
Article

Ab-initio Molecular Dynamics Simulation of the Changes in the Optical Properties of 2D MoS₂ When Doped with Pt at 300 K

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Abstract: Using first-principles molecular dynamics (FPMD), we performed numerical simulations at 300 K to explore the interaction of a 2D MoS₂ surface and a platinum atom, calculating the optical properties of the resulting material. The pristine MoS₂ is a semiconductor with a gap of around 1.80 eV. The Pt atom is chemisorbed by the surface with an adsorption energy of -1.72 eV. With the adsorption of the Pt atom, the material remains a semiconductor, and its energy band gap reduces to 1.04 eV. But changes in the material's energy band structure imply substantial changes in its optical properties. The energy band structure of the 2D MoS₂ with a sulfur vacancy V_s shows that the material becomes a conductor, and there are significant changes in its optical properties. We also found that the Pt atom chemisorbs in a sulfur vacancy of the material, with an adsorption energy of -4.12 eV. After the adsorption of Pt atoms in the sulfur vacancy, the material becomes a semiconductor with a band gap of 1.06 eV, and the changes in the optical absorption and reflectivity are significant.

Keywords: ab-initio; DFT calculations; 2D materials; MoS₂; optical properties; platinum; FPMD

1. Introduction

Bidimensional materials show different interesting physical properties, making them suitable for many potential applications, including energy storage [1–3], biomedical research [4–6], field-effect transistors (FETs) [7–10], as well as sensors and biosensing [11,12]. One of such materials is Molybdenum disulfide, MoS₂, a layered dichalcogenide with a hexagonal structure similar to graphene. Like graphene, the bonds between layers are weaker, allowing for a relatively easy dislocation [13–16]. Monolayer MoS₂ is also a direct-gap semiconductor with a band gap of 1.8 eV [17] with potential applications that have been explored in fields as diverse as ultrafast photonics, treatment of antibiotic-polluted water, drug-delivery purposes, water splitting, and FETs [18–24].

Studying the band structure and optical properties of such 2D materials helps explore their potential applications. The band structure of MoS₂ has been previously explored, including the effect of interlayer pressure [25]. Here, we studied the changes produced in the optical properties of MoS₂ when adsorbing Pt. We considered pristine MoS₂ and MoS₂ with a sulfur monovacancy (also labeled as V_s) on the unit cell. Vacancies on MoS₂ have been previously studied experimentally and by first-principles calculations, finding relatively low formation energies for a V_s vacancy [16,26], which in turn makes it relatively easy to find.

2. Results

Figure 1(a, b) shows the hexagonal unit cell considered. With a cell parameter of 6.3 Å, it contains 12 atoms: eight S atoms and four Mo atoms. We chose the size of the cell to ensure a sufficiently long distance between one bit and its repetition in the next cell due to the use of periodic boundary conditions. The unit cell we considered is large enough to give a sufficiently good amount of information while avoiding spurious interactions. Starting from this cell, we removed one S atom to create a vacancy. Figure 1(c) shows the PDOS for the pristine MoS₂, with a gap of 1.8 eV, in agreement with previously reported works [25]. Below the Fermi energy, notice the hybridization of orbitals p and d from molybdenum with orbitals s and p from sulfur. Above 2 eV, we can see the hybridization of the same orbitals, but the contribution of orbital p from molybdenum is negligible.

