

*Article*

# Spatio-Temporal Visualisation of Reflections from Building Integrated Photovoltaics

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**Abstract:** With the increasing adoption of building integrated photovoltaics (BIPV), concerns arise about potential glare. While recommended criteria to assess glare exist, it is challenging to apply these in the spatial and temporal domains and communicate the complex data to planning authorities and clients. This paper presents a new computational workflow using annual daylight simulation, material modelling using bi-directional scattering distribution functions (BSDFs) and image-based postprocessing to obtain 3-dimensional renderings of cumulative annual irradiance and glare duration on the built environment. The annual daylight simulation considers relevant sun positions in high temporal resolution (15-minute timesteps) and measured BSDFs to model different PV materials. The postprocessing includes a relative irradiance visualisation comparing the impact of a proposed PV proportional to a reference material. It also includes a new spatio-temporal workflow to assess the glare duration based on recommended thresholds. This workflow is demonstrated with a case study of a proposed PV roof for a church, assessing the glare potential of two different PV materials. The visualisations indicate glare durations well below the thresholds with satinated PVs, and in noncritical zones outside observer positions with standard PVs. Thus the proposed PV roof does not cause any disturbing glare.

**Keywords:** Building integrated photovoltaics; annual daylight simulation; reflection; RADIANCE; photon mapping; BSDF; HDR; image processing; feature detection

## 1. Introduction

The integration of photovoltaics (PV) into building façades as building integrated photovoltaics (BIPV) holds opportunities in meeting the increasing demand for renewable energy. BIPV significantly improves the energy balance of buildings and their autonomy. The dramatic cost reduction in recent years along with a diversity in available designs have motivated the increasing use of BIPV. The appearance of BIPV corresponds to that of glass façades, as PV modules are typically laminated with glass. This has in turn influenced the development of urban architecture, with a shift from traditional construction materials such as plaster or fibre cement towards an increasing prevalence of glass façades in general, and BIPV in particular.

A negative side effect of this development are potentially disturbing reflections from specular façades, which pose a challenge for building and environmental authorities [1]. Specular reflections are problematic because they may give rise to glare, which impacts occupants in adjacent buildings as well as pedestrians, but also personell in critical environments such as airports [2]. A high luminance in the observer's field of view, particularly in contrast to indoor luminance, can result in discomfort glare as the eye strains to accommodate the contrast, leading to rapid fatigue. In severe cases where the luminance is high enough to cause temporary visual impairment and after-images on the retina, this results in disability glare. Glare is highly subjective, and there is considerable variation in tolerance among individuals. As such, glare is typically expressed as a probability index rather than fixed metric thresholds [3].

**Table 1.** Nomenclature and symbols used in this paper.

Acronyms	
BAFU	Swiss federal environmental agency (Bundesamt für Umwelt)
BIPV	Building Integrated Photovoltaics
BSDF	Bidirectional Scattering Distribution Function
HDR	High Dynamic Range
LAI	German federal/state association for pollution control (Bund/Länder-Arbeitsgemeinschaft für Immissionsschutz)
PV	Photovoltaics
RPG	Swiss federal spatial planning law (Bundesgesetz über die Raumplanung)
RPV	Swiss federal spatial planning ordinance (Raumplanungsverordnung)
RADIANCE Tools	
<i>falsecolor</i>	Applies linear or logarithmic falsecolour scale to HDR image
<i>genbsdf</i>	Generates BSDF from measured data as XML file
<i>gensky</i>	Generates sky model for given date/time/location (solar position + optional sky dome)
<i>mkpmap</i>	Forward raytracer, generates photon map
<i>oconv</i>	Generates simulation model as octree (sky + geometry + materials)
<i>pcomb</i>	Modifies/filters HDR image pixels
<i>pcompos</i>	Composites multiple HDR images
<i>pcond</i>	Tone maps or adjusts exposure of HDR image
<i>rcalc</i>	Field-based calculator
<i>rcontrib</i>	Source/timestamp contribution raytracer, computes time-series irradiance from photons
<i>rtrace</i>	General backward raytracer, computes cumulative irradiance from photons
<i>vwrays</i>	Generates primary rays for a given viewpoint to pass into raytracer
Parameters [Units]	
DoY ( $\Delta$ DoY)	Day of Year (resp. increment) [d]
HoD ( $\Delta$ HoD)	Hour of Day (resp. increment) [h]
$\tau_A$	Maximum area of PV [ $\text{m}^2$ ]
$\tau_d$	Maximum distance to PV [m]
$\tau_L$	Maximum reflected luminance from PV [ $\text{cd}/\text{m}^2$ ]
$\tau_E$	Maximum irradiance on receiver from PV [ $\text{W}/\text{m}^2$ ]
$\tau_t$	Maximum sustained glare duration on any day of the year [h]
$\tau_T$	Maximum cumulative glare duration per year [h]

37 Consequently there is a demand for criteria to objectively assess the impact of specular reflections  
 38 in architecture, and take countermeasures if necessary. As these countermeasures can be costly,  
 39 legislation is required to prevent such situations from arising by applying the assessment criteria when  
 40 authorising a planned PV installation.

41 Well-known examples of problematic reflections from specular building façades include the  
 42 Vdara Hotel & Spa in Las Vegas and the “Walkie-Talkie” building in London [4], both of which feature  
 43 concave façades and required remedial measures such as applying a non-reflective film to the specular  
 44 surfaces. Another example is the Walt Disney Concert Hall in Los Angeles, whose exterior was sanded  
 45 down to mitigate reflection [5].

46 Documented examples of glare specifically from PV reflection include the installation at the  
 47 Manchester-Boston Regional Airport, which resulted in extremely disabling glare directed towards the  
 48 control tower [6]. An analysis conducted by the Massachusetts Institute of Technology (MIT) [2]  
 49 concluded that the existing guidelines issued by the FAA (U.S. Federal Aviation Authority) for  
 50 evaluating PV at airports are vague and do not consider the sun’s variable position over the year. The  
 51 situation was remedied by reorienting the modules by  $90^\circ$ .

52 Cases of PV reflection in residential settings are more sparsely documented, and often regional  
 53 in scope. A number of legal settlements over instances of PV glare are summarised by Bohren [7],  
 54 revealing varying interpretations of the existing legislation governing PV installations in Germany.

55 Similarly, an ongoing neighbourly dispute over glare from a solar thermal collector reveals the  
56 inadequacy of the relevant legislation currently in place in Switzerland [8,9].

## 57 2. Background

### 58 2.1. Current Legislation

59 The acceptance of BIPV by architects, authorities and communities requires a high degree of  
60 flexibility in design, and a form of governance that limits specular reflections from façades. Currently  
61 there is infact a surprising dearth of specific legislation to regulate these potentially disturbing or even  
62 disabling effects.

63 In Switzerland, BIPV in façades and areas of the building envelope except the roof are subject to  
64 mandatory approval by building and environmental authorities. Roof-mounted PV that is “adequately  
65 adapted” in compliance with article 18a of the federal spatial planning law (Bundesgesetz über die  
66 Raumplanung, RPG [10]), is exempt from authorisation. The RPG is implemented for PV installations  
67 according to Article 32a of the federal spatial planning ordinance (Raumplanungsverordnung,  
68 RPV [11]), which states that roof-mounted PV should (a) appear as homogeneous surface, (b) be  
69 of low reflectance in accordance with the state of the art, and (c) not overhang the roof edges.

