

## Article

**A wavelet-based method for the impact of social media on the economic situation: The Saudi Arabia 2030-vision case**Majed Salah S. Balalaa <sup>1</sup>, Anouar Ben Mabrouk <sup>2,3,4,\*</sup> and Habiba Abdessalem <sup>5</sup><sup>1</sup> Deanship of Public Relations and Media, University of Tabuk, Saudi Arabia.; mbalalaa@ut.edu.sa<sup>2</sup> Department of Mathematics, Faculty of Science, University of Tabuk, Saudi Arabia;  
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**Abstract:** In the present paper, a wavelet method is proposed to study the impact of electronic media on economic situation. More precisely, wavelet techniques are applied versus classical methods to analyze economic indices in the market. The technique consists firstly in filtering the data from unprecise circumstances (noise) to construct next a wavelet denoised contingency table. Next, a thresholding procedure is applied to such a table to extract the essential information porters. The resulting table subject finally to correspondence analysis before and after thresholding. As a case of study, the KSA 2030-vision is considered in the empirical part based on electronic and social media. Effects of the electronic media texts about the trading 2030 Vision on the Saudi and global economy has been studied. Recall that the Saudi market is the most important representative market in GCC continent. It has both regional and worldwide influence on economies and besides, it is characterized by many political, economic and financial movements such as the worldwide economic NEOM project. The findings provided in the present paper may be applied to predict the future situation of markets in GCC region and may constitute therefore a guide for investors to decide about investing or not in these markets.

**Keywords:** Textual analysis; Media; Correspondence analysis; Wavelet thresholding, GCC markets, KSA 2030-vision.

### 1. Introduction and motivation

A major problem in data analysis is the availability of abundant data, such as electronic textual news. Therefore, the analysis of such type of data is of great interest, and also extremely difficult because of many reasons. One main reason is the fact that electronic data is based in a great part on social media such as Facebook, Twitter, Instagram, etc. In such media, the control of the exactitude of news is extremely difficult. Besides, there is no rigorous analysis done on this news to extract the reality from fuzzy and/or false news. Consequently, there are no reasonable interpretations and discussions. Although, the affects and influence of this type of data has shown to be extremely important in many cases such as political changes in many countries.

Textual analysis has been the object of several studies. Antweiler and Frank in [3] investigated financial textual data. Dershowitz et al. in [28] applied the textual analysis for religious studies. In [36], a textual analysis is applied for political sciences. In [44], it is applied for literature texts analyzing. In economics, however, it is noticed that textual

analysis is not yet widely developed, except few cases such as [55,58].

In the literature, the most used techniques in textual analysis are based on the so-called multidimensional data analysis such as factorial and classification. Such methods have been shown to be efficient in visualization and classification aims in many cases. See [50].

The present paper focuses on the KSA 2030-vision and its circulation in electronic media, especially Twitter. A type of advanced mathematical analysis will be applied such as wavelet theory to study the impact of Twitter trading 2030 Vision on the Saudi and global economy. Recall in particular that Saudi Arabia has established 2030 projects that have a direct impact on the national market and thus the national economy, as well as the rest of the Gulf and global markets and economies, especially "Neom" project which will have a profound impact on the movement of markets and economies.

The KSA 2030-vision is an ambitious economic and social reform plan launched by the crown prince Mohammad Bin Salman in April 2016. This plan is elaborated as a response to the budgetary difficulties faced by the Saudi Arabia after the sharp decrease of oil prices in 2014. Its main goal is to reduce the oil dependency, diversify Saudi Arabia economic resources, and develop public service sectors like education, health, infrastructure, entertainment, and tourism. This program is based particularly on the development of the private sector, the attraction of foreign investors, the reduction of the unemployment rate, and the reconsideration of Saudi women status. The vision includes also plans related to the development of renewable energies, the mining sector as well as the production of natural gaz.

The KSA 2030-vision is structured around 13 operational programs: quality of life, national companies' promotion, Saudi character enrichment, housing, human capital development, public investment fund, financial sector development, national transformation, hajj and umrah, fiscal balance, national industrial development and logistics, strategic partnerships and privatization. These programs represent the vision realization system. They include plans that improve the life quality of residents, strengthen the national identity and Islamic values, provide more employment opportunities, support culture, entertainment and arts. One of the vision biggest plans is the "NEOM" project, a megacity including futuristic buildings, flying taxis, robot dinosaurs, etc.

Our main aim here is to predict the economic situation in KSA by means of the information circulating in social and electronic media on the 2030-vision. This choice is motivated and justified by the fact that KSA market is the most important representative market in GCC continent. It has both regional and worldwide influence on economies and besides, it is characterized by many political, economic and financial movements such as the worldwide economic NEOM project. Recall in particular, that the Kingdom of Saudi Arabia has established 2030 projects that have a direct impact on the national market as well as the rest of the Arab Gulf and international markets such as Aramco subscription, and particularly NEOM project which will have a profound impact on the market. This makes it of interest to study such market and understand its complexities. The last year is also characterized by the appearance of the pandemic COVID-19 that has been spread worldwide. GCC continent and especially KSA is related to all the world because of their

geographical position and their strong effect on the worldwide economies as biggest petroleum regions. Besides, they gather the largest workers' number. The Muslim saint cities in KSA are also the largest meetings of persons each year. These may be a strong cause of dispersion of viruses which may be next transferred to other countries.

In the present work, the method consists in applying wavelet theory essentially at the step of denoising the contingency table (seen as an image) [1]. Indeed, classical textual analysis suffers from one main disadvantage due to noised results and especially contingency matrices. Sometimes, retaining only the higher frequency forms (whose frequency is greater than to some threshold) leads to a partial lexical table which may not describe accurately the reality, especially when such forms constitute together a big part of the information. Besides, contingency tables may also be aggregated due to crossing different graphic forms of the lexicon with a set of variables fixed in advance. This makes the application of statistical methods in such cases resulting in non-accurate analysis of the relationship between the variables and the textual data. Wavelet methods, mainly wavelet thresholding, are adapted to overcome these problems without deleting a big piece of the information. The contingency table will be decomposed due to the application of wavelet analysis into components. The first component reflects the global shape of the image, and other components containing the noise. The application of the wavelet denoising method based on the thresholding permits to avoid this noise. The thresholding consists to remove the small coefficients which are typically noisy without affecting the image quality. Next, the denoised or thresholded contingency table is reconstructed by using an inverse wavelet transform. As the denoised tables are obtained, the results are subject of correspondence analysis [38,39] before and after thresholding. The efficiency of the proposed method is evaluated on correspondence analysis and classification results using Kohonen maps [43].

The findings provided in the present paper may be applied to predict the future situation of markets in GCC continent, and may constitute therefore a guide for investors to decide about investing or not in these markets. Moreover, wavelet theory as a mathematical tool is recently introduced in the field of finance and proved its performance compared to classical tools. In the field of textual analysis, in our knowledge, the present work is a first application of such a method, among [1] and [58]. In [1], the subject was about an economic applications similar to the present work, and in [58] the application has dealt with information processing. In the present work, one aim is to continue to prove the efficiency and the performance of such a method by applying it to different type of media texts.

