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## 2 **Medical video coding based on 2nd generation** 3 **wavelets: Performance evaluation**

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11

12 **Abstract:** The operations of digitization, transmission and storage of medical data, particularly  
13 images require increasingly effective encoding methods not only in terms of compression ratio and  
14 flow of information but also in terms of visual quality. At first, there was DCT (discrete cosine  
15 transform) then DWT (discrete wavelet transform) and their associated standards in terms of coding  
16 and image compression. After that, the 2nd generation wavelets seeks to be positioned and  
17 confronted to the image and video coding methods currently used. It is in this context that we  
18 suggested a method combining bandelets and SPIHT (set partitioning in hierarchical trees)  
19 algorithm. There are two main reasons for our approach: the first lies in the nature of the bandelet  
20 transform to take advantage by capturing the geometrical complexity of the image structure. The  
21 second reason stems in the suitability of encoding the bandelet coefficients by the SPIHT encoder.  
22 Quality measurements shows that in some cases (for low bit rates) the performances of the proposed  
23 coding compete with the well-established ones and opens up new application prospects in the field  
24 of medical imaging.

25 **Keywords:** Bandelet; medical imaging; quadtree decomposition; SPIHT coder; video coding; video  
26 quality measure.

27

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### 28 **1. Introduction and motivation**

29 The huge amount of patient medical data recorded at every moment in hospitals, medical  
30 imaging centers and others medical organizations have become a major issue. The need for  
31 quasi-infinite storage space and efficient real-time transmission in specific applications such as  
32 medical imaging, military imaging and satellite imaging requires advanced techniques and  
33 technologies including coding methods to reduce the amount of data to be stored or transmitted.  
34 Without coding of information, it is very difficult and sometimes impossible to make a way to store or  
35 communicate big data (large volumes of high velocity and complex images, audio and video  
36 information) via the internet. The encoding of these data is obtained by eliminating the redundant or  
37 unnecessary information in the original frame which can't be identified with the naked eye.

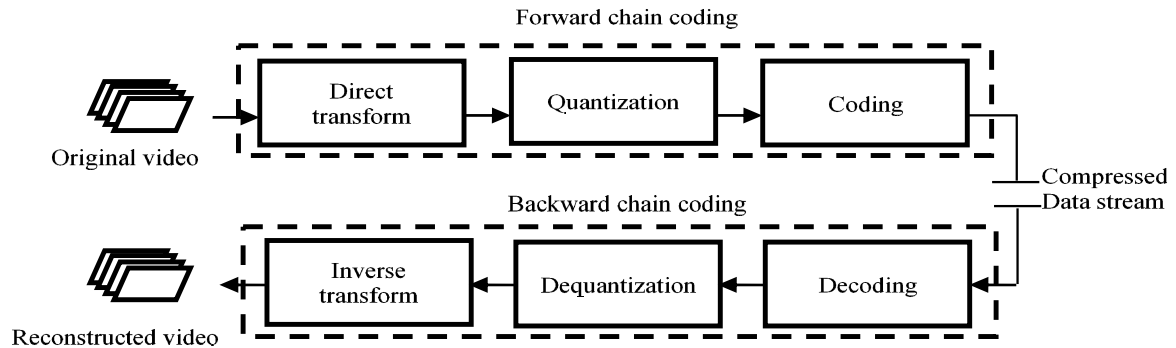
38

39 Figure 1 recalls the key steps of video coding:

40 Transformation is a linear and reversible operation that allows the image to be represented in the  
41 transform domain where the useful information is well localized. This property will make it possible  
42 during the compression to achieve good discrimination, that is to say the suppression of unnecessary  
43 or redundant information. The discrete cosine transform and the wavelet transform are among the  
44 most popular transforms proposed for image and video coding.

45 Quantization is the step of the compression process during which a large part of the elimination  
46 of unnecessary or redundant information occurs.

47 Coding techniques e.g. Huffman coding and arithmetic coding [16-18] are the best-known  
48 entropy coding particularly in image and video coding.



49  
50 **Figure 1.** Simplified video coding scheme

51

52 It is well known that lossless compression methods have the advantage of providing an image  
53 without any loss of quality and the disadvantage of compressing weakly. Hence, this type of  
54 compression is not suitable for transmission or storage of big data such as video. Conversely, lossy  
55 compression produces significantly smaller file sizes often at the expense of image quality. However,  
56 lossy coding based on transforms has gained great importance when several applications have  
57 appeared. In particular, lossy coding represents an acceptable option for coding medical images. E.g.,  
58 DICOM (Digital Imaging Communication in Medicine) JPEG based on DCT and DICOM JPEG 2000  
59 based on wavelet. In this context, wavelet-based image coding, e.g. JPEG2000, using multiresolution  
60 analysis [1-2] exhibits performance that is highly superior to other methods such as those based on  
61 discrete cosine transform (DCT), e.g. JPEG.

62 In 1993, Shapiro introduced a lossy image compression algorithm that he called embedded  
63 zerotrees of wavelet (EZW) [3]. The success of coding wavelet approaches is largely due to the  
64 occurrence of effective subband coders. The EZW encoder is the first to provide remarkable  
65 distortion-rate performance while allowing progressive decoding of the image. The principle of  
66 zerotrees, or other partitioning structures in sets of zeros, makes it possible to take account of the  
67 residual dependence of the coefficients between them. More precisely, since the high-energy  
68 coefficients are spatially grouped, their position is effectively computed by indicating the position of  
69 the sets of low energy coefficients. After separation of the low energy coefficients and the energetic  
70 coefficients, the latter is relatively independent and can be efficiently coded using quantification and  
71 entropy coding techniques.

72 In 1996, Said and Pearlman proposed a hierarchical tree partitioning coding scheme called set  
73 partitioning in hierarchical tree (SPIHT) [4], based on the same basic EZW, and exhibiting better  
74 performance than the original EZW.