70 An informal survey was conducted by the authors with building authorities in four Swiss Cantons  
71 (Bern, Basel, Neuenburg/Neuchâtel and Zürich) to determine whether specific requirements for glare  
72 protection from BIPV have been established locally. The survey revealed that none of the regional  
73 authorities currently enforce definite criteria for PV installations beyond those cited in the RPV, and in  
74 particular no specific parameters to identify potential glare from reflections.

75 The Swiss federal environmental agency (Bundesamt für Umwelt, BAFU) has issued a draft  
76 proposal that regulates emissions from artificial lighting and reflections from building façades as  
77 well as PV installations, but does not specify actual limits for glare [12]. Infact, the current proposal  
78 recommends that, if in doubt, the decision on whether a particular reflection is tolerable or not should  
79 be based on subjective expert opinion during an on-site inspection.

### 80 2.2. Current Technical Guidelines and Assessment Criteria

81 A recent review on the problem of reflections from building façades was published in [1], which  
82 proposes using glare impact categories as criteria for assessing the reflections. However, the criteria are  
83 entirely subjective, and not photometrically quantified. It does, on the other hand, propose radiometric  
84 limits to quantify the thermal impact of reflections.

85 Some technical guidelines to assess light emissions (direct or reflected) have been issued by  
86 government agencies [12,13] and trade associations [14]. These guidelines primarily cover the relevant  
87 photometric theory and practice (including instrumentation), as well the detrimental effects of light  
88 pollution on the environment. Sections specifically dedicated to PV installations define separate  
89 criteria for residential and commercial settings, where sensitivities tend to differ. These sections also  
90 recommend countermeasures such as (a) occluding the PV with natural barriers such as vegetation,  
91 (b) reorienting the modules, or (c) using PV with low reflectance, e.g. laminated with satinated  
92 frontglass.

93 While the guidelines do mention specific photometric criteria and limits for assessing glare from  
94 light emissions, these are intended as *recommendations* rather than standards for compliance, and this  
95 is explicitly stated. This inherent tolerance can be largely attributed to the highly subjective nature  
96 with which individuals perceive reflection as glare.

97 The German federal/state association for pollution control (Bund/Länder-Arbeitsgemeinschaft  
98 für Immissionsschutz, LAI) has issued a report with guidelines to measure, assess, and reduce light  
99 emissions [13]. This document explicitly states recommendations, quantifies influencing factors and  
100 mentions specific parameters to assess critical emissions from artificial lighting and building façades.

**Table 2.** Recommended PV reflection assessment criteria and thresholds.

Parameter, critical condition	Description	Threshold value	Units
$< \tau_d$	Distance to PV	50 (commercial) 100 (residential)	m
$> \tau_A$	Area of PV	100 (commercial) 10 (residential)	m <sup>2</sup>
$> \tau_\omega$	Angle subtended by PV at receiver	7.5	° (degrees)
$> \tau_L$	Reflected luminance from PV	30 (MIT) 50 (Swissolar)	kcd/m <sup>2</sup>
$> \tau_E$	Irradiance from PV at receiver	10 (Sandia Labs) $\approx 16.8$ (MIT) 30 (Swissolar)	W/m <sup>2</sup>
$> \tau_t$	Maximum sustained glare duration on any day of the year	30	min
$> \tau_T$	Cumulative glare duration per year	50	hours

101 On the basis of [13], Swissolar has issued a guideline with specific criteria relevant to PV  
 102 installations for practitioners [14]. These criteria, together with their recommended thresholds, are  
 103 summarised in Table 2. Note that multiple critical conditions (as defined by exceeding the relevant  
 104 threshold) reinforce the likelihood of glare. The most pertinent of these criteria in assessing potential  
 105 glare is the reflection luminance, with the irradiance on a receiver due to reflection as complementary  
 106 criterion.

107 Swissolar recommends an irradiance threshold of 30 W/m<sup>2</sup> for reflections based on a theoretical  
 108 maximum direct normal irradiance of ca. 800–1000 W/m<sup>2</sup> at medium altitude (typically higher on  
 109 an inclined PV panel) and a reflectance of ca. 3–4%<sup>1</sup>. However, an analysis of glint and glare from  
 110 solar power plants conducted by Sandia National Laboratories [15] reports that a solar irradiance of  
 111 only 1–10 W/m<sup>2</sup> at the eye can already lead to temporary blindness and afterimages. This analysis  
 112 was based on retinal irradiance metrics collated from experimental data. Glint constitutes short-term  
 113 glare that can be particularly hazardous to air and ground traffic, with recovery times for the aforesaid  
 114 irradiance range lasting 0.8 to 12 seconds in experiments.

115 Furthermore, an analysis of disability glare at an airport conducted by the Massachusetts Institute  
 116 of Technology (MIT) [2] proposes a reflected luminance threshold of  $\tau_L = 30$  kcd/m<sup>2</sup>. This limit is  
 117 based on the assumption that the eye can accommodate a luminance range of up to two orders of  
 118 magnitude, given an average indoor luminance of 300 cd/m<sup>2</sup>. Using the retinal irradiance metric  
 119 defined by Sandia National Laboratories [15], the authors concluded that this luminance is likely to  
 120 cause after-images. Assuming a luminous efficacy of 179 W/m<sup>2</sup> [16], a reflective PV surface area  
 121  $\tau_A = 10$  m<sup>2</sup> and a distance of  $\tau_d = 100$  m for a residential setting according to Table 2, the proposed  
 122 luminance threshold corresponds to an approximate irradiance threshold of  $\tau_E \approx 16.8$  W/m<sup>2</sup>. This,  
 123 like the limits reported by Sandia National Labs, lies well below the theoretical threshold proposed by  
 124 Swissolar.

125 To reinforce the presented analysis, the luminance resp. irradiance thresholds recommended  
 126 by MIT and Sandia National Laboratories are included in Table 2. In consideration of the above  
 127 evidence, and the fact that these thresholds were experimentally derived rather than rooted in theory,  
 128 an additional, more conservative irradiance threshold  $\tau_E = 10$  W/m<sup>2</sup> is applied in assessing the case  
 129 study simulations to complement the 30 W/m<sup>2</sup> recommended by Swissolar.

<sup>1</sup> Personal communication with Peter Toggweiler, Senior Technical Consultant for Basler & Hoffmann, Zürich, 27.03.2018.

### 130 2.3. PV Reflection Simulation

131 Reflections from PV are transient in time and space over the course of a year, and thus difficult  
132 to predict. A reliable annual prediction on the basis of computational simulation can therefore  
133 complement the practitioner's experience in selecting a candidate PV installation. Ideally, this analysis  
134 should be applied in the pre-project planning phase of a PV proposal to identify potentially disturbing  
135 reflections at an early stage. The results can then lead to adjustments to the project while still in  
136 the planning phase. In addition, authorities issuing building permits can base their decisions on the  
137 analysis. This avoids incurring additional expenses for subsequent adjustments in the course of the  
138 project, or additional consultancy for more elaborate reflection analyses.

139 There are few documented instances of simulation workflows and tools to specifically assess  
140 PV reflection, and they have all been developed in the context of aviation. Jakubiec and Reinhart [2]  
141 performed an analysis of disability glare from a PV installation at an airport, reporting reflected  
142 luminance levels in excess of 250 kcd/m<sup>2</sup> impacting the control tower. These measurements were  
143 used to validate an annual simulation of reflected luminance using the RADIANCE lighting simulation  
144 software suite [16]. An analytical reflection model of the PV module surface was derived from  
145 spectrophotometric measurements and HDR photographs of a sample at oblique viewing angles.  
146 Based on their results and a proposed luminance threshold, the authors were able to predict the  
147 monthly glare duration.