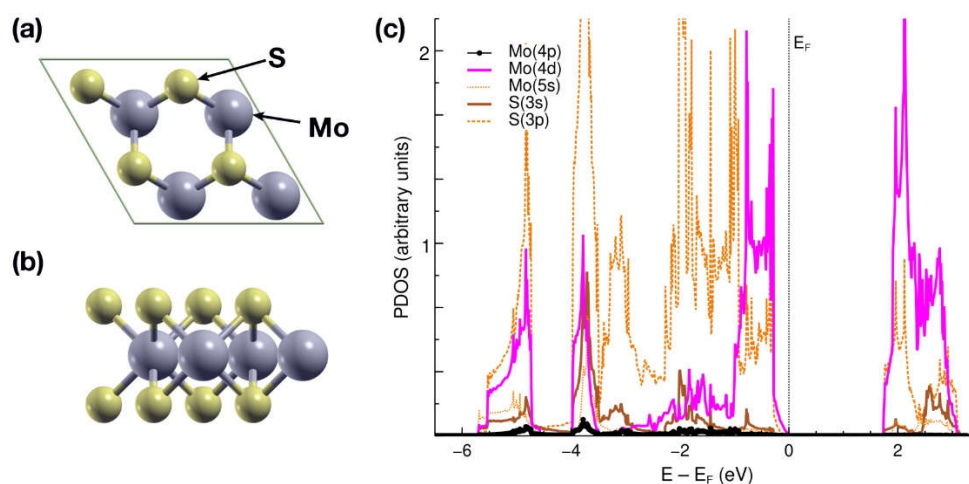


Figure 1. (a) XY-plane view of the unit cell considered for the pristine MoS₂. It contains 12 atoms: four Mo and eight S atoms. The cell parameter is 6.3 Å. (b) XZ-plane view of the unit cell. (c) The PDOS for the pristine MoS₂, showing a gap of 1.8 eV.

2.1. Pt-absorption on the pristine MoS₂ layer

We first placed the Pt atom at 3 Å directly above the MoS₂ surface. The ab-initio molecular dynamics calculation at 300 K showed that the MoS₂ surface absorbed the Pt atom, with an adsorption energy of -1.72 eV. Figure 2(a) shows the initial and final positions of the Pt atom during the adsorption process on the MoS₂ layer, along with a plot of the energy evolution of the system during the calculation. Figure 2(b) offers the PDOS for the Pt atom adsorbed on the pristine MoS₂. The effect of the absorbed Pt atom is a reduction of the band gap, which was observed to be of 1.04 eV in this case. Between 0 and -1.5 eV, there is a hybridization of orbitals s and d from platinum with orbitals s from sulfur and d from molybdenum. Below -6 eV, we have hybridized orbitals s, p, and d from molybdenum with orbitals s and d from platinum. Above 2 eV, we can see the hybridization of the same orbitals, but the contribution of orbital p from molybdenum is again negligible.