75 Video compression algorithms such as MPEG-4 and H.264 use inter-frame prediction to reduce  
76 video data between a series of images. This involves techniques such as differential coding where an  
77 image is compared with a reference image and only the pixels that have changed with respect to that  
78 reference image are coded.

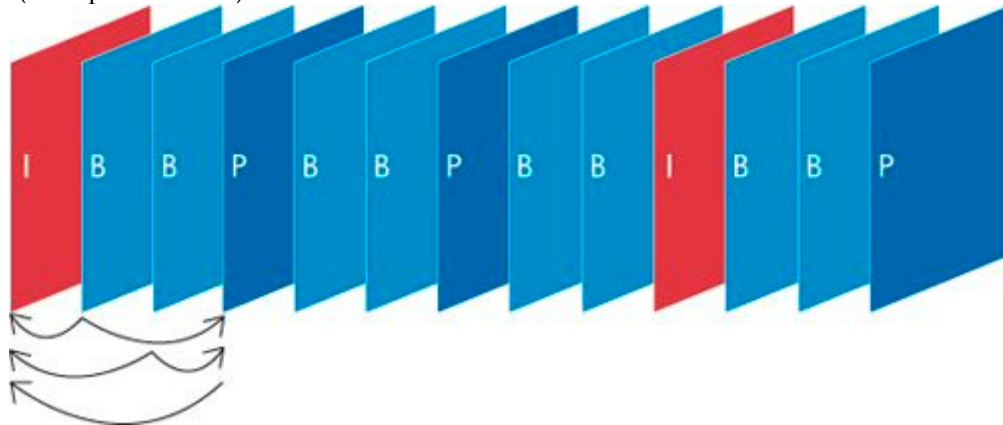
79 MPEG allows to encode video using three coding modes:

80 Intra coded frames (I): frames are coded separately without reference to previous images (i.e. as  
81 JPEG coding).

82 Predictive coded frames (P): images are described by difference from previous images.

83 Bidirectionally predictive coded frames (B): the images are described by difference with the  
84 previous image and the following image.

85 In order to optimize MPEG coding, the image sequences are in practice coded in a series of I, B,  
 86 and P images, the order of which has been determined experimentally. The typical sequence called  
 87 GOP (Group of Pictures) is as follows:



88  
 89 **Figure 2.** Typical sequence with I, B and P frames.

90 P frame can only refer to the previous I or P frames, while a B frame can refer to previous or subsequent I or  
 91 P frames.

92  
 93 To evaluate the visual quality of the reconstructed video, several measurements of the quality of  
 94 the MPEG video are validated in [5-6].

95 As a successor to the famous H.264 or MPEG-4 standards [7-8], HEVC (High Efficiency Video  
 96 Coding) or H.265 standard has recently been defined as a promising standard for video coding, In  
 97 June 2013 [9], the first version of HEVC was announced, and to improve the efficiency of the coding of  
 98 this standard, a set of its components requires more development. In addition, this new system  
 99 requires new hardware and software investments delaying its adoption in applications such as in the  
 100 medical field.

101 This work is motivated by the prospect to offer Our motivation lies in the prospect of offering a  
 102 new codec that is simple to implement with performances superior to the current H264 standard and  
 103 which could compete with the H265 or HEVC standard for some applications. This superiority is  
 104 based on the SPIHT algorithm and the second-generation wavelets.

105 One can ask: “Why using second generation wavelets (instead of classical wavelets)?”

106 This new generation of wavelets makes it possible to generate decorrelated coefficients, and to  
 107 eliminate any redundancy by retaining only the necessary information and it is better suited to  
 108 geometric data (ridges, contours, curves, or singularities). This 2nd generation wavelets consists of  
 109 Xlets such as shearlets, bandelets, curvelets, contourlets, ridgelets, noiselets, contourlets, etc. These  
 110 Xlets provide interesting performance in some applications, i.g. contourlets-based denoising [10],  
 111 contourlets-based video coding [11-12], curvelets-based contrast enhancement [13], bandelets-based  
 112 geometric image representations [14], shearlets-based image denoising [15], ...

113 In this paper, we analyse and compare to the current state-of-the-art coding methods, the  
 114 performances of a new coding method based on bandelet transform where its coefficients are encoded  
 115 using the set partitioning in hierarchical trees (SPIHT).

116 The remainder of this paper is organized as follows: Section 2 presents and recalls the main  
 117 properties of bandelet transform and Section 3 introduces bandelet-SPIHT-based video coding.  
 118 Section 4 focuses on the experimental aspect and the analysis of the results. It should be noted that  
 119 some preliminary results published recently in IEEE IECON 2016 [19] have been completed and  
 120 analyzed in order to point out the advantages but also the limitations of the proposed method.  
 121 Finally, Section 5 concludes this study.