148 Fraunhofer FIT developed an interactive system specifically to analyse glint and glare from PV  
149 at airports [17]. At the time of writing, this system only considered total specular reflection using  
150 an analytical BSDF model, ignoring the potentially significant diffuse component. Furthermore, the  
151 system does not consider the topography of the built environment (which is typically flat around  
152 airports), nor any of the abovementioned recommended thresholds in its assessment.

153 The sophisticated Solar Glare Hazard Analysis Tool (SGHAT) developed by Sandia National  
154 Laboratories [18] offers a convenient web-based interface using the Google Maps API. The user  
155 can select a region populated by PV superimposed on satellite imagery and adjust a multitude of  
156 parameters, such as PV tilt, orientation, elevation, and reflectance. The user must then select fixed  
157 observation points, for which the tool generates annual glare occurrence plots in three categories –  
158 including permanent eye damage – according to the retinal hazard metrics collated by Sandia Labs [15].  
159 Like Fraunhofer's system, SGHAT is primarily aimed at air traffic and satisfies FAA requirements.  
160 Unfortunately the tool is now restricted to military, state, and federal government users only, and its  
161 support ended in 2017. The SGHAT software is currently being licensed by Sims Industries as part of  
162 their ForgeSolar PV glare analysis toolset [19], which incorporates many of the aforesaid features and  
163 is available to registered users.

164 The PV reflection analysis workflow proposed in this paper primarily builds on earlier work  
165 by Yang [20], which applied forward raytracing and simplified density estimation techniques to  
166 locate reflections from a building façade on a 3D model of its surrounding built environment. This  
167 was implemented on a parametric design platform comprised of *Rhino* and *Grasshopper*. While the  
168 workflow proposed herein also leverages forward raytracing and density estimation, it does so in  
169 the unified context of RADIANCE and its photon mapping extension [21]. This work improves on the  
170 aforementioned simulation workflows by using data-driven BSDF models of the measured PV samples  
171 for a more accurate prediction of both specular and diffuse reflection. Furthermore, the proposed  
172 method benefits from the higher quality specular-diffuse reflections obtained with the photon map's  
173 forward raytracing algorithm.

### 174 3. Case Study

175 The PV reflection assessment workflow proposed in this paper is demonstrated on a case study  
176 of a PV retrofit of a church sited in Lucerne, Switzerland. The church of St. Michael was built in  
177 1967 by the architect Hanns A. Brütsch [22], an award-winning reformer of modern ecclesiastical  
178 architecture in Switzerland. The design of St. Michael is an example of *beton brut* creating sharp-edged



**Figure 1.** Aerial view of St. Michael's church with parish in foreground, looking northeast.

179 expressive building volumes with exposed concrete. The building encloses the patio with an entrance  
180 and gathering space while resembling a fortress from the street view. [Figure 1](#) shows the church in its  
181 current state in the context of its surroundings.

182 There are several large roof spaces, which were up for energy retrofit in 2010. But being an icon  
183 of *beton brut*, the church is a heritage protected site and as such, retrofit projects must maintain the  
184 original materials, construction and appearance. Initial applications to mount PV modules to some  
185 parts of the old roof were hence rejected by the municipal heritage board.

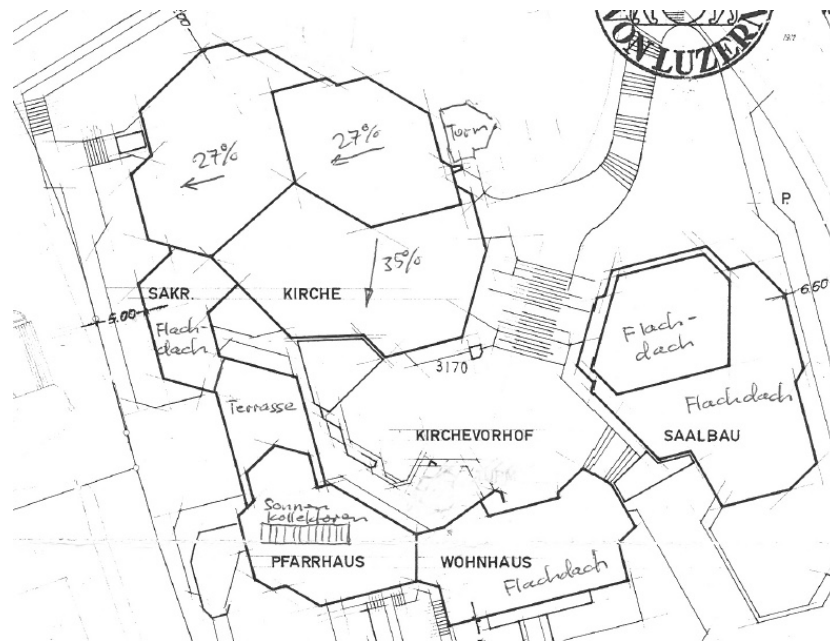
186 [Figure 2](#) shows the original site plan. The roof slopes annotated in handwriting indicate the roof  
187 sections identified for PV coverage. Two sections face west with a slope of 27%, while one section faces  
188 south with a slope of 35%. As such, the heritage board was concerned with disturbing reflections from  
189 the proposed roof sections. The proposed PV system installer visualised the zones potentially affected  
190 by reflections in [Figure 3](#) but could not make a conclusive verdict on the potential for glare. For this  
191 and other reasons, the project was put on hold.

192 A new attempt was made recently, in which the retrofit concept proposed to completely replace  
193 three larger roof sections with integrated photovoltaics. The PV roof shall visually maintain the small  
194 grained texture of the old roof tiles, and the construction details along eaves and verges shall follow  
195 the old dimensions, yet replace timber and fibre cement with metal and glass. In addition, the glare  
196 issue should be investigated by computational simulation to make informed decisions about zones  
197 and duration of potential glare, taking into account the material properties of different PV frontglass  
198 surfaces.

## 199 4. Simulation Methodology

### 200 4.1. Motivation

201 The primary objective of the proposed simulation methodology is to provide a visual prediction  
202 of potential glare zones in the context of the built environment around a planned BIPV installation.  
203 While luminance is generally the preferred criterion for identifying glare, it is unfortunately dependent  
204 on viewpoints facing the emitting building. These must be fixed for each simulation run, possibly



**Figure 2.** Original roof plan of St. Michael's church indicating slopes of each roof section.



**Figure 3.** Reflection zones and timespans from roof of St. Michael's church predicted by PV system installer for initially proposed PV roof retrofit. Image courtesy of BE Netz AG.

205 requiring multiple iterations. Viewpoint placement requires *a priori* knowledge or anticipation of  
206 where glare is likely to occur on behalf of the planner.

207 The irradiance on the built environment, on the other hand, can be rendered in one image to  
208 concisely convey areas of potential glare as seen from the emitting building. This provides an initial  
209 qualitative overview that fundamentally clarifies the presence or absence of potential glare as a first  
210 step in planning a PV installation. This saves the planner the burden of selecting observation points  
211 for a more comprehensive luminance analysis, e.g. in order to apply glare probability metrics. Such an  
212 analysis would then only be warranted for selected zones indicating potential glare.

213 The proposed approach is therefore entirely image-based, with irradiance resolved spatially and  
214 temporally as a time-series of rendered high dynamic range (HDR) images, which are referred to  
215 as *irradiance maps*. This time-series typically encompasses a simulated half-year due to analemmatic  
216 symmetry, and can be condensed into a single representative image, since a planner is generally not  
217 interested in assessing individual point-in-time data, but the aggregate annual result. The visualisation  
218 should therefore convey the latter by reducing the 3-dimensional spatio-temporal time-series to  
219 a 2-dimensional composite image. In doing so, the irradiance can be evaluated according to the  
220 recommended criteria in [Table 2](#) to identify glare and obtain the maximum sustained and cumulative  
221 glare durations per year, which are quantified with a falsecolour scale. Thus only the essential data  
222 is presented, making the visualisation suitable for non-expert clients and decision makers who may  
223 review the results during the building permit application process.