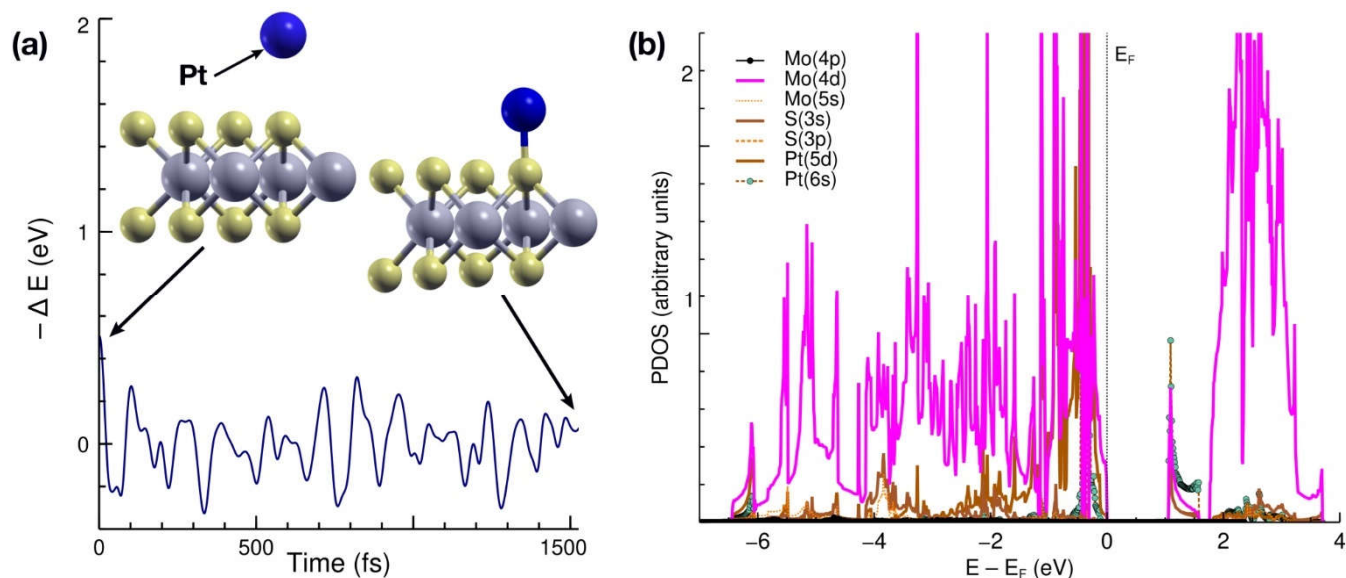


Figure 2. (a) Time evolution graph including the initial and final positions of the Pt atom interacting with the pristine MoS₂ surface. The MD calculation consisted of 1526 iterations and the system achieves stability at about 200 fs, much faster than the next case; (b) The PDOS of the system pristine MoS₂-Pt. The band gap is reduced to 1.04 eV in this case.

2.2. Pt-absorption on the MoS₂ + V_s vacancy layer

The next case considered was that of a sulfur V_s vacancy in the MoS₂ surface and its interaction with Pt. We performed FPMD calculations at 300 K for an initial configuration with the Pt atom at 3 Å directly above the S-vacancy of the system, like in the previous case (see Figure 3(a)). We obtained that the Pt atom is chemisorbed in the V_s vacancy, with an absorption energy of -4.12 eV. The vacancy we are considering in our unit cell is equivalent to a vacancy density of 12.5% on the surface. Figure 3(b) shows the PDOS for the Pt atom adsorbed on the MoS₂ surface. The band gap for this case was observed to be 1.06 eV. Between 0 eV and -4 eV, we can see the hybridization of the orbitals s and d from platinum with orbitals s and p from sulfur and p and d from molybdenum. Furthermore, between -4 eV and -6 eV, we have the hybridization of orbitals s, p, d from molybdenum with orbitals s, d from platinum and orbitals s, p from sulfur.