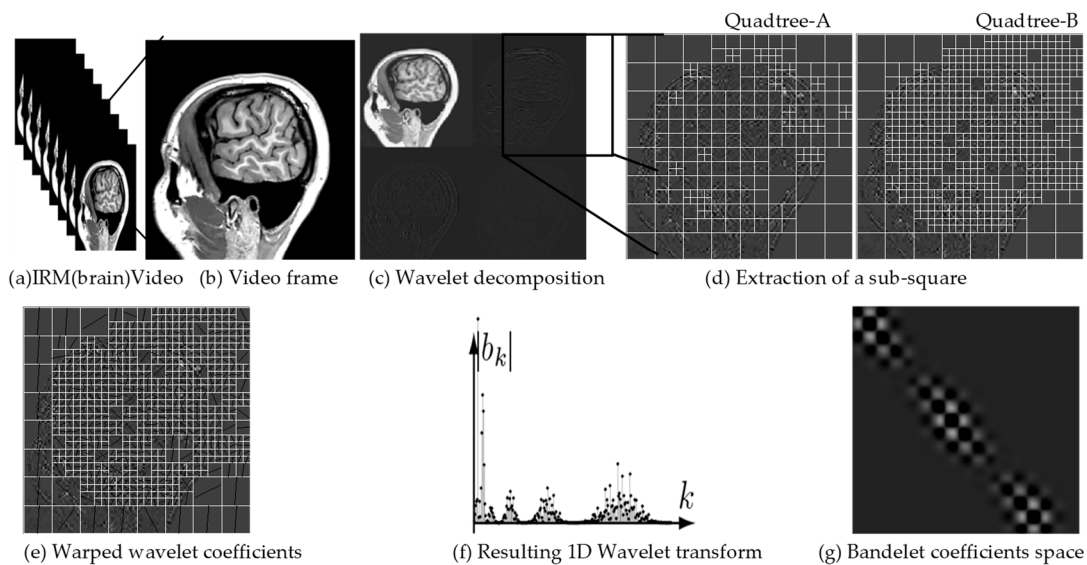


Figure 3. Example of graphical steps of the bandelet transformation algorithm

## 2. Bandelet transform algorithm

### 2.1. Bandelet transform

In order to organize intra- and inter-frames interactions, we choose the threshold to control the coding rate of the algorithm.

In step 2, 2D orthogonal or bi-orthogonal bandelet basis are performed to the original image.

The bandelization is implemented in the following steps.

Step 3:

- Performing dyadic square by recursive split of the original wavelet transform.
- Figure 3 graphically summarizes the main steps of bandelet transform illustrated on a brain MRI frame.
- Select each split dyadic square.

1D discrete wavelet transform is performed and stored in 2D image of the same size as projected result of the sampling location along potential directions and sorting 1D points result from left to right. The correct threshold and the good direction acquire a smaller approximation error.

To control the error between the recovered and the original signals for a fixed number of parameters (number of bits, quantization step and Lagrangian multiplier), a Lagrangian function is used to provide optimal direction. A better bandelet is, indeed, defined by minimizing a Lagrangian cost function. Moreover, the Lagrangian minimization requests no information on regularity.

The zigzag scanning order is used in low-scale to aggregate wavelet coefficients in the upper-left corner of the output square.

### 2.2. Geometric flows

The bandelet bases are based on an association between the wavelet decomposition and an estimation of the image information of geometric character. The estimation of the geometry is done by studying the contours present in an image. A contour is then seen as a parametric curve that will be characterized by its tangents. To do this, we look for gradients of significant importance in the frame.

Around each region of frames, the local geometry directions, in which the frame has regular variations in the neighborhood of each pixel, are determined by two-dimensional geometric flow of a vector field, instead to describe the geometry of the frames through edges.

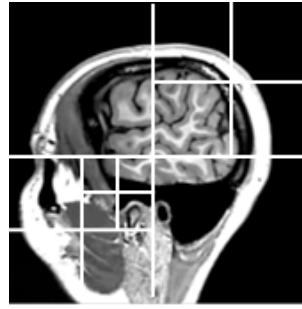


Figure 4. Example of quadtree decomposition

153  
154

### 155 2.3. Quadtree division process

156 In the discussed algorithm, on each dyadic square and scale, we apply the bandelet transform; it  
157 is evidently a redundant transformation. The best segmentation represented as a quadtree is obtained  
158 by the using of the Lagrangian optimization. An example of a quadtree area division is shown in  
159 Figure 3.

160 In order to minimize the distortion rate, we use a parallel vertical or horizontal flux in each  
161 dyadic square. The macro block is considered regular uniformly, in the case where there is no  
162 geometric flow and the wavelet basis is used. Otherwise, deformed wavelets replaced wavelet bases,  
163 as explained in [20-21].

164 All directions in each block acquired by quadtree decomposition are tested, where for a given  
165 quantization step the best quadtree requires a minimization of Lagrangian.

$$166 \quad L(f_d, R) = \|f_d - f_{dR}\|^2 + \lambda Q^2 \sum_j (R_{jS} + R_{jG} + R_{jB}) \quad (1)$$

167 where

168  $f_d$ : The original signal.

169  $f_{dR}$ : The recovered signal using inverse 1D wavelet transform.

170  $R_{jS}$ : The bits number needed to encode the dyadic segmentation.

171  $R_{jG}$ : The bits number needed to encode the geometric parameter.

172  $R_{jB}$ : The bits number needed to encode the quantized bandelets coefficients.

173  $\lambda$ : The Lagrangian multiplier is chosen to be equal to 3/28, for a justification of this value see [22].

174  $Q$ : The quantization step.

175 **Table 1.** Details and characteristics of all standards tested video

	N	u	m	be	Number	Width×	Vid
				r	of	Height	eo
Medical sequences				of	frames/		for
				fr	Second		mat
				a	(Hz)		
				m			
				es			
Brain (MRI sequence)	144	29.97	240×240				AVI
Bladder (Cancer)	662	29.97	480×320				AVI
Heart	87	29.97	340×336				AVI
Abdomen/ pelvis	295	29.97	340×352				AVI
Coronary angiography	594	29.97	360×360				AVI

176

177 The following steps implement the quadtree structure.

178 For each dyadic square  $S$  the value  $L(S) = L(f_d, R)$  of the Lagrangian is restricted to  $S$  :

179 • Initialize the quadtree with the square  $S$  of size  $L$  and initialize  $L_0(S)$ .