224 Because only PV reflections are to be assessed, irradiance from other sources – notably the direct  
225 component from the sun – is not falsecoloured, but composited into the visualisation in greyscale to  
226 aid in orientation and identify affected buildings in the environment. The proposed workflow follows  
227 from this, and the direct and PV reflection irradiance maps are rendered separately, with the latter  
228 falsecoloured before being composited with the former. More importantly, this also avoids false glare  
229 in panoramic views, since the sun paths are visible in the direct irradiance maps.

230 Each irradiance map in the time-series is rendered using RADIANCE in photon mapping mode.  
231 Because photon mapping traces rays from the light sources (suns) towards the receivers (built  
232 environment), it excels at simulating specular-diffuse transfers, or *caustics*. Depending on its specularity,  
233 the PV surface material can effectively redirect daylight towards the built environment as caustics.  
234 Photons are deposited and stored on the surrounding diffuse surfaces, and may be reused for  
235 subsequent renderings. The RADIANCE photon map also supports time-series renderings by tagging  
236 each photon with its emitting light source (sun position) [21].

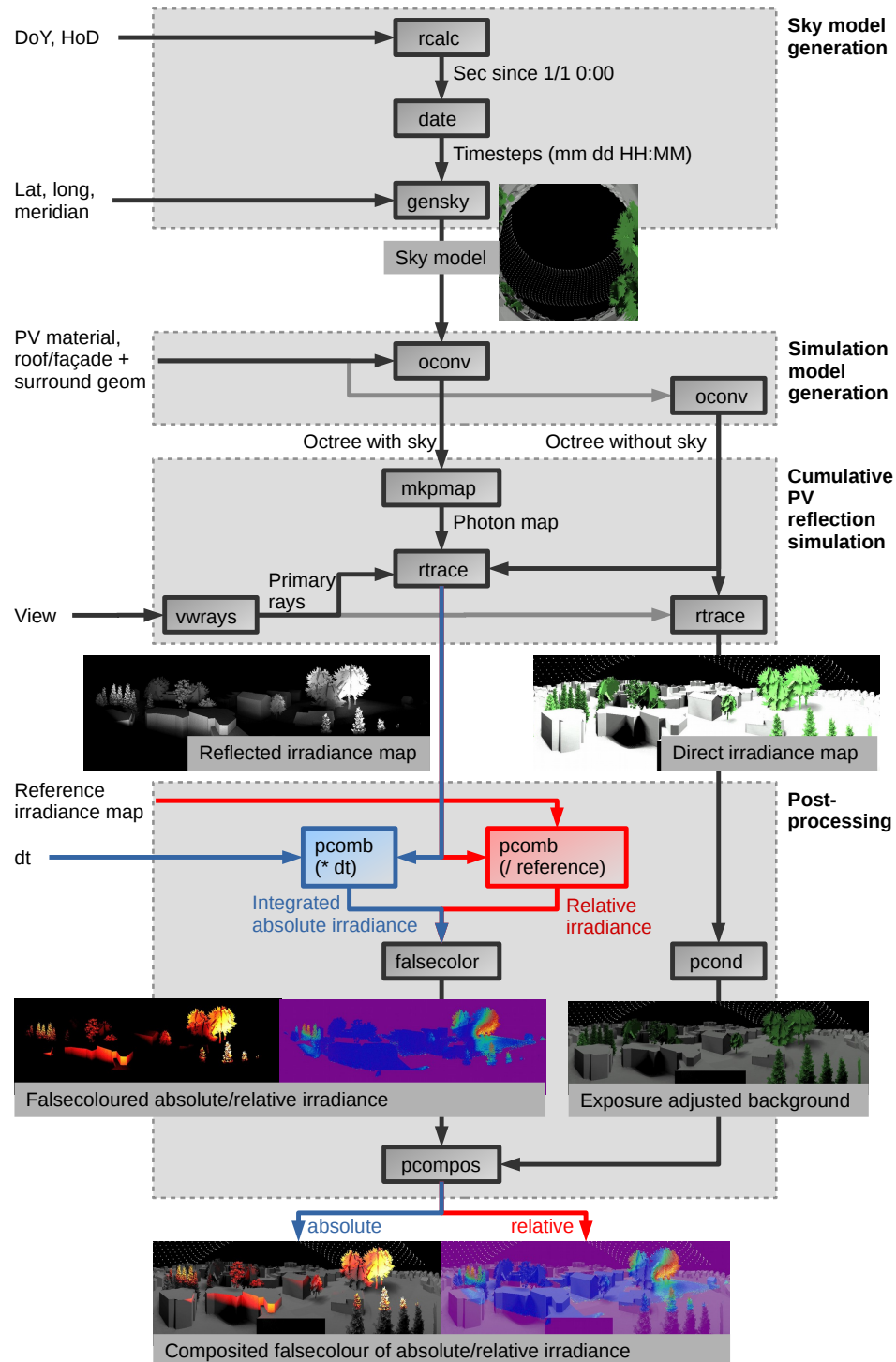
237 In addition to an efficient light transport algorithm, reliably predicting the irradiance reflected  
238 from PV also requires an accurate representation of the PV's reflecting behaviour. This is particularly  
239 important for standard PV modules with a glossy surface finish, which exhibit significant specular  
240 reflection. Consequently, the case study simulations use a data-driven representation derived from  
241 measurements of actual candidate PV samples.

#### 242 4.2. Workflow Overview

243 The proposed methodology consists of two workflows to visualise irradiance from PV reflection:  
244 a general workflow to assess cumulative annual irradiance, summarised in [Figure 4](#), and a  
245 spatio-temporal workflow to assess glare duration according to recommended criteria, summarised in  
246 [Figure 5](#). The latter builds on the former by using some of its output (photon map, simulation model,  
247 timesteps) and lies at the heart of the methodology.

248 Both workflows are managed in a UNIX Makefile which handles the multiple dependencies  
249 (corresponding to arrows in the flowcharts) and selectively runs individual components as targets. A  
250 separate simulation is run (technically an invocation of the Makefile) for each candidate PV material.

251 [Table 3](#) lists the simulation parameters chosen for the PV reflection case study. These coincide  
252 with the inputs shown on the left side of the general workflow overview in [Figure 4](#). The workflow  
253 components are detailed in the following subsections.



