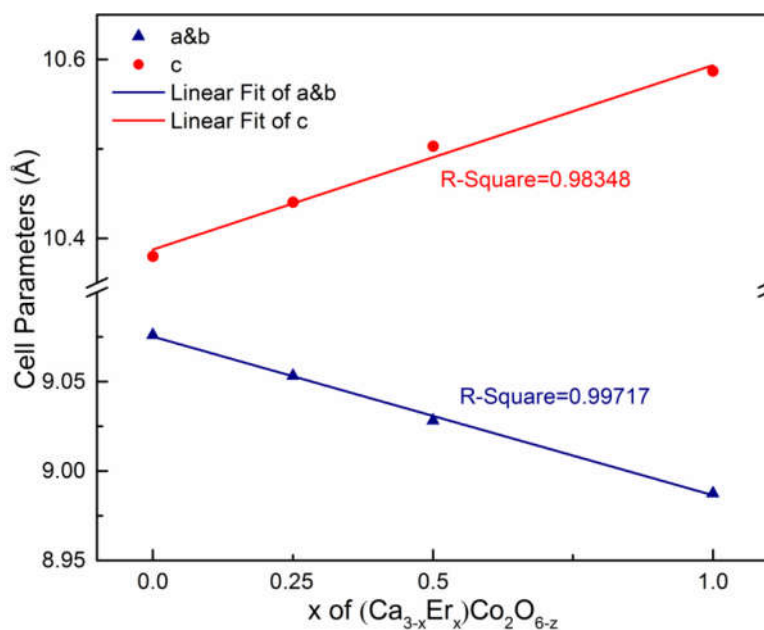


Figure 5. Cell parameters of $(Ca_{3-x}Er_x)Co_2O_{6-z}$ ($x=0, 0.25, 0.5, 1$).

The Co-O chain in the $Ca_3Co_2O_6$ crystal structure is part of a polyhedron chain parallel to the c axis. **Figure 6** gives the projection of the regular octahedrons and distorted trigonal prisms of the Co-O chain along the b axis. One can construct various planes using neighboring O ions in the Co-O chain; among these planes, the one perpendicular to the c axis was found to move most significantly with the doping of Er. **Table 4** gives the structural parameters of $(Ca_{3-x}Er_x)Co_2O_{6-z}$. With the increase of Er content, the $Ca_3Co_2O_6$ structure is lengthened in the c axis direction, mainly due to the lengthening of h_2 (shown in **Figure 6**), or the distorted trigonal prism in the Co-O chain is elongated.

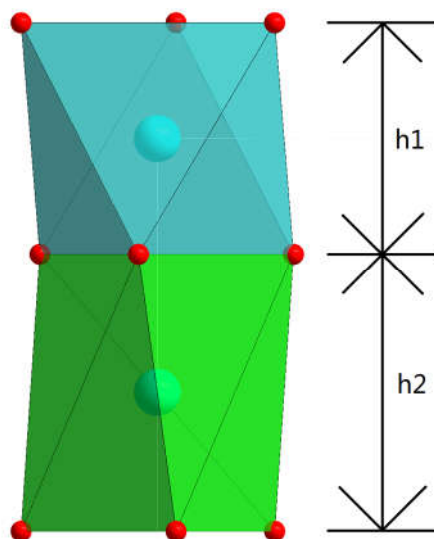


Figure 6. Projection of the regular and distorted octahedron in the Co-O chain along the b axis, where h_1 is the height of the regular octahedron along the c axis and h_2 is the height of the distorted trigonal prism along the c axis.