The proposed method lies in fact in a whole topic of representating textual data by means of time series, statistical series, signals and/or images. This will permit to apply sophisticated mathematical and statistical methods for different purposes such as filtering, denoising, extracting information, decrypting, modeling, etc. There are in the literature many similar studies and/or ideas using this conversion of textual data into numerical one to serve from mathematical tools such as wavelets. In [58], for example, a similar method has been applied for textual information. Biological series such as DNA and proteins are also types of textual and/or character data. Wavelets are applied in such concepts for the purpose of denoising, filtering, and forecasting. Fischer et al in [34]

applied a wavelet denoising method to predict transmembrane proteins helices. Arfaoui et al [4,5] Cattani et al conducted wavelet methods for the complexity and symmetries in DNA series, See [19,20,21,22,23] and also [17,18]. Schleicher [57] conducted a fascinating study on the use of wavelet methods in econo-financial fields, such as filtering, thresholding, denoising, forecasting, etc. A prominent comparison with Fourier analysis has been highlighted in [57] showing the superiority of wavelet analysis against Fourier one.

The rest of this paper will be as follows. Section 2 is concerned with a brief review of existing statistical methods for textual data analysis. In the next section, wavelet method is developed. Section 4 is devoted to the description of the data applied here. Section 5 is concerned with the discussion of the empirical results. Section 6 is a discussion section devoted to a comparison between wavelet analysis and Fourier, especially in relation to the present application of wavelets for textual data. Section 7 is a concluding part.

## 2. Textual data analysis

### 2.1. Existing statistical methods

The use of statistical methods for textual data analysis is called lexicometry [53]. This approach, known also by lexical analysis, allows a linguistic and/or statistical analysis of the texts in a given corpus. In the following table a comparison is conducted between two main categories of lexical methods including the quantitative analysis and the multidimensional descriptive analysis.

**Table 1:** Comparison between existing methods of textual analysis

	Quantitative analysis	Multidimensional analysis
Principle	Quantitative study of the text vocabulary (richness, distribution of words, etc.).	Analysis and visualization of the text content using factorial correspondence analysis and automatic classification.
Steps	-Segmentation of the corpus and identification of the graphical forms. -Assigning a sequence number to all the occurrences of the same graphical form ([47,48,49,50]).	-Identifying graphical forms. -Keeping forms that carry information. -The graphical forms are subject to a lemmatization process. -A lexical matrix, considered as a particular contingency table, is constructed. The graphical forms are the rows of this table, while the columns correspond to the corpus parts ([47]).
Advantages	Extremely helpful in the analysis of the vocabulary of different texts, the study of the evolution of an author style, and the comparison of many authors' styles ([53]).	Application of these techniques has proved a great value in the analysis of political speeches, interviews, open questions in surveys, electronic data, etc. This category of lexical analysis concentrates on the content of the texts rather than their forms, which make it a valuable tool for the comprehension of the corpus content.
Disadvantages	The main disadvantage of these techniques is that they give priority to the analysis of the form of the texts while neglecting the content.	Lexical table constructed could be noisy by various errors occurred while entering or segmentating ([33]). Errors related to the lemmatization step (combining homonyms or polysemous words) affect the results of the multidimensional data analysis methods ([46,51]).

### 2.2. Multidimensional methods: correspondence analysis and classification

Correspondence analysis has been originally developed by Benzecri in [16] as a descriptive multivariate technique for analyzing contingency matrices by exploring the eventual links rows/columns [48]. Since its appearance, correspondence analysis has been the object of many studies especially in data analysis applied in various research fields such as social sciences, financial data comprehension, management, etc.

One main strong point for correspondence analysis is its ability to simultaneously representing and explaining finitely many variables' categories in some suitable spaces having low dimensions. However, such reduction of dimensionality may induce a loss of information. The joint plot graphical display obtained via a correspondence analysis permits the identification of relationships between rows variables, columns and cells according to the placement in shared spaces ([38,39]).

Besides, the application of correspondence analysis allows to analyze the similarity character in the contingency matrix cells by using the well-known Chi-Square distances [16]. Such a distance is evaluated as a probability measure on the rows/columns of the contingency table by quotienting the frequency associated to the elements by the total frequency of the corresponding row/column. In Escofier [32], a geometrical representation has been developed for different modalities corresponding to the row/column's variables. Besides, the eventual link point-to-point is explained by means of similarities.

In textual data, correspondence analysis is somehow recent and needs more developments. The literature is growing up just in the last decades. In such a direction, correspondence analysis is applied on lexical tables by tabulating the different corpus terms issued from the textual documents. The table explains the eventual correspondence between cells and the textual units' occurrences such as repeated segments, terms and lemmas. In [31], the authors noticed that correspondence analysis may be also applied to study lexical words/documents relations graphically.

Besides, correspondence analysis is generally followed by classification methods in order to understand more the texts analyzed and to yield a simplified resume known in financial analysis as the map of different classes or sectors. The most known method is due to Kohonen map classification or self-organization map. This technique allows precisely the classification of the elements of the contingency table into rectangular/polygonal windows gathering clusters of similar data relatively to the similarity tests [47].

### **3. The wavelet method for textual data**

The basic idea behind wavelet analysis of data is its scale analysis ability. Indeed, wavelets satisfy some special mathematical requirements that are useful in data representation. For example, in the case of non-stationary data, wavelets are proved to be efficient descriptors for trend representing, volatility clustering and variance due to their ability to take into account both frequency and time in the multiresolution contrarily to the Fourier transform [37,60].

Wavelet analysis is based on two types of source functions, the father wavelet  $\phi$  and the mother wavelet  $\psi$  (which are in the majority of cases related to each other especially in the case of the existence of a multiresolution analysis). Their Fourier transforms satisfy

$$\hat{\phi}(0) = 1 \text{ and } \hat{\psi}(0) = 0.$$

The father and mother wavelets permit to describe efficiently the components of the signal. The father wavelet is adopted to the smooth or the low-frequency part, and the mother is well adopted to the details or the high-frequency parts of the signal. The first step consists in introducing the wavelet basis elements formally expressed (in the dyadic version) as

$$\phi_{j,k}(t) = 2^{-\frac{j}{2}}\phi(t - 2^j k/2^j) \text{ and } \psi_{j,k}(t) = 2^{-\frac{j}{2}}\psi(t - 2^j k/2^j).$$

These copies needs to be mutually orthogonal to yield good representations. Existing examples are due to Haar, Daubechies, Symlets, Coiflets, etc. Using wavelet basis, a signal  $f$  may be approximated at a level  $J \in \mathbb{Z}$  by

$$f_j(t) = \sum_k S_{j,k} \phi_{j,k}(t) + \sum_k d_{j,k} \psi_{j,k}(t) + \dots + \sum_k d_{1,k} \psi_{1,k}(t)$$

where  $j$  describes the frequency, and  $k$  reflects the number of coefficients in the corresponding component and describes the position or the time. One has

$$S_{j,k} = \int \Phi_{j,k}(t) f(t) dt \text{ and } d_{j,k} = \int \psi_{j,k}(t) f(t) dt.$$

The  $S_{j,k}$ 's are called the approximation coefficients and the  $d_{j,k}$  are called the detail or wavelet coefficients. More specifically, the detail coefficients describe the higher frequency oscillations and the fine scale deviations of the wavelets in the representation of the signal. The approximation coefficients represent the smooth part of the signal and thus permit to capture the trend and/or the seasonality. So that, the wavelet series of the signal  $f$  is splitted into two parts; a first part composed of the trend and reflects the global shape of the signal, and a second part composed of the fluctuations as follows,

$$f(t) \approx S_j(t) + D_j(t) + D_{j-1}(t) + \dots + D_1(t)$$

where

$$S_j(t) = \sum_k S_{j,k} \phi_{j,k}(t) \text{ and } D_j(t) = \sum_k d_{j,k} \psi_{j,k}(t).$$