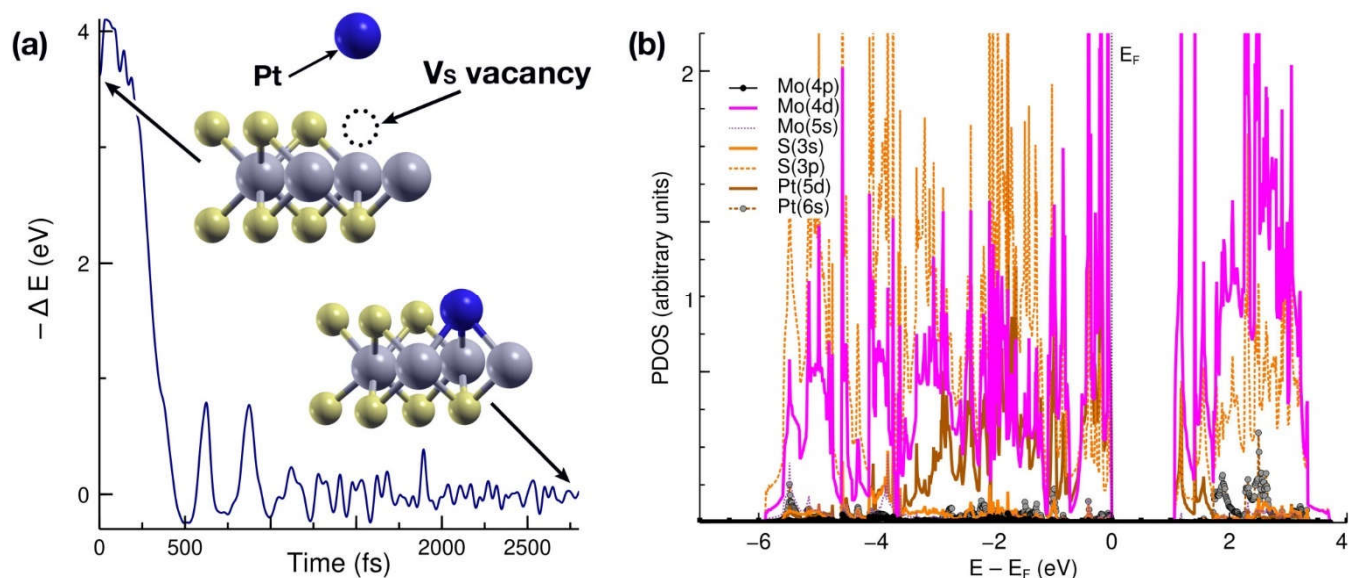


Figure 3. (a) Initial and final configurations during adsorption of a Pt atom on the MoS₂ system with a V_s vacancy. The time evolution graph shows that stability appears after about 700 fs. The MD calculation at 300 K consisted of 2800 iterations and shows that the Pt is chemisorbed by the surface, occupying the place of the vacancy; (B): The PDOS of the final system, showing a reduction similar to that of the previous case (the band gap is now 1.06 eV) when compared with the pristine MoS₂.

2.3. Energy band structures

In Figure 4, we can see the energy band structure calculations for the pristine MoS₂, the same system with an adsorbed Pt atom, the surface with a V_s vacancy, and the latter with an adsorbed Pt atom. The Fermi energy is normalized at zero.

The proposed manipulation of the MoS₂ surface causes an overall reduction in the band gap related to the pristine surface. There are exciting features. Notice that the pristine surface is a semiconductor with a band gap of 1.8 eV, as expected. The adsorption of a Pt atom does not change that property, but it reduces the band gap to 1.04 eV. However, the MoS₂ with a sulfur vacancy becomes a conductor. Furthermore, notice that the adsorption of a Pt atom on the latter destroys the conductor feature, and a band gap appears with a value of 1.06 eV. The changes in the band structure implied substantial changes in the optical properties of the surface.