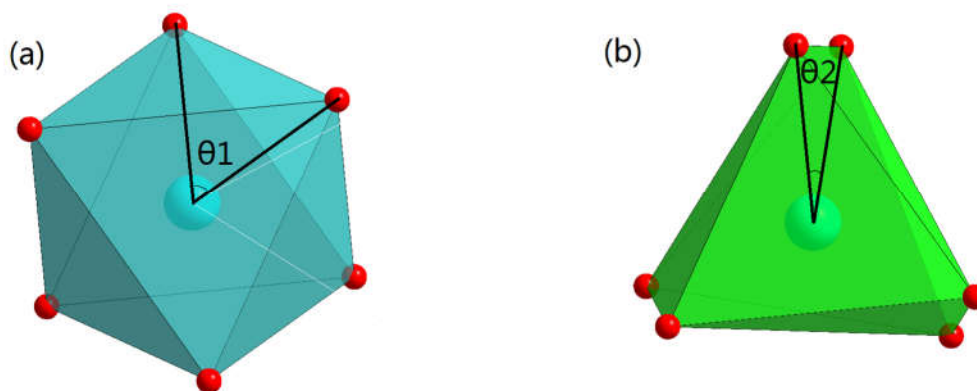


Figure 7. Projection of the regular octahedron (a) and distorted trigonal prism (b) in the Co-O chain along the *c*-axis, θ_1 and θ_2 in the figure represent the angles in the projection.

Table 4. Structural parameters of $(Ca_{3-x}Er_x)Co_2O_{6-z}$. In this table, h_1 and h_2 represent the distance between the planes of oxygen ion perpendicular to the *c*-axis (**Figure 6**). Columns O_{CCa} and O_{CEr} represent the occupancy of Ca and Er ions, which are in the position of 18e. θ_1 and θ_2 are the angles in the projection of **Figure 7**, the bracketed values represent standard deviation.

<i>x</i>	$h_1(\text{Å})$	$h_2(\text{Å})$	$h_1+h_2(\text{Å})$	O_{CCa}	O_{CEr}	$\theta_1(\text{degree})$	$\theta_2(\text{degree})$
0	2.367	2.823	5.19	1	0	60.000(44)	15.290(39)
0.25	2.3529	2.8674	5.2203	0.916	0.076	60.000(53)	14.683(52)
0.5	2.3608	2.8911	5.2519	0.834	0.16	60.000(51)	14.540(52)
1	2.3312	2.9623	5.2935	0.666	0.298	60.000(45)	14.349(38)

Ca ion is replaced by Er ion in $(Ca_{3-x}Er_x)Co_2O_{6-z}$ crystal structure. Since Er ion is positive trivalent and Ca ion is positive bivalent, Er^{3+} entering $(Ca_{3-x}Er_x)Co_2O_{6-z}$ structure would be less than Ca^{2+} , and causing site vacancy. In **Table 4**, O_{CCa} and O_{CEr} represent the occupancy of Ca and Er sites, which are in the position of 18e. Moreover, the radius of Er^{3+} is smaller than that of Ca^{2+} [39], so the entry of Er ion is expected to lead to the shortening of the crystal structure of $(Ca_{3-x}Er_x)Co_2O_{6-z}$ in the direction of *a* & *b*.

In **Figure 3**, the crystal plane (300) can be used to represent the *a* & *b* direction, and the crystal plane (113) can approximately represent the *c* direction. With the increase of *x*, the crystal plane (300) moves towards the higher angle direction, which means the crystal structure becomes shorter in the *a* & *b* direction, and the crystal plane (113) shifts towards the lower angle direction, which means the crystal structure becomes longer in the *c* direction.

Figure 7 shows the *c* axis projection of the regular octahedron and distorted trigonal prism in the Co-O chain, and **Table 4** shows the angle of θ in **Figure 7**. The angle θ_1 of the regular octahedron is 60° , while the angle θ_2 of the distorted trigonal prism is much less than 60° . With the increase of *x*, angle θ_2 tends to become even smaller. This is the reason why the distorted trigonal prism becomes elongated in the direction of the *c* axis.