**Figure 4.** General PV reflection simulation workflow to assess cumulative annual irradiance.

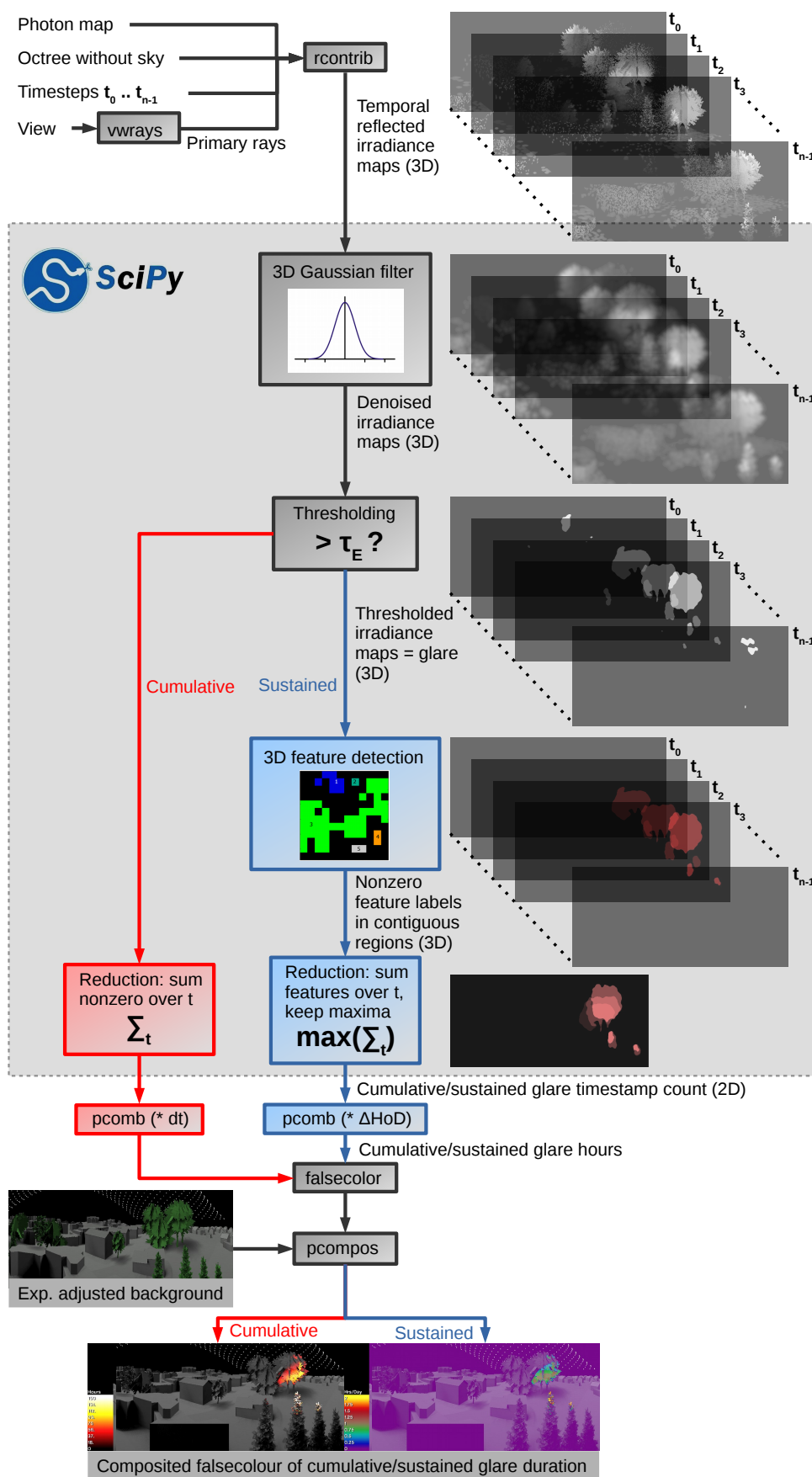


Figure 5. Spatio-temporal PV reflection simulation workflow to assess glare duration.

**Table 3.** Simulation parameters for PV reflection case study.

Parameter	Description	Value
DoY	Day of year	[0, 181]
$\Delta\text{DoY}$	Day of year increment	7
HoD	Hour of day	[4.5, 20.5]
$\Delta\text{HoD}$	Hour of day increment	0.25
$N_t$	Number of timesteps (sun positions)	1280
Lat, long	Site latitude, longitude	47.038°N, 8.312°E
Merid	Timezone meridian	15°E (CET)
$N_p$	Number of photons	250M
$n_p$	Photon lookup bandwidth	400 ( <i>rtrace</i> ), 4000 ( <i>rcontrib</i> )

### 254 4.3. General Workflow

255 The general workflow summarised in Figure 4 generates the timesteps, corresponding sky model  
 256 and octree for the simulation. Furthermore, it simulates PV reflection by generating a photon map  
 257 representing the incident flux on the built environment. These intermediate results are also used for  
 258 the spatio-temporal workflow to apply criteria and evaluate glare duration.

259 The workflow visualises cumulative annual irradiance in absolute units ( $\text{Wh}/\text{m}^2$ ), and as ratio in  
 260 relation to a reference material. The latter is primarily intended to compare the irradiance distribution  
 261 of proposed and existing candidate materials. Both absolute and relative workflows share common  
 262 components (shown in grey in Figure 4). Components specific to evaluating absolute irradiance are  
 263 highlighted in blue, while those specific to relative irradiance are highlighted in red.

264 This simulation workflow is comprised of four stages: sky model generation, simulation model  
 265 generation, cumulative PV reflection simulation, and postprocessing. These are detailed in the  
 266 following subsections.

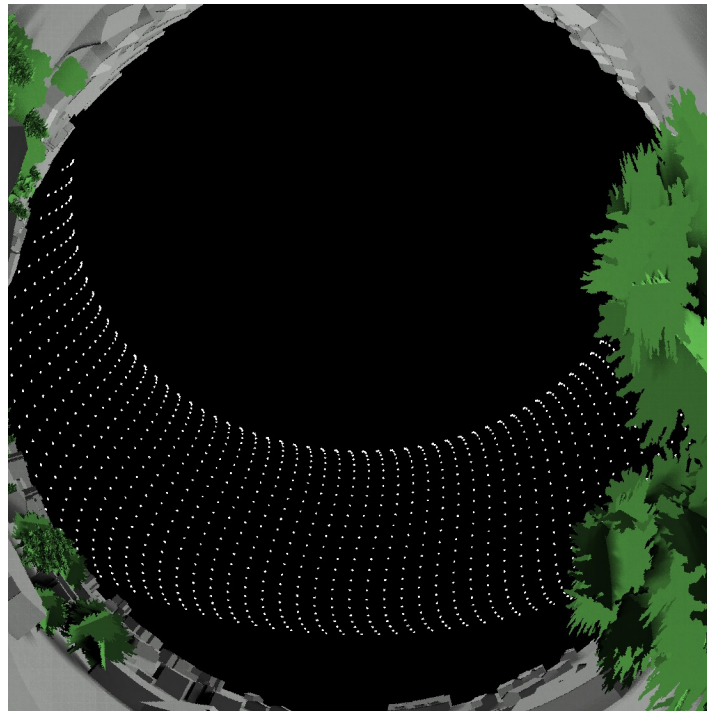
#### 267 4.3.1. Sky Model Generation

268 In the initial simulation stage, timesteps are generated in fixed intervals, enumerated as day  
 269 of year (DoY) since Jan. 1st, and local hour of day (HoD) for the current DoY. DoY and HoD are  
 270 incremented by  $\Delta\text{DoY}$  days and  $\Delta\text{HoD}$  hours, respectively, with the latter being fractional. See Table 3  
 271 for timestep ranges and increments used in the case study.

272 Note that DoY increments can be coarse, as the sun paths progress very slowly on a daily basis. By  
 273 contrast, sun paths change rapidly over the course of a day, and HoD is sampled densely. According  
 274 the Nyquist Theorem, the latter should be sampled in at least 15-minute intervals to adequately resolve  
 275 the maximum sustained glare duration threshold  $\tau_t$  of 30 minutes in Table 2.

276 DoY and HoD are converted to absolute seconds with RADIANCE's *rcalc* utility and passed  
 277 as seconds since the Epoch (Jan. 1st 1970 UTC) into the UNIX *date* utility, which generates the  
 278 corresponding date and time in UTC. These timesteps are passed to RADIANCE's *gensky* tool to  
 279 generate corresponding sky models. The timesteps are converted to local time for the specified  
 280 timezone, latitude and longitude of the site under investigation.