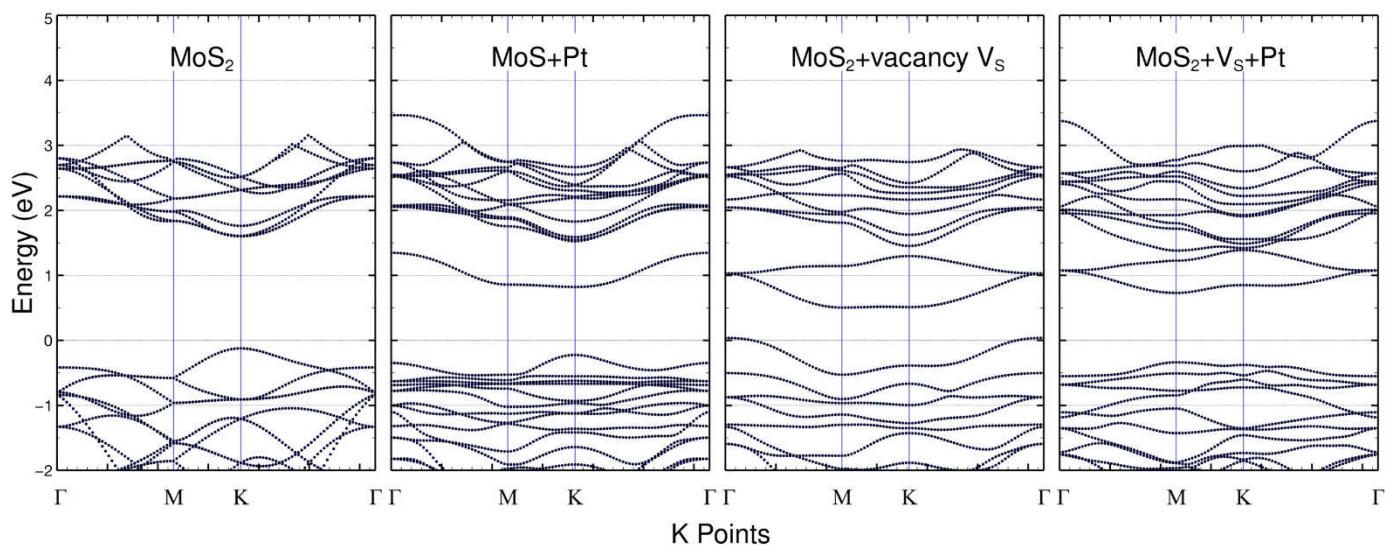


Figure 4. The energy band structure calculations for the pristine MoS₂, the same system with an adsorbed Pt atom, the surface with vacancies, and the latter with an adsorbed Pt atom. The Fermi energy is at zero.

2.4. Optical properties

For each of the cases considered, we calculated the optical absorption spectra in the infrared (IR), visible (VIS), and ultraviolet (UV) range along the Z-axis (see Figure 5). Figure 6 shows the reflectivity.

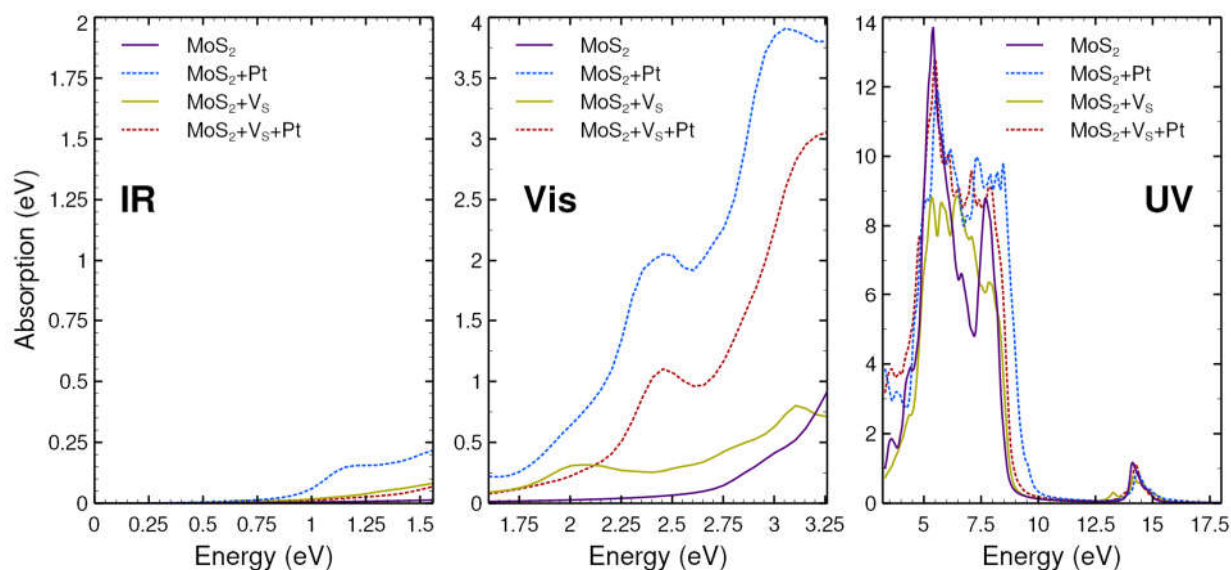


Figure 5. Absorption spectra in the infrared (left), visible (center), and UV (right) ranges, along the direction perpendicular to the surface for the systems we have investigated: pristine MoS₂, Pt adsorbed on pristine MoS₂, the same with a sulfur vacancy (MoS₂+V_S), and the latter surface with a Pt atom adsorbed on the surface (MoS₂+V_S+Pt). The vertical scale is the same for the three sections of the plot, but the range shown differs to make the features of each section more visible. In calculating this graph we have increased numerical precision to guarantee its accuracy.