To compute the coefficients appearing in the wavelet series decomposition of a signal one did not need in practice to apply the numerical integral computation for all these coefficients. Moreover, there is also no need to compute all the coefficients simultaneously. Wavelet theory provides however a flexible way by applying the so-called wavelet filters and algorithms [26,27,40]. A set  $H = \{h_{j,l}: l = 0, \dots, L_j - 1\}$  is called a wavelet filter at the level  $j$  with length  $L_j = (2^j - 1)(L - 1) + 1$  and total width  $L$  if it satisfies

$$\sum_{l=0}^{L_j-1} h_{j,l} = 0, \quad \sum_{l=0}^{L_j-1} h_{j,l}^2 = 1 \quad \text{and} \quad \sum_{l=0}^{L_j-1} h_{j,l} h_{j,l+2n} = 0$$

for all non-zero integer  $n$ . By the same way a scaling filter  $G = \{g_{j,l}: l = 0, \dots, L_j - 1\}$  is given by  $g_{j,l} = (-1)^{l+1} h_{j,L_j-1-l}$ .

The maximum overlap discrete wavelet transform (MODWT) is a type of wavelet transform issued from the discrete one [56]. It may be adopted to signal without being necessarily of dyadic size [54]. Here also, the MODWT may be associated for both wavelet and scaling coefficients by considering

$$\tilde{W}_{j,t} = \sum_{l=0}^{L_j-1} \tilde{h}_{j,l} X_{t-l} \quad \text{and} \quad \tilde{V}_{j,t} = \sum_{l=0}^{L_j-1} \tilde{g}_{j,l} X_{t-l}$$

for  $t = 1, \dots, N - 1$  where

$$\tilde{h}_{j,l} = \frac{h_{j,l}}{2^{\frac{j}{2}}} \quad \text{and} \quad \tilde{g}_{j,l} = \frac{g_{j,l}}{2^{\frac{j}{2}}}$$

called the rescaled wavelet and scaling filters respectively. For backgrounds on wavelet analysis and especially its application in finance and economics the readers may refer to [2,7,8,9,10,11,12,13,14,15,25,35,40].

A denoising technique has been developed by Donoho and Johnstone in [29] using wavelet transform to get the so-called wavelet thresholding. It is next applied for denoising in various fields particularly in signal and image processing where its efficiency has been proved. The main idea consists in eliminating detail coefficients that are irrelevant relative to some threshold. The signal is reconstructed with thresholded coefficients by applying an inverse wavelet transform. Two main types of wavelet thresholding will be considered such as the hard and soft ones [30]. The first type consists in dropping to zero all the wavelet coefficients that are lower than a given threshold by setting

$$d_{j,k} \rightarrow d_{j,k} \chi_{[0,\infty[}(|d_{j,k}|).$$

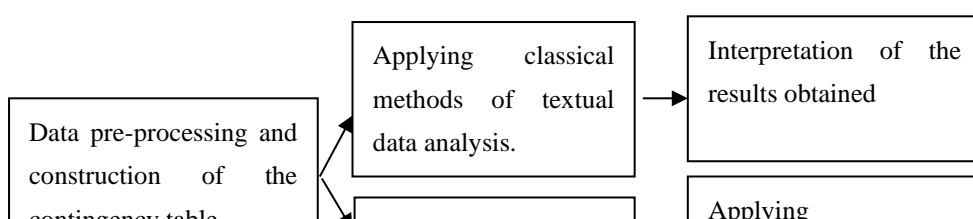
The second type consists in setting

$$d_{j,k} \rightarrow (d_{j,k} + \lambda \text{sign}(d_{j,k})) \chi_{[0,\infty[}(|d_{j,k}|),$$

where  $\lambda > 0$  is the threshold. The parameter  $\lambda$  is selected by applying the most commonly used and universal global threshold due to Donoho and Johnstone [29],

$\lambda = \sigma \sqrt{2 \log N}$  where  $N$  being the length of the signal and  $\sigma^2$  is the noise variance.

In our present paper, the denoising technique described above is used to remove noise from the contingency table constructed before applying the multidimensional textual data analysis methods. The principle of the proposed method is illustrated by Figure 1 below.



**Figure 1.** The organigram of wavelet method for textual data processing

It is clearly noticed from the diagram above (Figure 1) that the role of the wavelet technique intervenes in the step of filtering (denoising) the data contained in the contingency matrix. Recall that for data bases applied in this type of analysis, being noised, uncertain, fuzzy, missing in some cases, affects negatively the findings. It may lead to non-accurate decisions for the makers, politicians, leaders, etc. False and inaccurate interpretations cause confused and bad decisions. In economics/finance, investors also wait generally for accurate analyses to decide about their investments. These are also motivations among those raised previously that led us apply wavelet techniques. Hereafter, a brief resume of the wavelet processing is given, with some comparison with existing methods in textual analysis.

- Step 1: In the classical methods, the data applied may suffer from many problems such as the lack of data, and essentially imprecision and fuzziness. Wavelet technique consists in resolving these circumstances before processing by applying denoising methods, reconstruction of missing data, and correction of fuzzy parts.
- Step 2: The construction of the contingency tables in textual analysis is always denoised in all the classical methods. By applying wavelet denoising, a clean data basis is obtained and thus a denoised contingency table.
- Step 3: A second processing on the contingency table consists in classical methods to eliminate the least information forms (the forms with minimal frequency) in the lexical corpus, by letting to zero the corresponding values in the contingency table. However, considering a table (as equivalent to an image for example) and letting to zero in mathematical image processing may lead to non-accurate results and lacunarity. Recall that small parts in a time series may form together a great piece. In wavelet theory there is no need to eliminate these parts, while their effect may be evaluated on the whole image via their wavelet coefficients.
- Step 4: Being constructed the clean contingency table, a re-processing by the factorial correspondence analysis is conducted.

In fact, textual analysis wavelet processing is not very widely known. The efforts in such a field need more developments. In our knowledge, few works have been developed such as [55,59], where wavelets have been applied for the purpose of classification and comparison of textual data relatively to multiresolution levels. In [52], wavelet transform has been applied for the visualisation of breakpoints in textual data. In [42], wavelet thresholding method has been applied for detecting irrelevant parts in textual data.

#### 4. Data analysis



Social media sources, like Twitter, Facebook are becoming very popular around the world. The analysis of the large amounts of data generated by these medias is therefore very useful. These are short messages that may include hyperlinks and various types of multimedia like images or videos. However, the writing style used is often non-standard, where abbreviations and lots of mistakes may exist such as spelling, lexical, grammar mistakes, writing in some languages with foreign languages letters especially Arabic tweets and messages which are included in the present study.