In conclusion, with the increase of *x* value in $(Ca_{3-x}Er_x)Co_2O_{6-z}$, the diffraction peak migration direction of $Ca_3Co_2O_6$ in XRD pattern is inconsistent. The structure analysis of $(Ca_{3-x}Er_x)Co_2O_{6-z}$ series samples shows that with the increase of *x* value, Er ions in the structure of $(Ca_{3-x}Er_x)Co_2O_{6-z}$ increase, and the radius of Er ion is smaller than that of Ca ion, because Er ion is +3 valence and Ca ion is +2 valence, The valence equilibrium makes the number of incoming Er ions less than the number of replaced Ca ions, so the structure of $(Ca_{3-x}Er_x)Co_2O_{6-z}$ is shortened in the *a* & *b* directions; As the *x* value

increases, the Co-O chain becomes longer, so the structure of $(\text{Ca}_{3-x}\text{Er}_x)\text{Co}_2\text{O}_{6-z}$ becomes longer in the c direction.

3.2.3. $(\text{Er}_{1-x}\text{Ca}_x)\text{CoO}_{3-z}$

ErCoO_3 was found in the $\text{CoO}_x\text{-ErO}_y$ boundary binary system. ErCoO_3 has a perovskite structure, it is a perovskite-type oxide, and it has thermoelectric properties. The solid solution region $(\text{Er}_{1-x}\text{Ca}_x)\text{CoO}_{3-z}$ forms with the addition of doping element Ca. thirteen samples were selected near ErCoO_3 to explore the boundary of the solid solution region $(\text{Er}_{1-x}\text{Ca}_x)\text{CoO}_{3-z}$, and the range of x in solution region $(\text{Er}_{1-x}\text{Ca}_x)\text{CoO}_{3-z}$ is from 0 to 0.33.

4. Discussion

It appears that the ionic size of the alkaline-earth and lanthanide ions governs the trend of phase formation, extent of solid solution formation of $(\text{R}_{1-x}\text{Ca}_x)\text{CoO}_{3-z}$, $(\text{R}_{1-x}\text{Ca}_x)_2\text{O}_{3-z}$, $(\text{Ca}_{3-x}\text{R}_x)\text{Co}_4\text{O}_{9-z}$ and $(\text{Ca}_{3-x}\text{R}_x)\text{Co}_2\text{O}_6$, as well as the tie-line relationships in the $\text{CaO-CoO}_x\text{-RO}_y$ systems. Because of different phase formation and different range of solid solutions in the La, Dy, and the Er systems, the tie-line relationships are substantially different, leading to different appearance of the diagrams.

Since the doped element R in $\text{CaO-CoO}_x\text{-RO}_y$ series are lanthanide elements, these diagrams are expected to be related. Therefore, the next step of our present study is to compare the ternary phase diagrams of $\text{R}=\text{La}$ [28], Dy [33] and Er at 885°C . **Figure 8** and **Figure 9** show the $\text{CaO-CoO}_x\text{-RO}_y$ ternary phase diagrams of $\text{R}=\text{La}$ and Dy.