180 •  $(S_1, S_2, S_3, S_4)$  are the fourth sub-squares defined for each square  $S$ , and

181  $L'(S) = L_0(S_1) + L_0(S_2) + L_0(S_3) + L_0(S_4) + \lambda Q^2$  is the Lagrangian of the sub-tree

182 • The sub-squares should be merged if  $L(S) < L'(S)$ . If so, declare  $S$  as a leaf and record

183 the optimal geometry. Update  $L_0(S) = \min(L(S), L'(S))$ .

184 Repeat the previous step for each square  $S$  of size  $2L$ .

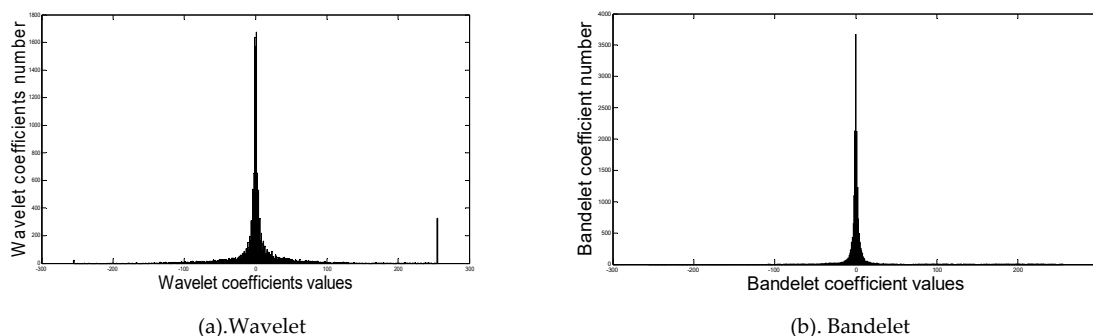
#### 185 2.4. Warped wavelet along geometric flows

186 In order to perform the complex geometry and remove the redundancy of orthogonal wavelet  
187 coefficients, bandelet basis decomposition is applied with a fast application of the geometric  
188 flow, quadtree decomposition, warping and bandeletization.

189 In each dyadic square at each scale, the geometric flow is used to warp the wavelet basis along  
190 the direction regularity. After warping, the next step is to construct bandelets by applying a  
191 bandeletization procedure.

192 The function of wavelet includes high-pass filters and the vanishing moments at lower  
193 resolutions, this is valid for vertical and diagonal detail coefficients, but not for horizontal  
194 detail coefficients. The problem of regularity along the geometric flow is due to the function of  
195 scaling where it includes low-pass filters and does not have the vanishing moment at lower  
196 resolutions.

197 To take advantage of regularity along the geometric flow for horizontal detail coefficients, the  
198 deformed wavelet basis is bandeletized by replacing the horizontal wavelet with modified  
199 horizontal wavelet function. In near of singularity, the wavelets coefficients correlations are  
200 removed by using bandeletization operation.



203 **Figure 1.** Analyses histogram of bandelet and wavelet coefficient values

206 After warping and bandeletization operations, the regions are regular along the vertical or  
207 horizontal direction. In the end, warped wavelets are used to compute bandelet coefficients with 1D  
208 discrete wavelet transform than are encoded using SPIHT coder.

209 The next section is based on the principal that the most significant coefficients are achieved by  
 210 the bandelet transform. In the applications of time constraints, this result confirms that our approach  
 211 can be used.

212 Figure 4 illustrates this feature and compares wavelet and bandelet coefficients histograms  
 213 results. Therefore, the SPIHT encoder, primarily applied to the wavelet results, will become  
 214 Bandelet-SPIHT in this contribution.

### 215 3. Process of encoding

216 SPIHT algorithm [4] is one of the most efficient encoder nowadays, were it used in many  
 217 applications [23-24]; whose special performances show its outperform to the JPEG 2000 in many  
 218 practical situations. The list of effectiveness values symbols, are not used by SPIHT encoder such as  
 219 EZW [25].

220 The SPIHT algorithm takes up the principles evoked in EZW while proposing to recursively  
 221 partition the coefficient trees. Thus, where EZW encodes an isolated insignificant coefficient, SPIHT  
 222 performs a recursive partitioning of the tree so as to determine the position of the significant  
 223 coefficients in the descendant of the considered coefficient. The significant coefficients are coded  
 224 similarly to EZW: their sign is sent as soon as they are identified as significant coefficients and they  
 225 are added to the list of coefficients to be refined.

226 This algorithm also works by bit planes. The Bits sent during the significance pass correspond to  
 227 the program executed at the encoder during the execution of the classification algorithm of significant  
 228 and insignificant coefficients. By following the same program, the decoder remains synchronous with  
 229 the decisions of the encoder and finds the same classification.

230 In each pass of SPIHT, the only wavelet coefficients are encoded with magnitudes exceeding a  
 231 certain halved threshold values where is defined as:

$$232 \quad T_p = 2^n, n = \log_2 \left[ \max_{(i,j)} |c(i,j)| \right] \quad (2)$$

233 Where:

234  $p = 0, 1, \dots, P$  denote the number pass

235  $c(i, j)$  is the coefficient at position  $(i, j)$  in frame.

236 The coefficients sets are ordered in spatial orientation trees, with roots in the lowest frequency  
 237 subband.

238 The following is the three descending nodes set to correspond to wavelet coefficients at  
 239 coordinates  $(i, j)$ :

- 240 • Offspring set denoted by  $O(i, j)$  in the same spatial orientation. Except for lowest level
- 241 nodes that have four offspring.
- 242 • Type A set denoted by  $D(i, j)$ .
- 243 • Type B set (excluding the offspring) denoted by  $L(i, j) = D(i, j) - O(i, j)$ .

244 The resulting bandelet coefficients are ordered according to the its test of significance and  
 245 stored in three separate sets of lists: list of insignificant sets (LIS), list of insignificant pixels (LIP)  
 246 and list of significant pixels.