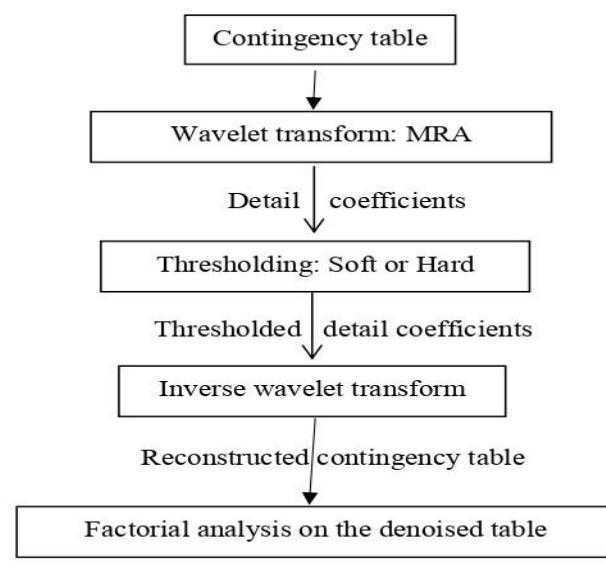
In this work, the main focus is on the analysis of the tweets that circle around the word about KSA 2030-vision, and which are written in Arabic. For the data collection, at the beginning, the twitter search API (Application programming interface) is applied, which allows to return tweets responding to a certain request. However, the limit of this method is that the number of tweets returned cannot exceed one week. For this reason, it is decided to collect the tweets by ourselves by varying each time the search keywords according to the different programs of the vision (the 13 programs). Since interests are on real time content, only original tweets are considered in the analysis. Duplicated and in-reply tweets are eliminated from the data. A set of 627 tweets are collected by successive copy/paste operations. Table 2 bellow shows an example of these tweets.

**Table 2.** Example of the tweets collected (Translated from original Arabic texts)

Date	Program	Text
03/2020	Housing program	The housing program worked on using modern and varied construction techniques, which contributed to the fast and high quality delivery of housing units.
05/2019	Pilgrims' and visitors' services	Pilgrims' and visitors' service program is planning to reach 30 million pilgrims annually by 2030.
03/2019	Human capacity development	The human capabilities development program aims to achieve strategic objectives of the 2030-vision. -Building an integrated educational journey (lifelong learning)- Comprehensive support for talented people and developing their skills. -Enrolling in prestigious universities. -Improving equal access to quality education for all.
11/2018	National entrepreneurship	The national company leadership program works to raise the percentage of local content and diversify the economy by creating opportunities for small and medium-sized companies.
11/2018	Strategic partnerships	The strategic partnerships program contributes to achieving the Saudi Vision 2030 by building and deepening strategic economic partnerships at the regional and global level.
10/2018	Public investment funds	The public investment fund program works to enhance the role of the public investment fund as the effective engine to diversify the economy in the Kingdom, and to develop specific strategic sectors through developing and maximizing the impact of the fund's investments.
08/2018	Privatization program	Privatization program is one of the programs to achieve Saudi_Vision_2030 for the development of local and foreign investments... The involvement of the private sector in the process of adopting regulations and drawing up investment policies, including the privatization system, is a pioneering step to enhance the competitiveness of the investment environment and achieve the highest possible level of transparency and governance.

After the data collection, a pre-processing stage must be conducted. The starting step reposes on the usual cleaning methods consisting mainly in removing links, hashtags, punctuation marks, numbers, non-alphabetic characters, diacritics and stop words. This step is realized due to arabic StemR package of R language. The corpus is reorganized by omitting stop words such as adverbs, articles, conjunction. In order to obtain legible and interpretable graphic representation, words with a frequency greater than 5 are kept. This has resulted in a final corpus of 3856 occurrences and 181 graphical forms. The next step consists in constructing the lexical matrix based on the 181 terms and the 13 programs of the KSA 2030-vision. This results in a (181×13) matrix. Each cell (i,j) is affected by the value 1 if the i term is mentioned in the j program and by the value 0 otherwise. This allows to interpret the contingency matrix as a binary image which permits by the next its wavelet processing [42].

In our case, the application of wavelet analysis intervenes essentially in the step of denoising the contingency table (seen as an image). Recall that a pre-processing step of the corpus resides in general to a noisy contingency table. The application of wavelet analysis permits to decompose such a table into components, a first component relative to the approximation coefficients and which reflects the global shape of the image, and other components containing the details and/or the fluctuations, relative to the detail coefficients. In this second part, the noise is concentrated. The application of the wavelet denoising method based on the thresholding permits to avoid this noise. Recall that wavelet transform leads to a sparse representation of the image, which leads to a concentration of the image features in a few large-magnitude wavelet coefficients. The thresholding consists to remove the small coefficients which are typically noisy without affecting the image quality. Next, the denoised or thresholded contingency table is reconstructed by using an inverse wavelet transform. The diagram in Figure 2 illustrates the application of wavelet analysis in our case.



**Figure 2:** The wavelet analyzing procedure.

## 5. Results and discussions

### 5.1 Correspondence analysis before denoising

#### a) Variance explained by the factors

In this step, a correspondence analysis is applied on the original non thresholded lexical table. In Table 3, the eigenvalues and the percentages of inertia explained are presented, provided with the cumulative percentages for all dimensions of the contingency matrix. It is noticed that the first axis contains approximately 15.22% of the inertia, and the second one accounts for approximately 13.07%. The two axes together yield a cumulative total amount of inertia of approximately 28.29%. Statistically speaking, in correspondence analysis, this cumulative percentage is not satisfactory enough, as an important high percentage is expected for the total variance to be explained by these two principal axes.

**Table 3.** The factors eigenvalues and variance (before denoising)

Factor	Eigenvalue	Explained variance (%)	Cumulative variance (%)
1	0.23964162	15.22	15.22
2	0.20582392	13.07	28.29
3	0.17350014	11.02	39.31
4	0.15208723	9.66	48.96
5	0.14197041	9.02	57.98
6	0.13169175	8.36	66.34
7	0.12096496	7.68	74.02
8	0.10259253	6.51	80.54
9	0.09538481	6.06	86.60
10	0.08561771	5.44	92.03
11	0.07146756	4.54	96.57
12	0.05398047	3.43	100.00

#### **b) Representation of the first factorial plan**

Figure 3 illustrates the projections of the row vectors and the column vectors of the lexical table on the first factorial plan before denoising. This graph presents a scatter plot concentrated around the gravity center which is due to the low percentage of the inertia explained by the factorial plan (only 28.29% of the total variance is explained). Such a representation leads to a low analysis quality, since a good one is generally obtained when the first two dimensions represent a large part of the total variance.

By looking to the modalities of the variable “program” (columns of the contingency table) having an absolute contribution higher than the average one, it is observed that the modalities (prog.11) and (prog.5) are important for the first factor and the modalities (prog.1), (prog.12), (prog.3) and (prog.6) are important for the second factor. However, the result of the relative contribution shows that only the modality (prog.11) is well represented with a squared cosine values equal to 0.64 (Table 4). All the other modalities have a bad representation quality on the first factorial plan and therefore they cannot be retained in the analysis.