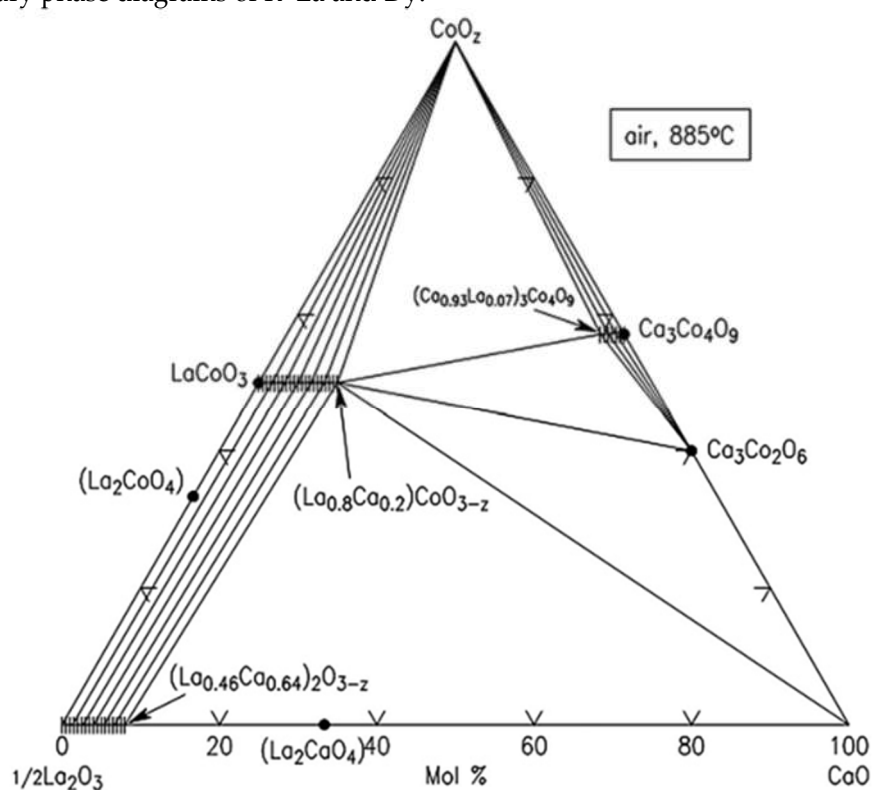


Figure 8. Phase diagram of the $\text{CaO-CoO}_x\text{-LaO}_y$ system at 885°C in air [28].

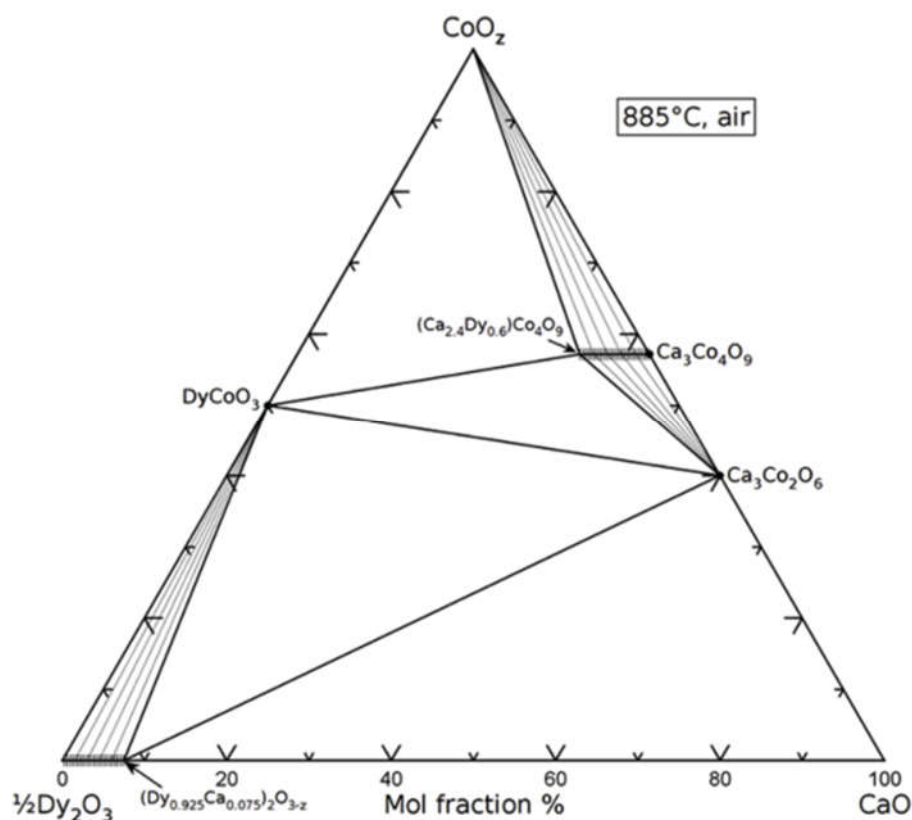


Figure 9. Phase diagram of the CaO-CoO_x-DyO_y system at 885 °C in air [33].