281 Similarly to the RADIANCE simulations for MIT's PV reflection analysis [2], a worst case scenario  
 282 is assessed by generating a sunny sky consisting only of a distant light source representing the sun's  
 283 position, without cloud cover. Solar sources for each timestep are accumulated in a RADIANCE  
 284 sky model file, with the exception of sun positions below the horizon (notably in the very early  
 285 and late winter hours); these are ignored by *gensky*. With the DoY and HoD parameters in table  
 286 Table 3 this results in 1280 timesteps / sun positions. These are shown in a hemispherical projection  
 287 facing the zenith as seen at the site under investigation in Figure 6. Note that due to analemmatic  
 288 symmetry, it suffices to simulate half a year, hence DoY is limited to 181. The second half of the  
 289 year is compensated for by suitably weighting the accumulated irradiance during postprocessing, as  
 290 described in Subsection 4.3.4.



**Figure 6.** Fisheye view (hemispherical projection) of sunny sky model with 1280 timesteps as seen from the roof of the case study, with south in the lower centre.

#### 291 4.3.2. Simulation Model Generation

292 The simulation model consists of the geometry of the site under investigation (roof or façade) as  
293 well as its immediate surroundings, at least within a radius of 100 m according to the recommended  
294 threshold  $\tau_d$  in Table 2. In addition, PV material models are a critical ingredient; these should be  
295 reasonably accurate in modelling the scattering behaviour of the proposed candidate PV modules to  
296 obtain a realistic assessment of the reflection. Both simulation components are detailed in the following  
297 subsections.

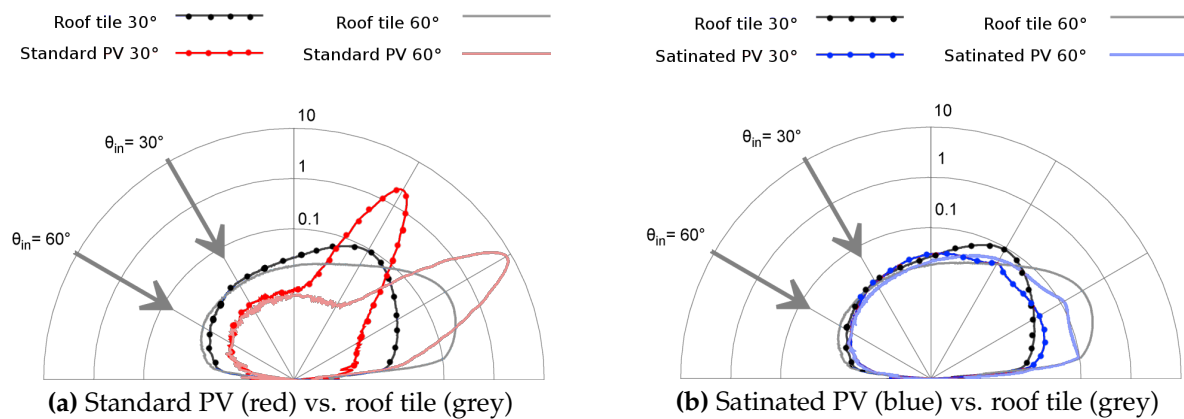
298 The geometric and material models are distilled along with the previously generated sky model  
299 into a RADIANCE scene octree with the *ocnv* tool. Since the proposed analysis primarily concerns  
300 the reflected component from the PV, this component is processed separately. Since RADIANCE offers  
301 no immediate option to exclusively render this component, an additional octree *without* sky model is  
302 generated; in conjunction with the RADIANCE photon mapping extension, this can be used to only  
303 render the indirect irradiance from PV reflection. The octree with sky is used to render the direct  
304 component, which is used as background for visualisation during postprocessing.

#### 305 *Geometric Model of Church and Surroundings*

306 The authors obtained a digital terrain model of St. Michael's church and its built environment  
307 from the Geographic Information System of the Canton of Lucerne (GIS Kanton Luzern) [23]. This  
308 model was extracted from point cloud data obtained from LIDAR scans and is available to the public.  
309 Trees in the immediate environment of the church were identified from photographs and satellite  
310 images, and added with the RHINO 3D modelling software. In addition, minor corrections to the  
311 church roof geometry were made by hand based on the original blueprints. The entire geometry was  
312 then exported with RHINO to the RADIANCE format for the simulation. All surfaces other than the  
313 church roof were assigned Lambertian materials with 25% reflectance.



**Figure 7.** Photographs of material samples used in the case study: standard PV (a), satinated PV (b), and existing roof tile (c).



**Figure 8.** Polar BSRDF plots of standard (a) and satinated (b) PV modules for incident angles of 30° and 60°. Corresponding BSRDF plots of the existing roof tile are superimposed for reference.