Figure 3 contains clearly a condensed part that is not easy to interpret, and reflects therefore a bad projection of the data according to the classical method applied before the wavelet processing. The majority of modalities are accumulated around the origin. In the sense of signal or image speaking, this figure is interpreted as a noised image. In the appendix, some modified versions of Figure 3 are provided in order to clarify more and to show the unefficiency of the classical method. This motivates the application of wavelet analysis proposed in the present work. Indeed, the application of the wavelet transform in the case of the contingency table permits to decompose the latter according to the



<u>db4_hard</u>	<u>45.99</u>	<u>29.13</u>	<u>75.12</u>
<u>db4_soft</u>	<u>59.39</u>	<u>33.73</u>	<u>93.12</u>
<u>db6_hard</u>	<u>54.60</u>	<u>26.83</u>	<u>81.43</u>
<u>db6_soft</u>	<u>60.64</u>	<u>34.25</u>	<u>94.89</u>
<u>db8_hard</u>	<u>46.61</u>	<u>28.19</u>	<u>74.80</u>
<u>db8_soft</u>	<u>61.19</u>	<u>34.79</u>	<u>95.98</u>
<u>db16_har</u>	<u>42.43</u>	<u>24.82</u>	<u>67.25</u>
<u>db16_sof</u>	<u>61.48</u>	<u>35.86</u>	<u>97.34</u>

From Table 5, it is easily concluded a significant improvement of explained variance relative to the first plan. Moreover, the soft thresholding yields better improvement than the hard threshold. It is also noticed that the highest result of the cumulative explained variance is reached by using the wavelet db16 with approximately 97.34%. This permits to conclude that such a solution is the most powerful, and thus it will be subject of the next steps. It guarantees a minimum waste of information.

#### **b) Absolute and relative contribution of the modalities**

The correspondence analysis in this case is of a good quality as the sum of the variance explained by the first two factors adds up to 97% of the total inertia. This can be shown also by the analysis of the relative contribution of the different modalities of the variable "program". As presented in table 6, for the first axis, the most contributing modalities (with the highest absolute contribution values are (prog.11), (prog.8), (prog.1), (prog.12), (prog.10) (prog.4) and (prog.7). Their relative contribution values are higher than 0.8 (only for the modalities (prog.4) and (prog.7)) meaning that they are well represented on this axis. The axis 2 is constructed by the modalities (prog.2), (prog.3), (prog.5), (prog.9) and (prog.6). With a squared cosine values higher than 0.7 (only for the modality (prog.6)), these modalities are also well represented on the second axis.

**Table 6.** Relative and absolute contribution of the variable "program" modalities (after denoising)

	<u>Absolute contribution</u>		<u>Relative contribution</u>	
	<u>Axis 1</u>	<u>Axis 2</u>	<u>Axis 1</u>	<u>Axis 2</u>
<u>prog.1</u>	<u>13,40</u>	<u>4,30</u>	<u>0,83</u>	<u>0,16</u>
<u>prog.2</u>	<u>0,10</u>	<u>14,90</u>	<u>0,01</u>	<u>0,95</u>
<u>prog.3</u>	<u>0,30</u>	<u>14,40</u>	<u>0,03</u>	<u>0,93</u>
<u>prog.4</u>	<u>8,50</u>	<u>7,00</u>	<u>0,67</u>	<u>0,32</u>
<u>prog.5</u>	<u>1,50</u>	<u>13,50</u>	<u>0,15</u>	<u>0,79</u>
<u>prog.6</u>	<u>5,30</u>	<u>9,50</u>	<u>0,48</u>	<u>0,50</u>
<u>prog.7</u>	<u>7,00</u>	<u>7,40</u>	<u>0,61</u>	<u>0,37</u>
<u>prog.8</u>	<u>13,60</u>	<u>2,60</u>	<u>0,88</u>	<u>0,10</u>
<u>prog.9</u>	<u>2,50</u>	<u>13,30</u>	<u>0,23</u>	<u>0,72</u>
<u>prog.10</u>	<u>12,30</u>	<u>1,10</u>	<u>0,92</u>	<u>0,05</u>
<u>prog.11</u>	<u>18,00</u>	<u>0,10</u>	<u>0,99</u>	<u>0,00</u>
<u>prog.12</u>	<u>13,00</u>	<u>0,90</u>	<u>0,91</u>	<u>0,04</u>
<u>prog.13</u>	<u>4,60</u>	<u>11,00</u>	<u>0,41</u>	<u>0,58</u>

A significant improvement of the relative contribution of the rows of the contingency table (the graphical forms) is also noted after denoising. Table 7 presents a comparison of the results obtained before and after denoising for some graphical forms. As shown in this table, the representation quality of the graphical forms on the first plan is better after denoising. Taking for example the modality (partnership), the sum of the squared cosine

values on the first two axes goes from 0.12 before denoising to 1 after denoising of the lexical table, thus showing a good representation quality on this plan.

**Table 7.** Comparison of the relative contributions of some graphical forms before and after denoising

	Before denoising		After denoising	
	Axe 1	Axe 2	Axe 1	Axe 2
Training	0,05	0,14	0,98	0,02
Partnership	0,09	0,03	0,97	0,03
Financial	0,14	0,09	0,01	0,97
Participation	0,00	0,00	0,14	0,85
Tourism	0,23	0,13	0,12	0,83
Upgrade	0,23	0,13	0,01	0,97

Therefore, the interpretation of the relative position, on the first factorial plan, of the different modalities (the rows and the columns of the contingency table) is identified as the most important.

### c) Representation of the first factorial plan

In Figure 4, the projections of the contingency matrix rows and columns on the first factorial plan are provided after the denoising. On this graphical display, only the words whom contribution to the inertia are greater than the average are illustrated, and an acceptable representation quality (squared cosine values higher or equal to 0.7). It is precisely noticed that the first factor explain approximately 61.48% of the total variation, while the second factor explains approximately 35.86 %.

On the right of the first axis (Figure 4), the modalities (prog.8), (prog.1) and (prog.11) are observed to be in proximity of the graphical forms (economy), (Saudi), (small), (medium), (regionally), (creation), (job), (more), (sport), (quality), (better), (pilgrimage) and (million). In fact, the goal of national companies' promotion program is to promote the development of national companies and to support the competitiveness of small and medium sized enterprises as well as their productive and export capacities. This leads to enhance the Saudi economy regionally and internationally and to the creation of more job opportunities. Through the quality-of-life program, the government seeks to improve the way of life of Saudis by encouraging them to participate in cultural, entertainment and sports activities. Hajj and Umrah program aims to increase the number of pilgrims to 30 million in 2030.

On the left side of axis 1, (prog.12), (prog.10), (prog.4) and (prog.7) are found to have a higher representation quality for the first two modalities ( $\cos^2 = 0.91$  and  $0.92$ , respectively) than for (prog.4) and (prog.7) ( $\cos^2 = 0.67$  and  $0.61$ , respectively). These modalities are situated in proximity of the graphical forms (training), (programs), (human), (partnership), (competitiveness) and (strategic). In fact, the human capital development program aims to improve educational and training systems in order to provide a human capital that responds to the labour market requirement and that promotes the kingdom's international competitiveness. For the strategic partnerships program, its main objective is to ameliorate and strengthen the economic partnerships with the foreign countries that are considered as strategic actors for the KSA 2030-vision success. Among these countries, France, Germany, United States, Great Britain, China,

South Korea, Japan and Russia have to be good partners. Recall that the objective of fiscal balance program is to achieve a balanced budget, maintain stable reserves and conserve the government debt capacity. While the privatization program leads to the amelioration of the services quality provided, the increase of the government revenues and the creation of new jobs. In such a program, many sectors are concerned by privatization such as telecommunication, environment, water, labour market, transport, housing, pilgrimage and visits, health, education, municipalities, energy, and agriculture.