247 During the initialization step, added pixels to LIP are tested, added descendants sets to LIS are  
 248 sequentially assessed and significant pixels are stored in initial empty list LSP.

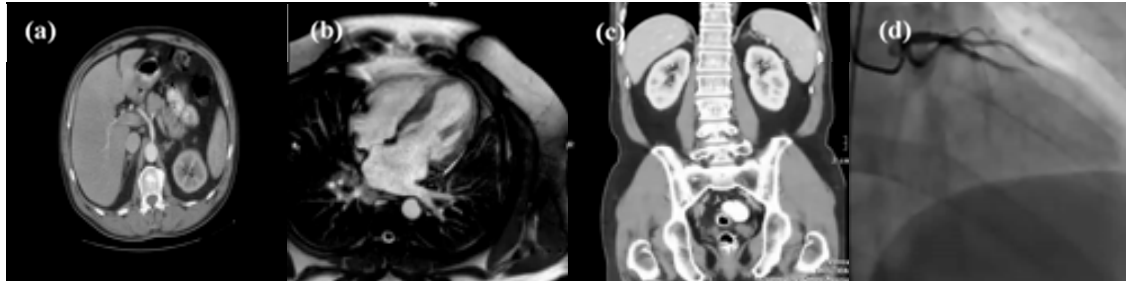
249 The coding operation being with LIP, if pixels are insignificant, it stays in LIP; otherwise, pixels  
 250 moved towards LSP.

251 Also for LIS, insignificant pixels stay in LIS. The significant pixels are divided into significant  
 252 A-type set where will be divided into B-type set and four pixels; type B set is added to the end  
 253 of LIS, while the remainders are examined for significance.

254 The principal proposed coding method is formulated as follows:

- 255 • Step1: Medical videos input
- 256 • Step2: Performing 2D discrete wavelet transform to decompose sequences into a subband.

- 257 • Step3: Decompose the frame recursively into the equal squares  
 258 • Step4: The geometric flow is applied to the each square.  
 259 • Step5: Warping the discrete wavelets along the geometric flux.  
 260 • Step6: Perform the 1D discrete wavelet transform to bandelize the wavelet bases.  
 261 • Step7: SPIHT encoded the resulting bandelets coefficients.  
 262



263 **Figure 5.**Medical video used for assessment

264 (a) Bladder cancer; (b) Heart; (c) Abdomen/Pelvis; (d) Coronary angiography.

- 265  
 266  
 267 • Step8: Gauging the quality of the recovered video sequences according to both  
 268 objective and subjective criterions.  
 269

## 270 4. Experimental results

271 We proposed in this work, a new algorithm for medical video coding based on the bandelet  
 272 transform coupled by SPIHT coder that detect complex geometric and reduce different existing  
 273 redundancy in video.

274 The accuracy of the algorithm is tested in a bit-rate range varies from 0.1 to 0.5Mbps on some  
 275 sized medical video sequences; each sequence has variable number of frames, and frame rate equal to  
 276 29.97 frames/second. The set tested medical videos are illustrated in Figure 5.

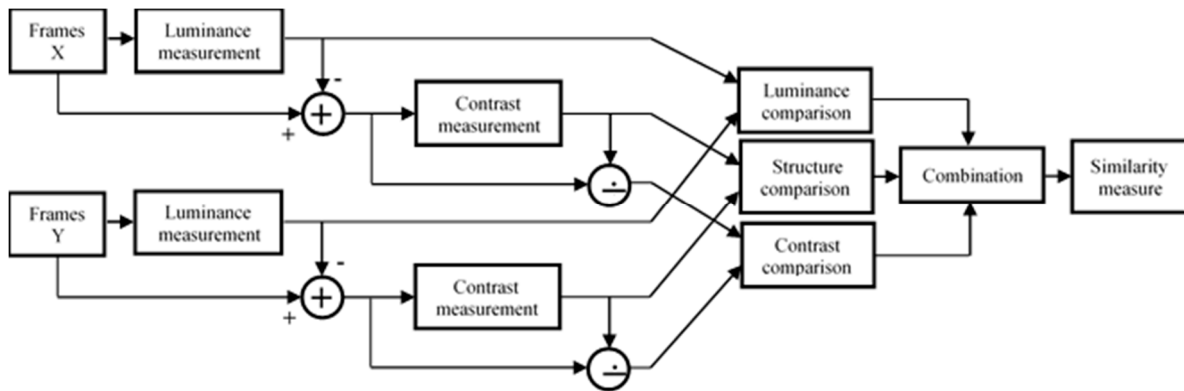
277 The perceived quality of recovered frames has been measured. Moreover, a comparison between  
 278 Bandelet-SPIHT and the wavelet transform using SPIHT encoder, MPEG-4, and H.26x, showed  
 279 promising results.

### 280 4.1. Warped wavelet along geometric flows

281 The characteristic of the multimedia services quality is summarized in a single term of the quality  
 282 of the experience [26-27], especially, with the appearance of digital video coding, storage, and  
 283 transmission systems and their fundamental limitations in the measuring the quality of video.

284 The National Telecommunications and Information Administration (NTIA) is one of the  
 285 pioneered organizations were it general models for estimating video quality [28], it is adopted with  
 286 the American National Standards Institute (ANSI) and included in The International  
 287 Telecommunication Union (ITU) as a normative method [29]. Also, this domain recognized other  
 288 organizations were having performed major research efforts [30-31].

289 The objective metrics are used to judge the performance of proposed algorithm and the higher quality  
 290 of the reconstructed frames is measured [32-34].  
 291



292  
293 **Figure 6.** Block diagram of the SSIM measurement system

294 The peak signal-to-noise ratio (PSNR) represents an objective evaluation parameter for the  
295 measurement of image quality, is defined as follows:

$$296 \quad PSNR = 10 \log_{10} \left( \frac{(2^n - 1)}{MSE} \right) \quad (2)$$

297 where

298 •  $(2^n - 1)$  is the dynamic of the signal (the maximum possible value for a pixel). In the  
299 standard case of an image where the components of a pixel are coded on  $n = 8$  bits,  $(2^n - 1) = 255$ .