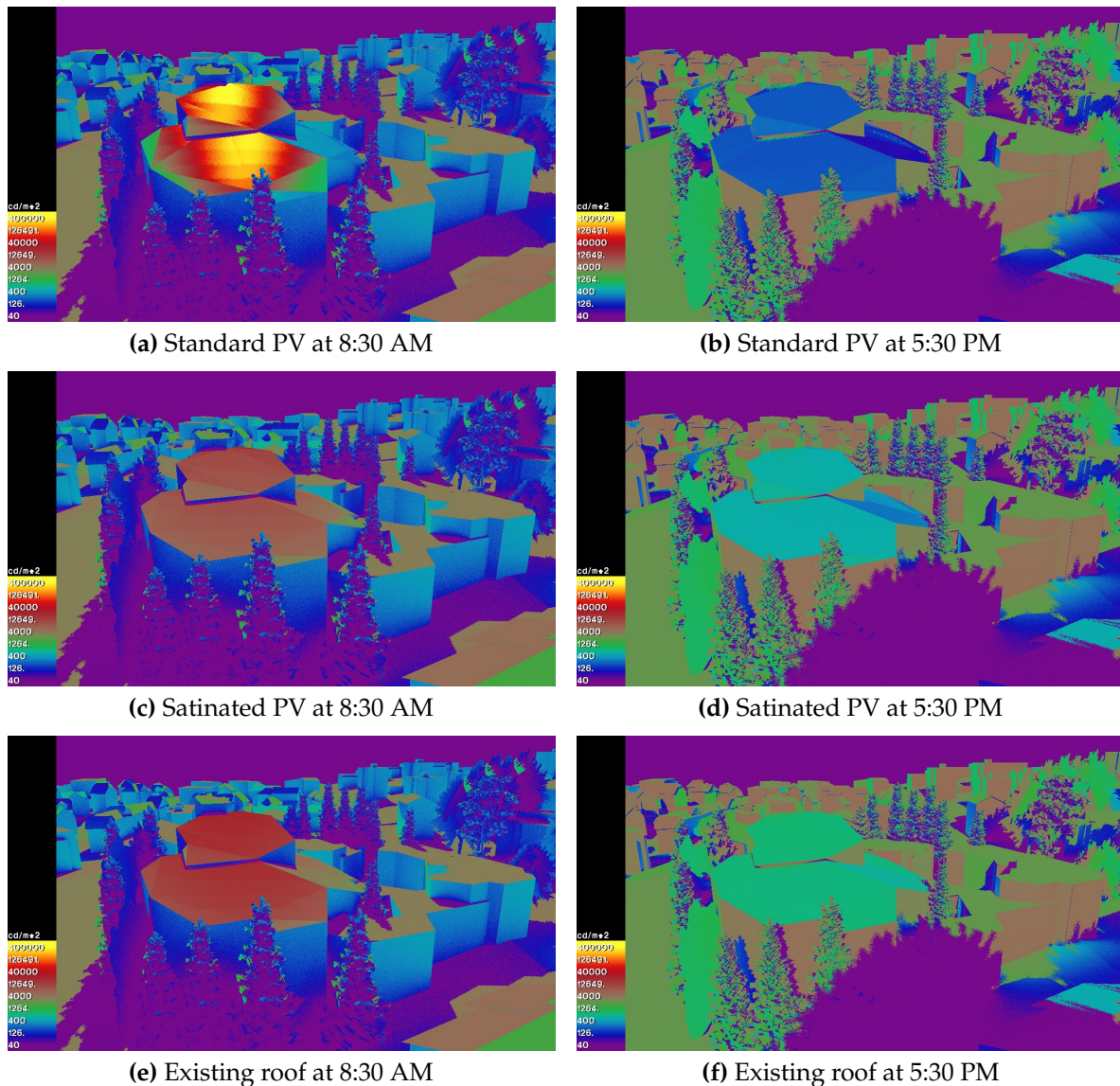
#### 314 Candidate PV Material Models

315 Samples of the proposed PV modules as well as the existing roof tiles were obtained from the  
 316 manufacturers. The samples included a standard PV module exhibiting glossy reflection, and a  
 317 satinated module with pronounced diffuse scattering more closely resembling the existing roof tile  
 318 appearance (see photographs in Figure 7). All three samples were analysed in terms of their scattering  
 319 behaviour for the simulation. To this end, each sample was measured in a goniophotometer to obtain  
 320 its BSDF (Bidirectional Scattering Distribution Function) [24], which was observed to be isotropic in  
 321 all cases. Figure 8 shows polar plots of the measured PV BSDFs for two incident directions, with the  
 322 existing roof tile BSDF superimposed as reference.

323 The candidate PV materials were modelled with the data-driven *bsdf* material primitive in  
 324 RADIANCE, which reads the data from an XML file. The XML format describes a variable-resolution  
 325 tensor tree representation of BSDF data [25], which is output by the *genbsdf* tool. The resulting data  
 326 driven BSDF model has an angular resolution of up to 128 directions in the incident plane, and 128 × 128  
 327 in the exitant hemisphere. The resolution was adaptively reduced by thresholding the least significant  
 328 80% of data.

329 Figure 9 shows falsecolour RADIANCE luminance renderings of the data-driven BSDF models  
 330 applied to the roof of the case study model. The renderings convey the appearance of the PV roof and  
 331 the different scattering characteristics of the material models subject to the time of day. As expected

332 from the BSDF plots, both the existing roof tile and satinated PV module exhibit predominantly diffuse  
 333 scattering. On the other hand, the standard PV module exhibits pronounced specular reflection,  
 334 particularly on summer mornings, conspicuously diverging in appearance from the original roof.



**Figure 9.** Falsecolour luminance renderings of the case study model looking east on June 11th at 8:30 AM (a,c,e) and 5:30 PM (b,d,f). The roof material is modelled as a data-driven BSDF for the standard PV (a,b), satinated PV (c,d), and existing roof tile (e,f). The distinct scattering behaviour of each BSDF is evident at different times of day.

### 335 4.3.3. Cumulative PV Reflection Simulation

336 The previously generated octrees (with and without sky) containing the simulation models are the  
 337 basis for the PV reflection simulation. Flux transport within the model is precomputed by generating a  
 338 photon map, which is then subsequently rendered to evaluate the irradiance on the environment. Both  
 339 steps are explained in the following sections.

#### 340 *Photon Map Generation*

341 The proposed workflow uses the RADIANCE out-of-core photon mapping extension [21,26]  
 342 developed specifically to efficiently simulate specular redirection with very large photon maps.

343 Out-of-core techniques enable paging photons on demand from disk, and maintain an active subset of  
344 these in-core in a custom cache. In addition, contribution photons are used to identify flux originating  
345 from individual sun positions corresponding to the timesteps to render the time-series irradiance maps  
346 in the spatio temporal workflow (see subsection 4.4).

347 The contribution photon map is generated with the *mkpmap* tool and written to a separate file for  
348 subsequent rendering by *rtrace* or *rcontrib*. The photon map represents the precomputed light transport  
349 from the PV material onto the surrounding surfaces and can be reused for multiple renderings. *Mkpmap*  
350 leverages the parallelism inherent in photon tracing since all photon paths are independent.

351 A number of optimisations are employed to reduce the photon count to the minimum required  
352 for the simulation, at the expense of increased photon distribution time (ca. 4 hours on an 8-core  
353 system with the case study). The photon transport is limited to a single forward scattering event  
354 from the PV surfaces onto the surroundings with *mkpmap*'s *-lr 1* option [27]. This forces *mkpmap* to  
355 disregard secondary photon reflections by terminating the photons prematurely. The rationale for this  
356 optimisation is that secondary reflections are negligible as long as the surroundings are diffuse.

357 In addition, the photon paths are limited to a cumulative length of 100 m with the *-ld* option, in  
358 accordance with the recommended criterion  $\tau_d$  in Table 2 for a residential zone. Photons are again  
359 terminated beyond this distance, thus limiting their footprint to the region of interest. Acceptable  
360 results (in terms of noise) can thus be obtained with a moderate number of photons.

361 Lastly, photon ports [27] are used to emit photons directly onto all PV surfaces (in this case,  
362 the roof), disregarding reflections from exterior walls or the surroundings. To this end, photons are  
363 displaced a small distance along the sun vector from the PV surfaces, and emitted towards them.  
364 Irregularly shaped polygons, as in the case of the roof of St. Michael's are handled via rejection  
365 sampling.

### 366 *Rendering*

367 PV reflections are rendered as a separate component using the previously generated photon  
368 map and RADIANCE octree without sky, thus omitting the direct component. The irradiance from the  
369 PV reflection onto the surroundings is evaluated via photon density estimates from the previously  
370 generated photon map with *rtrace*. This general raytracing tool in the RADIANCE suite supports parallel  
371 raytracing and can be used for rendering by passing in primary rays from a view via *vwrays*. The  
372 renderings are then output as RADIANCE HDR images. These are then postprocessed for visualisation  
373 of the reflected component as described in the following section.

374 The direct component is also rendered with *vwrays / rtrace* but using the octree with sky. The  
375 indirect (reflected) component is omitted by setting zero ambient bounces with the *-ab 0* option. The  
376 resulting direct irradiance map serves as background for the subsequent postprocessing.

377 Note that renderings are generated from two representative perspectives: a plan view as an  
378 overview for context, with the site under investigation in the centre, and a cylindrical projection as  
379 360° panoramic view from the roof. The latter aids in identifying "hotspots" on adjacent buildings, as  
380 well as their corresponding directions. A fore clipping plane was used to prevent the church geometry  
381 from occluding the foreground.

### 382 4.3.4. Postprocessing

383 In the postprocessing phase, the rendered PV reflection irradiance maps are evaluated. For the  
384 absolute annual irradiance, Wh (Watt-hours) are derived from the reflected irradiance on the built  
385 environment. For the relative annual irradiance, a unitless ratio of reflected irradiance to that of the  
386 (previously rendered) reference case is derived in order to compare the reflection distribution in the  
387 environment. Both evaluation modes are detailed in the following subsections.

388 In both cases, the reflected irradiance map is falsecoloured and composited with the direct  
389 irradiance map. The latter is attenuated beforehand by *pcond* using the *-e* (exposure) option to provide  
390 a background for the visualisation to aid in orientation; it does not convey radiometric data.