The second axis is constructed, on its right side, by the modalities (prog.2), (prog.9) and (prog.13) with a higher representation quality for prog.2 and prog.9 ( $\cos^2=0.95$  and  $0.72$ , respectively) than for (prog.13). In proximity of these modalities, the words (investment), (saving), (development), (growth) and (zones) are detected. In fact, the financial development program has a main role in creating an efficient, stable and diversified financial sector, which in turns leads to the national economy development, the diversification of its resources and the stimulation of saving, growth and investment. The primary goal of the national industrial development and logistics program is the development of the industrial zones and the manufacturing production while the Saudi character enrichment program aims to develop and strengthen the national personality of Saudi citizens by fostering a set of Islamic and national values.

On the left hand of axis 2, the modalities (prog.3), (prog.5) and (prog.6) are observed with a higher representation quality for (prog.3) and (prog.5) ( $\cos^2= 0.93$  and  $0.79$ , respectively) than for (prog.6). By studying the contribution of the words that participate to the construction of this axe, the graphical forms (life), (decent), (home), (access), (citizen), (own), (women), (development) and (tourism) are detected. In fact, in order to improve the percentage of the Saudis homeowners as well as the quality of homes that guarantee a decent life for citizens, several initiatives have been taken through the housing program. Talks are about the facilitation of the finance access for the purchase of a real estate, the improvement of housing service quality, the construction of housing suitable for all income groups and the encouragement of the private sector to carry out real estate's projects. For the national transformation program, its main objectives are the transformation of the health sector, the amelioration of the environment living of Saudis, the preservation of natural resources, the enhancement of the associative sector, the raising of the women participation in labor market, the facilitation of working access for disabled people, the enhancing of the working conditions of foreign workers and finally the development of private and tourism sector. Through the public investment fund program an improvement of the public investment fund and a promotion of its investment capabilities are the main desired goals.

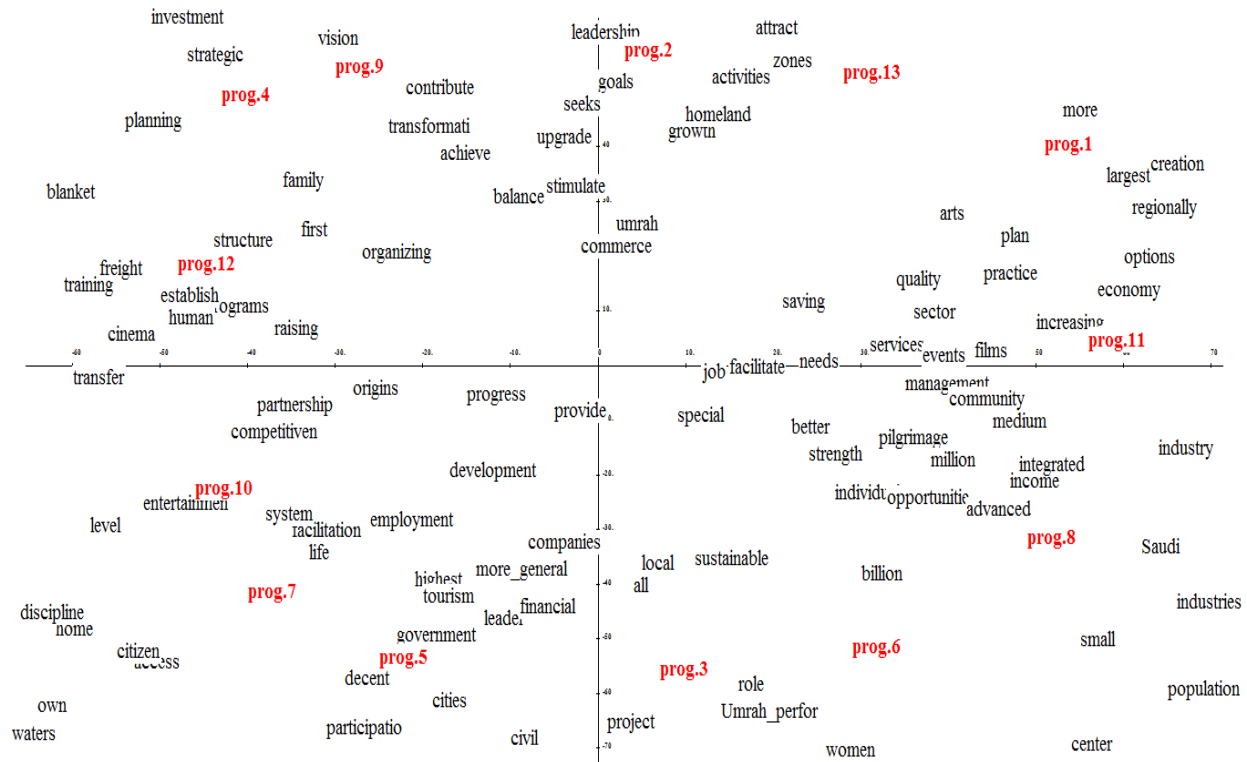


Figure 4. The first factorial plan from correspondence analysis on denoised lexical table.

Table 8. The 13 programs of the KSA 2030-vision

Program	Corresponding Sector
Program1	Quality of Life Program
Program2	Financial Sector Development Program
Program3	Housing Program
Program4	Fiscal Balance Program
Program5	National Transformation Program
Program6	Public Investment Fund Program
Program7	Privatization Program
Program8	National Companies Promotion Program
Program9	National Industrial Development and Logistics Program
Program10	Strategic Partnerships Program
Program11	Hajj and Umrah Program
Program12	Human Capital Development Program
Program13	Saudi Character Enrichment Program

### 5.3 Classification results: Kohonen map

Unlike factorial plans, The Kohonen self-organizing map allows more simplified visualization by representing simultaneously and without superposition, the rows and the columns of the contingency table presenting similar profile, in rectangular or polygonal windows. A Kohonen map representation is given in figure 4 where each window regroups co-occurring graphical forms. The modalities of the variable “program”



figure also in different windows of the map. This graph allows then a quickly identification of the words co-occurrences as well as the lexical proximities between the modalities.

A comparable synthesis to that resulting from of the correspondence analysis (figure 3), is obtained. For example, the class 13 of Figure 5, characterized by the modalities (prog.4) and (prog.9) and the class 16 of the same figure, characterized by the modalities (prog.1) and (prog.13) are characterized by neighboring graphical forms in the two representations (“vision” “strategic”, “planning”, “investment” etc. for class 13 and “more”, “house”, “construct”, etc. for class 16). These two categories are distant on the two representations which is the case for the other classes. For example, in class 9, the modality (prog.12) is detected in proximity of the graphical forms “training”, “structure”, “raising”, “programs”, etc, situated far away, on the two figures, from class 12 where the modality (prog.11) is in proximity of the words “regionally”, “increasing”, “quality”, “arts”, etc. These findings show that the wavelet method has maintained the complementarity aspect between factorial analysis and classification methods, which proves its efficiency for textual data analysis.

#### **6. Further discussion**

There are many different points in Fourier analysis relatively to wavelet one. One simple task resides in the fact that two different signals and/or images may have the same Fourier transform. Moreover, in Fourier transform a useful information in the signal/image may be dispersed on the whole frequency domain and thus may not be detected by the transform. This is what we call the localisation property. Indeed, compared to Fourier, wavelet transform permits a well localization in both time and frequency, and permits besides to analyse the data according to the scale. From the point of view relative to the frequency content, a stationarity character is always assumed on the whole-time domain for Fourier analysis. From the point of view of localisation, any modification and/or change at a point in the time domain will be reflected in Fourier transform sense on the whole domain. Furthermore, wavelet decomposition of signals permits an independently component-wise analysis. Fourier transform could not detect simultaneously long-term and high-frequency movements, especially for non-stationary signals.