300 • MSE represents the mean square error between two frames, namely the original frame and  
301 the recovered frame of size and is given by

$$302 \quad MSE = \frac{1}{MN} \sum_{i=1}^M \sum_{j=1}^N (f(i, j) - f_r(i, j))^2 \quad (3)$$

303 The PSNR is an easy, fast and very popular quality measurement metric, widely used to compare the  
304 quality of video encoding and decoding. Although a high PSNR generally means a good quality  
305 reconstruction, but this is not always the case. Indeed, PSNR requires original image for comparison,  
306 but this may not be available in every case, also PSNR does not correlate well with subjective video  
307 quality measures, so is not very suitable for perceived visual quality [35]. Hence, the interest in  
308 considering a measure of structural similarity (SSIM) adapted to the human visual system. SSIM  
309 index introduces three key features: luminance contrast and structure This metrics is defined in (4)  
310 and the block diagram of the SSIM measurement system is represented in Fig 6:

$$311 \quad l(x, y) = \frac{2M_x M_y + C_1}{M_x^2 + M_y^2 + C_1} \quad (5)$$

312 where

313  $M_x$  and  $M_y$  are the mean intensity of the signal  $x$  and  $y$  defined by  $M_x = \frac{1}{N} \sum_{i=1}^N x_i$  and

314  $M_y = \frac{1}{N} \sum_{i=1}^N y_i$  respectively.

315  $C_i = K_i^2 D^2$ ,  $i = 1, 2$ , and  $K_i$  is a constant, such as  $K_i \ll 1$  and  $D$  is the dynamic range of the pixel values

316 ( $D = 255$  corresponds to a grey-scale digital image when the number of bits/pixel is 8).

317 The contrast comparison function  $c$  takes the following form:

$$318 \quad c(x, y) = \frac{2\sigma_x \sigma_y + C_2}{\sigma_x^2 + \sigma_y^2 + C_2} \quad (6)$$

319 where

$$320 \quad \sigma_x = \left( \frac{1}{N-1} \sum_{i=1}^N (x_i^2 - (M_x)^2) \right)^{1/2}$$

321 The structure comparison function  $s$  is defined as follows:

$$s(x, y) = \frac{\sigma_{xy} + C_3}{\sigma_x \sigma_y + C_3} = \frac{\text{cov}(x, y) + C_3}{\sigma_x \sigma_y + C_3} \quad (7)$$

$$C_3 = \frac{C_2}{2} \text{ and } \text{cov}(x, y) = M_{xy} - M_x M_y$$

$$\text{with } M_{xy} = \frac{1}{N-1} \sum_{i=1}^N x_i y_i$$

Hence, the explicit expression of the structural similarity (SSIM) index is:

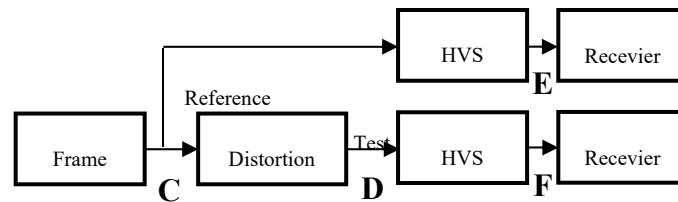
$$\text{SSIM}(x, y) = \frac{(2M_x M_y + C_1)(2\sigma_{xy} + C_2)}{(M_x^2 + M_y^2 + C_1)(\sigma_x^2 + \sigma_y^2 + C_2)} \quad (8)$$

where

$$\sigma_{xy} = \left( \frac{1}{N-1} \sum_{i=1}^N (x_i y_i)^2 - (M_{xy})^2 \right)^{1/2}$$

Generally, over the whole video coding, a mean value of SSIM is required as Mean SSIM (MSSIM):

330



331

332 **Figure 7.** Diagram of the visual information fidelity (VIF) metric.

$$\text{MSSIM}(f, f_r) = \frac{1}{L} \sum_{i=1}^L \text{SSIM}(f_i, f_{ri}) \quad (9)$$

333

334 where and are the contents of frames (original and recovered respectively) at the  $i$ th local  
335 window (or sub-image), and is the total of local windows number in frame.

336 The MSSIM values exhibit greater consistency with the visual quality.

337 In 2006, Sheikh and Bovik [36] proposed a new paradigm for video quality assessment: information  
338 video fidelity (VIF). This criterion quantifies the Shannon information that is shared between the  
339 original and recovered images relatively to the contained information in the original image itself. It  
340 uses natural scene statistics modelling in conjunction with an image-degradation model and a human  
341 visual system (HVS) model.

342 Visual Information Fidelity uses the Gaussian scale mixture model (GSM) in the wavelet domain. To  
343 obtain VIF one performs a scale-space-orientation wavelet decomposition using the steerable pyramid  
344 and models each subband in the source as  $C = SU$ , where is a random field of scalars and is a  
345 Gaussian vector.

346 The distortion model is where is a scalar gain field and is an additive Gaussian noise.

347 VIF then assumes that the distorted and source images pass through the human visual system  
348 and the HVS uncertainty is modelled as visual noise and for the source and distorted image  
349 respectively.