Notice that the optical absorption in the infrared region has its most significant values for the surface of Pt adsorbed on pristine MoS₂ and the smallest for MoS₂ with a vacancy. We have the same behavior in the visible range, except for the interval between 2.90 eV and 3.25 eV, where the smallest values correspond to MoS₂ with a vacancy. In the ultraviolet region, Pt on the pristine MoS₂ has the most significant absorption, keeping the overall shape related to pristine MoS₂ with about the same positions for peaks and valleys. In this

case, the absorption between 6.00 eV and 7.00 eV is around 46% larger, related to the pristine surface.

In the case of reflectivity, the most substantial change related to pristine MoS₂ is between 0 eV and 5.00 eV and comes from the Pt adsorbed on non-defective MoS₂. In the same region, the smallest values correspond to MoS₂ with a vacancy. The most considerable value for reflectivity is for Pt adsorbed on defective MoS₂, which occurs around 8.6 eV.

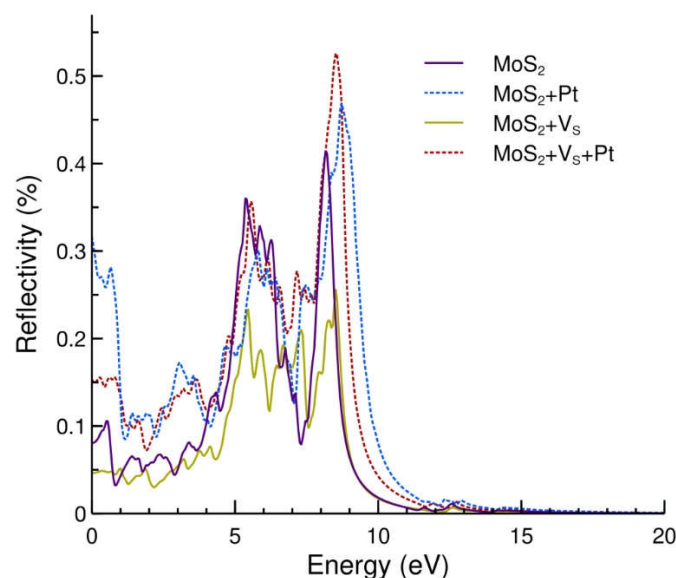


Figure 6. Reflectivity spectra for the three first cases. The substitutionally adsorbed Pt atom increases the reflectivity overall. Most of the reflectivity is observed in the visible spectra, with a negligible amount for energies beyond 20 eV.

3. Discussion

We performed FPMD simulations to investigate the Pt adsorption effect on the optical properties of 2D MoS₂. We considered pristine and defective MoS₂ at 300 K and atmospheric pressure. The proposed manipulation of the MoS₂ surface causes an overall reduction in the band gap related to the non-spoiled surface. There are exciting features. The clean surface is found to be a semiconductor with a band gap of 1.8 eV, which agrees with previous works. The adsorption of a Pt atom reduces the band gap to 1.04 eV. However, the MoS₂ with a sulfur vacancy V_s becomes a conductor, as can be seen from the band structure diagram. However, the adsorption of a Pt atom on the latter destroys the conductor feature, and a band gap appears with a value of 1.10 eV. The changes in the band structure implied substantial changes in the optical properties of the surface. Notice that the vacancy we are considering in our unit cell is equivalent to 12.5% vacancy density on the surface.

The optical absorption in the infrared region has its most significant values for the surface of Pt adsorbed on pristine MoS₂ and the smallest for MoS₂ with a vacancy. We have the same behavior in the visible range, except for the interval between 2.90 eV and 3.25 eV, where the smallest values correspond to MoS₂ with a vacancy. In the ultraviolet region, Pt on the pristine MoS₂ has the most significant absorption, keeping the overall shape related to pristine MoS₂ with about the same positions for peaks and valleys. In this case, the absorption between 6.0 eV and 7.0 eV is around 46% larger, related to the clean material.