La is the first element in the lanthanide series, and CaO-CoO_x-LaO_y [28] is the first phase diagram of CaO-CoO_x-RO_y (R is lanthanide) series at 885 °C, therefore CaO-CoO_x-LaO_y has provided a guide for the entire series of phase diagrams. The phase diagrams of CaO-CoO_x-LaO_y and CaO-CoO_x-ErO_y were compared. The solid solution regions of (Ca_{3-x}R_x)Co₄O_{9-z} and (R_{1-x}Ca_x)Co₂O_{6-z} existed in both systems. Although both systems contain perovskite RCoO₃ phase, LaCoO₃ and ErCoO₃ have different structures. LaCoO₃ phase is rhombohedral and with a space group of R-3c [28], while ErCoO₃ phase is orthorhombic with space group Pnma. The difference in size of lanthanide ions ($r_{La^{3+}} > r_{Ca^{2+}} > r_{Er^{3+}}$) [39] results in the different structures of LaCoO₃ and ErCoO₃. In the CaO-CoO_x-LaO_y system in air at 885 °C, there is no solid solution phenomenon near Ca₃Co₂O₆, which is different from the CaO-CoO_x-ErO_y system in air at 885 °C. And in the CaO-CoO_x-LaO_y system in air at 885 °C, there is a solid solution phenomenon near La₂O₃, which is different from the CaO-CoO_x-ErO_y system in air at 885 °C.

In the phase diagram of the CaO-CoO_x-DyO_y and CaO-CoO_x-ErO_y systems, only one solid solution region is the same, namely (Ca_{3-x}R_x)Co₄O_{9-z}, but the range of the two solid solution regions is different when R=Dy, $0 \leq x \leq 0.6$, and R=Er, $0 \leq x \leq 0.9$. (Ca_{3-x}Er_x)Co₂O_{6-z} is a new solid solution region, and other CaO-CoO_x-RO_y (R is lanthanide element) phase diagrams do not show solid solution phenomenon at Ca₃Co₂O₆ at 885 °C. Because of the different phase formation of these three systems, the tie-line relationships are also very different. In the La system, there are four three-phase regions and four two-phase connecting tie-line bundles [28]. In the Dy system, there are four three-phase regions and three two-phase connecting the tie-line bundles [33]. In the Er system, however, due to the addition of the (Ca_{3-x}Er_x)Co₂O_{6-z} phase, there are four three-phase regions and five solid solution tie-line regions.

5. Conclusions

The phase diagram of CaO-CoO_x-ErO_y system at 885 °C has been drawn. This phase diagram shows the phase relationships between the phases in the CaO-CoO_x-ErO_y ternary system, which is crucial for knowing and understanding the properties and properties of the materials in the system. There are four three phase zones and five solid solution contact zones in the system. Three series of

solid solutions have been found in the CaO-CoO_x-ErO_y system at 885 °C, which are respectively (Er_{1-x}Ca_x)CoO_{3-z} (0 ≤ x ≤ 0.33) with simple perovskite structure, and (Ca_{3-x}Er_x)Co₄O_{9-z} (0 ≤ x ≤ 0.9) and (Ca_{3-x}Er_x)Co₂O_{6-z} (0 ≤ x ≤ 1.25) with perovskite-derived structures. The solid solution phenomenon will lead to changes in the structure of materials, which will lead to changes in the properties and properties of materials. The solid solution of perovskite and its derived structure in the system will affect the properties of materials. Studying the structure of materials will help to understand the changes in material properties, and help to explore the acquisition of materials with more efficient energy conversion and storage. The solid solution is formed near Ca₃Co₂O₆. With the increase of x value in (Ca_{3-x}Er_x)Co₂O_{6-z}, the diffraction peak migration direction of Ca₃Co₂O₆ in XRD pattern is inconsistent. The structural analysis of (Ca_{3-x}Er_x)Co₂O_{6-z} series samples concludes that this difference is the anisotropic expansion of the unit cell.

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