350 The model is then:

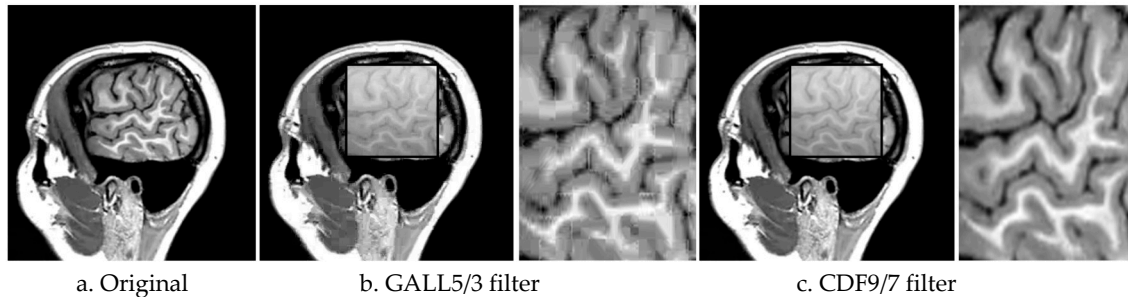
$$\text{Reference signal} \quad E = C + N \quad (10)$$

$$\text{Test signal} \quad F = D + N \quad (11)$$

353 Where  $E$  and  $F$  denote the visual signal at the output of the HVS model from the reference and  
354 the test videos respectively, from which the brain extracts cognitive information.

355 The VIF measure takes values between 0 and 1, where 1 means perfect quality and is given by:

$$356 \quad VIF = \frac{\sum_j I(C^j; F^j / s^j)}{\sum_j I(C^j; E^j / s^j)} \quad (12)$$



357  
358

359

**Figure 8. Recovered frames using:**

360

(b). Bandelet(GALL5/3)-SPIHT and (c). Bandelet(CDF9/7)-SPIHT at 0.2Mbps.

361

where,  $I(X;Y/z)$  is the conditional mutual information between  $X$  and  $Y$ , given  $z$ ;  $C$  denotes the

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random field from a channel in the original image,  $s^j$  is a realization of  $S^j$  for a particular image and

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the index  $j$  runs through all the sub bands in the decomposed image.

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#### 4.2. Choice of the perfect filter and transform

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In this part, MRI video is encoded with performing of the Bandelet-SPIHT algorithm for various  
366 bit rates. Pixels resolution MRI images is made using different filters, where each with its own  
367 peculiar properties (filter orders, symmetry and compact support) has been investigated. In order to  
368 find the best objective measures filter for video compression, the pioneer biorthogonal families was  
369 considered, thus the wavelets CDF9/7 (Cohen-Daubechies-Feauveau) and GALL5/3 (GENERATING  
370 ANY LEVELS LE) are used, they part of the family of symmetric biorthogonal wavelets CDF.

371

The choices of these filters are for their simplicity, symmetry and for the support width. CDF9/7  
372 and GALL5/3 are characterized with  $(9/7, 2)$  and  $(5/3, 4)$ , respectively.

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where  $(I/J, K)$ ,  $I/J$  and  $K$  showing the number of coefficients in decomposition low-pass filter  
374 (analysis)/ reconstitution high pass filter (synthesis) and number of vanishing moments [37-40].

375

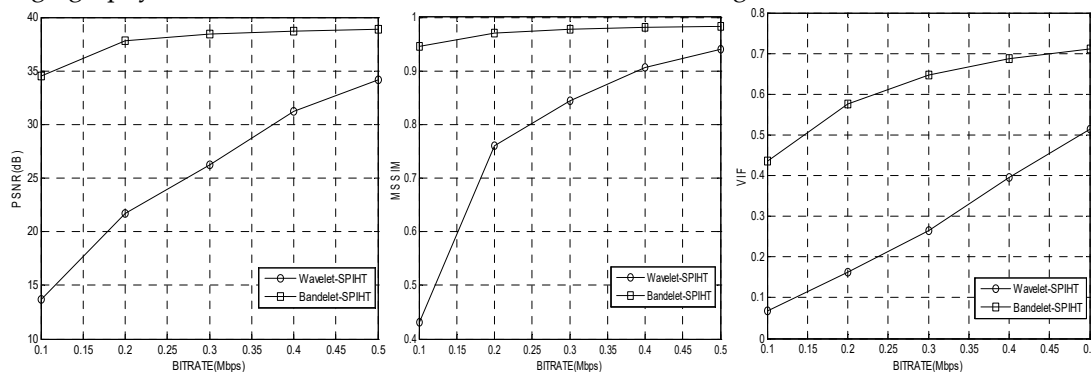
After an accurate visual inspection of the images in Figure 8, we adopt the bi-orthonormal  
376 wavelets CDF9/7 rather GALL5/3 to reduce the artifacts levels. The results obtained show that the  
377 visual quality of the recovered frame using the Bandelet algorithm (CDF9/7) + SPIHT is close to the  
378 original frame.

379

On the other hand, we notice a presence of fuzzy areas in the case of the use of GALL5/3 filter,  
380 which is arduous to detect by a simple observation.

381

Comparative results between (Bandelet+SPIHT) algorithm and (Wavelet +SPIHT) applied to coronary  
382 angiography test frame at various bit rates are illustrated in Figure9.