For the reflectivity, the most substantial change related to pristine MoS₂ is between 0 eV and 5.00 eV and comes from the Pt adsorbed on non-defective MoS₂. In the same region, the smallest values correspond to MoS₂ with a vacancy. The maximum reflectivity is for Pt adsorbed on defective MoS₂, which occurs around 8.60 eV.

Understanding the optical properties of MoS₂ — and the effect that vacancies alone and in combination of the Pt decoration have on them — is essential as it could be helpful in the developing of FETs-related technologies. For future research we are exploring the potential of these combined systems in sensor technologies, particularly for pollutant molecule sensing devices. Another interesting feature reserved for future research is the variation of vacancy concentration and its effects on the properties of these materials.

4. Materials and Methods

All ab-initio calculations in this work were made using the Quantum ESPRESSO code [27,28] within the Density Functional Theory (DFT), the pseudopotential formalism, and the projector-augmented wave (PAW) method [29]. All the calculations were non-relativistic, non-spin polarized, with cut-off energy of 80 Ry (1088 eV), and threshold energy for convergence of 1.0×10^{-6} eV. This code suite considers periodic boundary conditions and plane-wave expansions.

In this work we considered Born-Oppenheimer first principles molecular dynamics (FPMD) as implemented by Quantum ESPRESSO. FPMD is the method chosen whenever bonds may be broken or formed, or in the presence of complex bonding as in transition metals [30–33], which is the case here. The FPMD calculations considered a 551 k-points mesh within the Monkhorst–Pack special k-point scheme [34]. Velocity rescaling (first method) is used to control the temperature of 300 K considered in this work. For the time step, we used the default value of 20.0 a.u. where $1 \text{ a.u.} = 4.8378 \times 10^{-17} \text{ s} = 0.048378 \text{ fs}$. This is equivalent to a time step of $0.96756 \approx 1 \text{ fs}$. The convergence parameter considered for the MD calculations was set as $1.0 \times 10^{-4} \text{ eV}$.

The valence electronic states considered are, for hydrogen: 1s, for molybdenum: 4d⁵ 5s¹, for sulfur: 3s² 3p⁴, for platinum: 5d⁹ 6s¹. The geometrical optimizations used an 882 k-points mesh and the stable coordinates obtained from the molecular dynamics. The XCrySDen software was used for visualization purposes [35].

We calculated the energy band structure to obtain the imaginary part of the dielectric tensor. We used the Kramers-Kronig relations [36] to obtain the real part, following the procedure explained in more detail in a previous work [37]. We obtained the reflectivity and the optical absorption by considering the two components of the tensor, using the following equations (where n is the refractive index and k is the extinction coefficient):

$$R_{ii}(\omega) = \frac{(n - 1)^2 + k^2}{(n + 1)^2 + k^2} \quad (1)$$

$$A_{ii}(\omega) = \frac{2\omega k(\omega)}{c} \quad (2)$$

where

$$n_{ii} = \sqrt{\frac{|\epsilon_{ii}(\omega)| + \text{Re}\epsilon_{ii}(\omega)}{2}} \quad (3)$$

$$k_{ii}(\omega) = \sqrt{\frac{|\epsilon_{ii}(\omega)| - \text{Re}\epsilon_{ii}(\omega)}{2}} \quad (4)$$

We calculated the adsorption energy for all cases by using the following formula [38]:

$$E_{\text{adsorption}} = E_{\text{system 1 + system 2}} - E_{\text{system 1}} - E_{\text{system 2}} \quad (5)$$

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administration, J.M.R.-d.-A., L.F.M.; Resources, L.F.M.; Validation, J.M.R.-d.-A., M.C., A.F.J.G. and L.F.M.; Writing—original draft, J.M.R.-d.-A. and L.F.M.; Writing—review and editing, J.M.R.-d.-A. and L.F.M. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

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