Related to the present subject, the procedure applied in our case may also be viewed as a wavelet filtering of a noisy image. In such a purpose, the procedure consists in removing the detail coefficients which are below a fixed threshold. In the case of Fourier transform, the coefficients in the frequency domain below a certain bandwidth are removed. Due to the localization property, the wavelet method in this case is performant as Fourier one needs a large number of coefficients, which may affect the local character of the image. This disadvantage does not occur for wavelet filtering as it permits to estimate the scale or the level of best wavelet decomposition. A scale-wise or level-wise analysis provides more understanding of the image or the series.

Already with relation to the present work, which may be subscribed also in the whole topic of socio-economic studies, the wavelet decomposition permits to observe economic actions, decisions, income, and money at different scales, by acting the forecasting at the scale levels instead of the whole-time domain. In [57], for example, the

author discussed the relationship between income and money by applying causality tests to the wavelet series and stated that at the lowest timescales, money is caused by the income Granger. However, and in the contrary, income is caused by money Granger, at business-cycle periods. Moreover, the Granger causality may go in both directions at the highest scales. More about these facts may be found in [57] and the references therein.

Finally, the application of the wavelet transform in the case of the contingency table permits to decompose the latter according to the different multiresolution levels, and next to apply the best decomposition for the purpose of denoising and the corresponding analysis.

## **7. Conclusion**

In the present work, a contribution in wavelet theory applied for the purpose of textual analysis is developed. Recall that the use of wavelet theory in the processing of textual data is in fact an area that is not yet very widespread. In this paper, main focuses are on the circulation, in electronic media, of the KSA 2030-vision. The hybrid method based on combining wavelet thresholding and correspondence analysis has been proved to be efficient and performant for textual data. Removing the lexical noise from the contingency table constructed has minimized the loss of information and yielded an improvement of the rate of inertia explained by the first factorial plan. The application of the wavelet method permitted to maintain a complementarity aspect between factorial and classification methods, which permits in turns a high quality of representation and an interpretable factorial plan.

The wavelet correspondence analysis applied permits to understand and predict the situation in the KSA market such as Saudi Arabia. The idea starts by constructing a contingency table from a corpus constituted from social media articles about the 2030-vision of the Kingdom. It seems that the construction of contingency tables suffers always from noise due to many factors such as human mistakes. To remove the noise, the wavelet theory is then intervened by applying precisely the concept of wavelet thresholding.

The results of the present paper showed that the joint use of correspondence analysis and wavelet thresholding in textual data analysis is efficient and performant in analysing textual data and conducting good conclusions. The denoised contingency table permitted an improvement of the inertia rate explained by the principal factorial plan obtained by the application of the correspondence analysis. The quantity of lost information is minimized with an information rate being maximal and a number of axes being small. The wavelet denoising permitted also a good quality of factorial plan representing, provided with a good exploitation of the classification results. This in turns led to valuable interpretations.

The present work with the few ones applying wavelets in textual analysis field may lead to many future directions, such as mixed languages' corpuses, without need to translation, which may induce ambiguous results due to confusions in the senses issued from translation for example, and the choice of the good word that reflects the best the meaning from a language to another. A serious and challenging idea may be realised by generalizing the method to more large texts, such as written media, which will induce a

big data bases, and thus a complication in the processing and the analysis. Duplicated and in-reply tweets are eliminated from the data.

Related to the case study, it will be of interest to apply the method to other markets and to deduce eventual comparisons and eventual dependences between markets, such as GCC, Asian, and also petroleum exportations' countries, which are nowadays searching to reduce the dependency of their economy to petroleum, especially with the appearance and the development of other sources such as solar energy, and clean energy in general.

**Author Contributions:** “Conceptualization, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; methodology, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; software, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; validation, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; formal analysis, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; investigation, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; resources, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; data curation, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; writing—original draft preparation, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; writing—review and editing, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; visualization, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; supervision, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; project administration, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem; funding acquisition, M. S. S. Balalaa, A. Ben Mabrouk and H. Abdessalem. All authors have read and agreed to the published version of the manuscript.”.

**Funding:** This research has received no external funding.

**Acknowledgments:** The authors would like to thank the editor(s) of Mathematics and the anonymous reviewers for the interest given to our work and for the valuable comments which improved the paper.

**Conflicts of Interest:** The authors declare no conflict of interest.

1 waters solutions prog.7 process ports own output level	home finance enough distinguish discipline corporation citizen access	2 tourism prog.5 participation leader highest	government financial electricity decent civil cities	3 two-mosques role project prog.3 introduction healthy countries all umrah-perfor	4 women thriving support small residence prog.6	population market industries contribution center billion additional	
5 transfer technique targets system prog.10	partnership life facilitation entertainment competitive cinema	6 vitality provide progress origins more general	launching future employment development companies care	7 works sustainable strength special signature	local initiative individual council better	8 prog.8 pilgrimage opportunitie million medium management	integrated industry income community advanced Saudi
9 training structure raising programs prog.12 human	freight first family establish environment blanket	10 umrah style stimulate social platform organizing	mining education domiciliation cooperation commerce balance	11 strengthen saving needs job infra improvement facilitate challenges	12 step services sector regionally quality prog.11 practice plan	options largest increasing films events economy creation capability arts	
13 year vision	most_promine medical	14 upgrade transformation	goals diversification	15 zones wealth	16 sport prog.13		

transform sustainability strategic prog.9 prog.4 planning pillars	investment guests globally essential energy digital allocating	seeks prog.2 most important leadership implementation	develop contribute Arabic agreement achieve	new homeland growth facilities culture authority attract activities	prog.1 products more house efforts construct box achievements
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Figure 5. Kohonen map visualization

Appendix

The following figures are in fact reproductions of Figure 3, provided to more explain it. In Figure 3a below, the Figure 3 is reproduced by eliminating the overlapped (superposed) modalities and accumulated around the centre. Figure 3b illustrates the same graph as Figure 3 from which the modalities centred at the origin are omitted. Finally, in Figure 3c, the ellipse covers the modalities whom projections on the first plan are not well represented, and which are hidden or condensed in the original Figure 3.