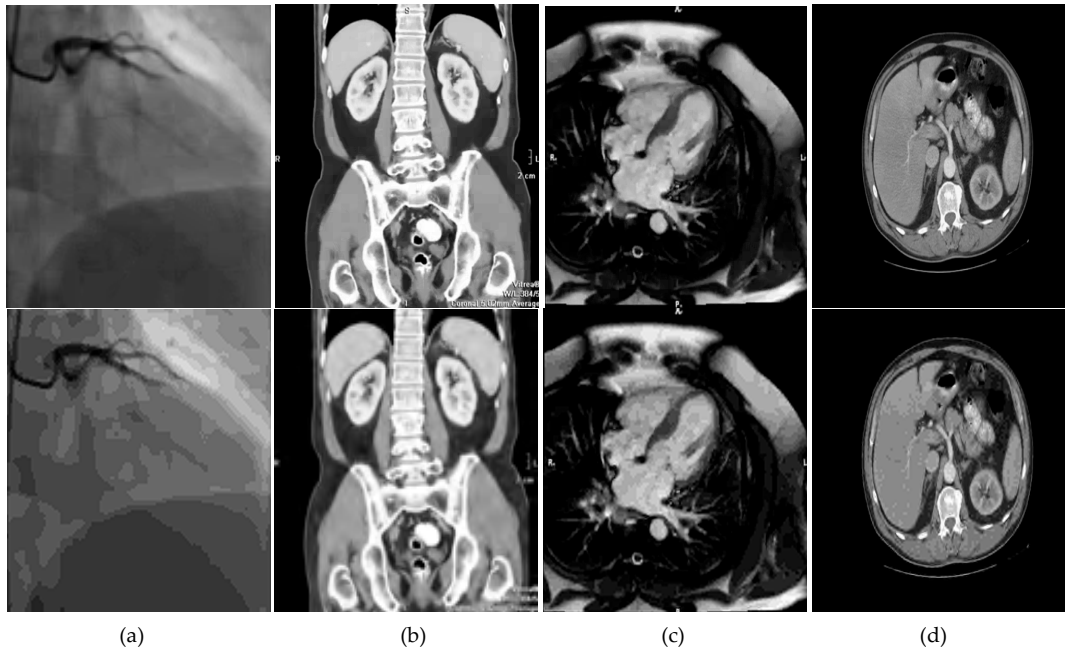


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**Figure 9.** Performance evaluation of Bandelet-SPIHT versus (Wavelet) SPIHT in terms of objective parameters.

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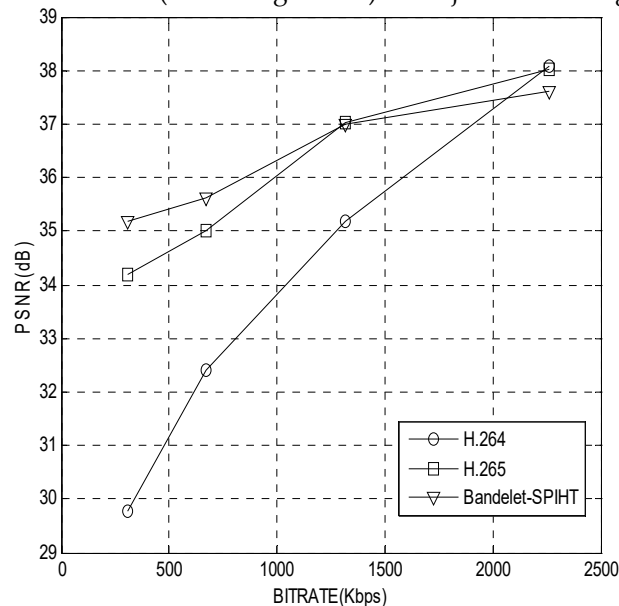
395

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**Figure 10.** Comparative quality assessments medical video using Bandelet(CDF9/7)-SPIHT (Top row), and Wavelet(CDF9/7)-SPIHT (Bottom row) at 0.5 Mbps

Figure 10, shows the visual results for tested medical video. From this figures, it is clearer that the performance of (Bandelet+SPIHT), indicates that our algorithm gives best results compared to the conventional and state-of-the art coding methods and it is an apt tool to detect all special complex geometric.

While the discrete wavelet transform (SPIHT algorithm) is subject to blocking artifacts



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**Figure 11.** Comparison PSNR (dB) between the existing coding standards and proposed coding method

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#### 4.3. Bandelet-SPIHT versus standards encoder comparison

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To check and prove the efficiency of the algorithm, more comparison with H.26x and MPEG standards are required. The H.264 and H.265 are known standards especially in the security industry. It is interesting to examine the maximum PSNR (dB) at the output of the proposed algorithm. As illustrated in Figure 11, the proposed method demonstrates its relatively better performance compared to the standard video coding H.264 and H.265 in terms of PSNR. For example, under 2Mbps it is clearly seen that the PSNR curves of the proposed algorithm is significantly outperformed

406 to the conventional standards encoders. Furthermore, for low bit rates (e.g. 1Mbps) our method can  
407 exceed H.264 and H.265 encoders by 2.41 dB and 0.23 dB respectively. Moreover, the PSNR  
408 improvements are more significant in high values.

## 409 5. Conclusion

410 The objective motivating our study was to propose a coding method with high performances in  
411 terms of visual quality and PSNR at low bit rates. Bandelets using SPIHT encoder is an effective  
412 candidate meeting the specific requirements of our application in the medical field and particularly in  
413 medical imaging where the quality of the image at low bit rates is a major requirement for the  
414 practitioner.

415 In order to show the efficiency of Bandelet-SPIHT algorithm, a set of medical sequences as test  
416 examples is considered. At low bit rates, Bandelet-SPIHT algorithm gives significantly better results  
417 (PSNR and visual quality) comparing to some cutting-edge coding techniques such as H.26x family  
418 (namely H.264 and H.265).

419 From this point of view, the expected goal is achieved and the prospects for application in  
420 medical imaging are promising.

421 Geometric image compression methods are a very dynamic search direction. One could mention  
422 the construction of transformations that adapt automatically to the geometry without the need to  
423 specify it or discrete geometry approaches ... They all agree, however, that geometry is the key to  
424 significantly improve current compression methods.

425

426 **Author Contributions:** Methodology, Abdeldjalil Ouahabi; Project administration, Abdelmalik Taleb-Amed;  
427 Software, Merzak Ferroukhi and Yacine Habchi; Supervision, Mokhtar Attari; Validation, Mohamed  
428 Beladgham.

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