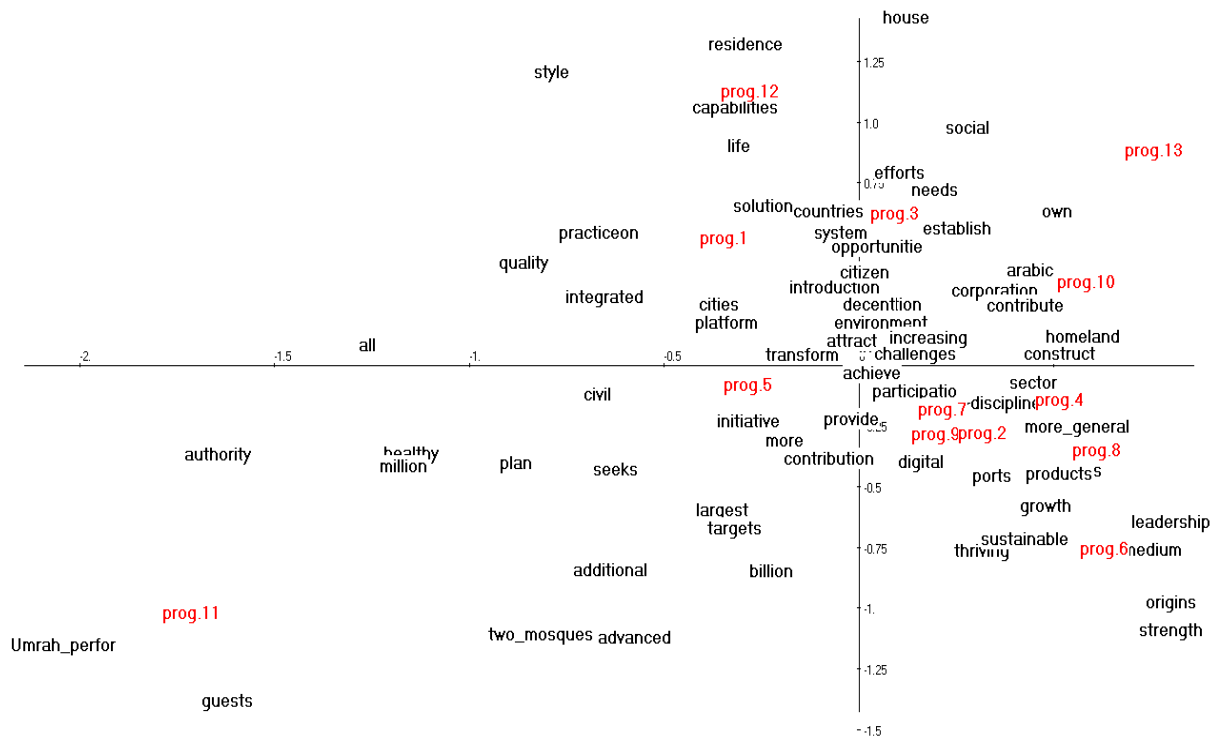
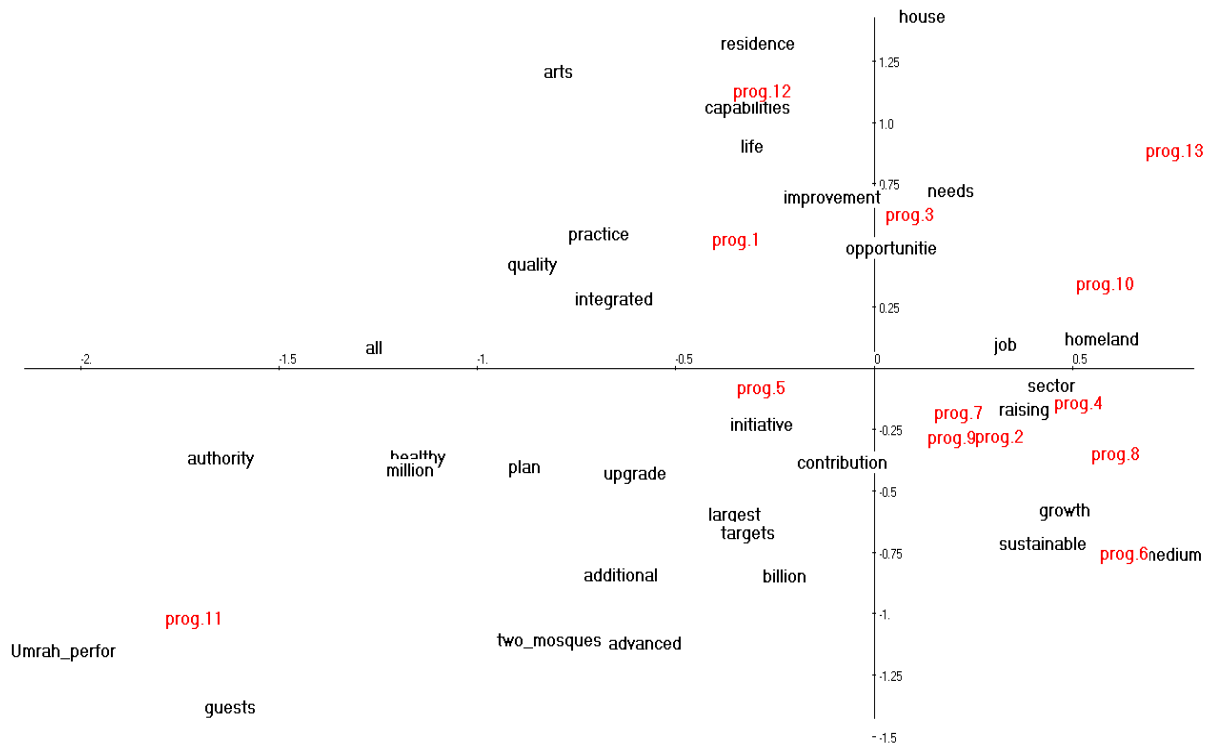
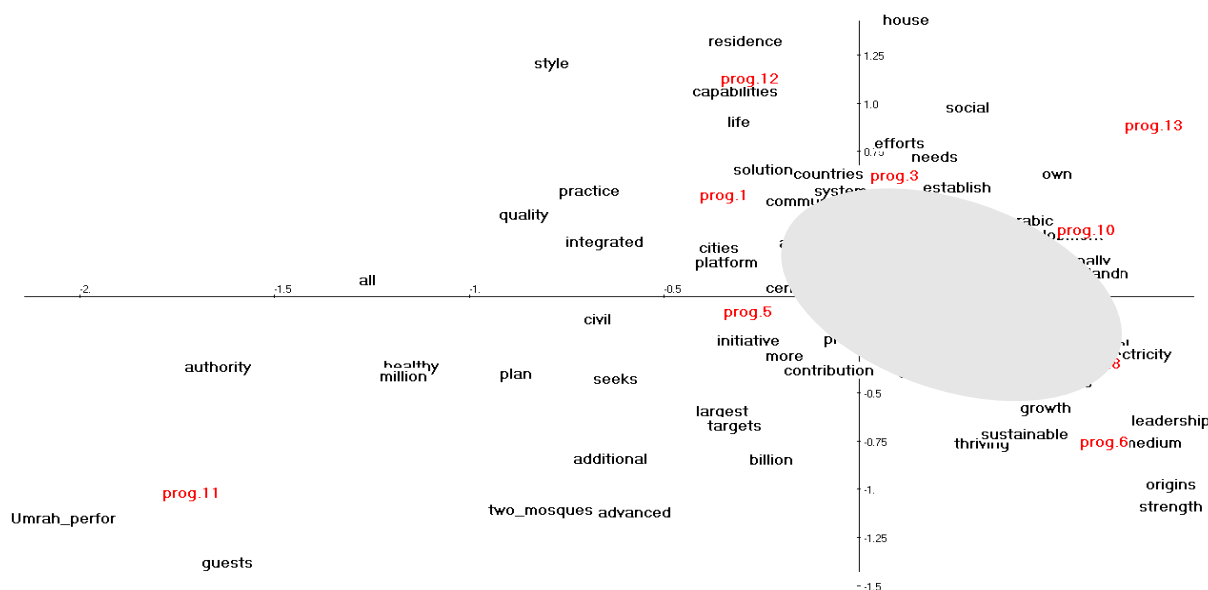


Figure 3a. A reproduction of Figure 3 by eliminating the superposed modalities.



**Figure 3b.** A reproduction of Figure 3 by eliminating modalities centred at the origin.



**Figure 3c.** A reproduction of Figure 3 where the ellipse covers the hidden modalities whom projections on the first plan are not well represented.

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