### 391 *Absolute Annual Irradiance*

To evaluate the absolute annual irradiance from PV reflection, the raw reflected irradiance data (consisting of cumulative irradiance proportional to the number of simulated timesteps) is multiplied with an annual integration factor  $dt$ . This is done by scaling the HDR pixels in the reflected irradiance map by  $dt$  using the *pcomb* utility. Given timesteps spanning half a year ( $DoY \in [0, 181]$ ), the annual integration factor  $dt$  to obtain the cumulative irradiance in Watt-hours [Wh] is approximated by:

$$dt \approx 2\Delta HoD \cdot \Delta DoY, \quad (1)$$

392 where the factor 2 compensates for the symmetric second half of the year. The accuracy of the integrated  
393 annual irradiance obviously depends on the increments  $\Delta HoD$  and  $\Delta DoY$ ; smaller increments (and  
394 consequently more timesteps) will result in a finer grained simulation and more accurate results, at the  
395 expense of longer simulation and postprocessing times.

### 396 *Relative Annual Irradiance*

397 To visualise the reflected irradiance distribution in relation to that of a reference case, the reflected  
398 irradiance map pixels are divided by those in the reference irradiance map (obtained from a previous  
399 simulation run with the reference material) using *pcomb*. The ratio is clamped to zero for pixels with  
400 zero irradiance (typically in peripheral or occluded areas, where no photons were deposited), thus  
401 avoiding division by zero. The resulting image is unitless, with values above 1 indicating the PV  
402 reflection exceeds that of the reference, and values below 1 indicating the inverse.

### 403 *4.4. Spatio-Temporal Workflow*

404 The spatio-temporal workflow summarised in [Figure 5](#) follows from the general workflow and  
405 reuses its generated simulation model, photon map, and timesteps. From these, it simultaneously  
406 renders temporal reflected irradiance maps for each timestep using the *RADIANCE rcontrib* tool.  
407 The photon map supports the association of flux contributions with individual solar sources (and  
408 corresponding timesteps) in order to evaluate the constituent irradiance at each timestep. As in the  
409 general workflow, the irradiance maps are rendered with an octree without sky to only visualise the  
410 reflected component; the direct irradiance map is reused here again as background for compositing  
411 the visualisation.

412 The goal of this workflow is to assess glare duration as primary criterion for identifying  
413 problematic glare zones, where glare is defined as reflected irradiance exceeding the threshold  $\tau_E$  in  
414 [Table 2](#). The output is a visualisation of the cumulative glare duration (as isolated events) over the  
415 course of a year, as well as the maximum *sustained* glare for any day of the year. The latter is derived  
416 from the maximum number of contiguous timesteps for which the irradiance exceeds the threshold  
417 without interruption. This implies temporal contiguity, which the proposed workflow identifies using  
418 feature detection. As with the general workflow, both outputs share common components (shown in  
419 grey in [Figure 5](#)), and those specific to cumulative glare duration are highlighted in red, while those  
420 specific to sustained glare are highlighted in blue.

421 The postprocessing in this workflow is considerably more elaborate and mostly implemented  
422 with a Python script using the *ndimage* multi-dimensional image processing submodule as part of the  
423 SciPy scientific computing library [28]. The script processes a chronological time-series of irradiance  
424 maps as a 3-dimensional volume (2D matrices with an additional temporal dimension).

425 The spatio-temporal postprocessing of the time-series irradiance maps consists of four main steps  
426 (five for sustained glare): filtering, thresholding, feature detection (for sustained glare), reduction, and  
427 visualisation. These are detailed in the following subsections.

#### 428 4.4.1. Filtering

429 The 2D reflected irradiance maps rendered by *rcontrib* for each timestep are read from disk by  
430 the SciPy script and stacked in chronological order to form a spatio-temporal irradiance volume  
431 represented as a 3D matrix. Due to memory constraints and the high resolution of the irradiance maps,  
432 the timesteps will typically only encompass a single day, although the method would in principle  
433 work on the entire annual set of timesteps.

434 As the reflected irradiance maps are the result of Monte-Carlo raytracing with sparse photon  
435 distributions in dark areas, they exhibit considerable noise which can lead to unwanted temporal  
436 and spatial fluctuations after thresholding that break up potentially contiguous regions. The noise is  
437 reduced with a 3D Gaussian filter, thus improving temporal continuity and stabilising the subsequent  
438 thresholding. While this leads to a loss in detail, it instead emphasises large patches of glare, which is  
439 in fact desirable for the intended result.

#### 440 4.4.2. Thresholding

441 As the main criterion for identifying glare, the filtered pixel in the irradiance volume is compared  
442 against the recommended threshold  $\tau_E$  in Table 2. This results in a binary value for each pixel indicating  
443 whether its corresponding irradiance is below or above the threshold; a nonzero value thus indicates  
444 the presence of glare according to  $\tau_E$ . Note that, although the pixels assume integer values, the *ndimage*  
445 library still treats the data as floating point, at the expense of increased memory consumption.

#### 446 4.4.3. Feature Detection (Sustained Glare)

447 When assessing sustained glare, the proposed workflow must identify neighbouring, i.e.  
448 contiguous, instances of glare along the spatial and temporal axes. This entails isolating regions  
449 of consecutive nonzero pixels (categorised as glare in the previous step) via feature detection. A  
450 method typically used in computer vision, feature detection attaches nonzero labels to neighbouring  
451 pixels. By applying this in three dimensions, it also accounts for temporal contiguity. The output is  
452 a new volume with nonzero integer labels in pixels categorised as glare over multiple consecutive  
453 timesteps. Each feature corresponds to a separate glare event and has a unique label.

#### 454 4.4.4. Reduction

455 In this step, the 3D thresholded irradiance volume is reduced to a single 2D image for visualisation.  
456 For the cumulative glare duration, this entails simply summing the thresholded binary pixel values  
457 over the temporal axis.

458 For sustained glare, however, this entails summing (i.e. counting) all instances of pixels with  
459 nonzero labels along the temporal axis. The pixels' actual values are disregarded, since these are  
460 unique for each contiguous region identified by the feature detection. In addition, disjunct features  
461 may overlap in time, e.g. if a pixel experiences several glare events in the course of a day from  
462 multiple PV surfaces. To account for this, only the maximum number of nonzero pixels from all  
463 features is accumulated, since a planner is primarily interested in assessing the longest glare duration  
464 as worst-case scenario.

465 The output of both reductions is a 2D matrix containing an integer count of the number of  
466 timesteps corresponding to the cumulative or sustained glare duration. This is weighted accordingly  
467 in the final step of the workflow. In preparation for this, the matrices are written back to disk as  
468 RADIANCE HDR images by the SciPy script, at which point it terminates.

469 As mentioned above, the current workflow processes daily irradiance maps, consequently the  
470 resulting HDR images must be accumulated for the entire simulation run; this entails another level of  
471 reduction (accumulating maxima in the case of sustained glare) in a separate Python script, which is  
472 not shown in Figure 5.

#### 473 4.4.5. Visualisation

474 The final step in the proposed spatio-temporal workflow entails scaling the glare duration timestep  
475 count in the reduced HDR images, falsecolouring them, and compositing them with an attenuated  
476 background image of the direct irradiance as in the general workflow.

477 As in Subsection 4.3.4, the HDR images containing cumulative annual timestep counts are scaled  
478 with the annual integration factor  $dt$  (Equation 1) with RADIANCE's *pcomb* tool, resulting in cumulative  
479 annual glare duration in hours. For sustained glare, however, the HDR images are scaled with the  
480 hourly timestep increment,  $\Delta HoD$ , to arrive at the corresponding maximum glare duration for any  
481 day of the year, in hours.

### 482 5. Results and Discussion

#### 483 5.1. Annual Reflected Irradiance

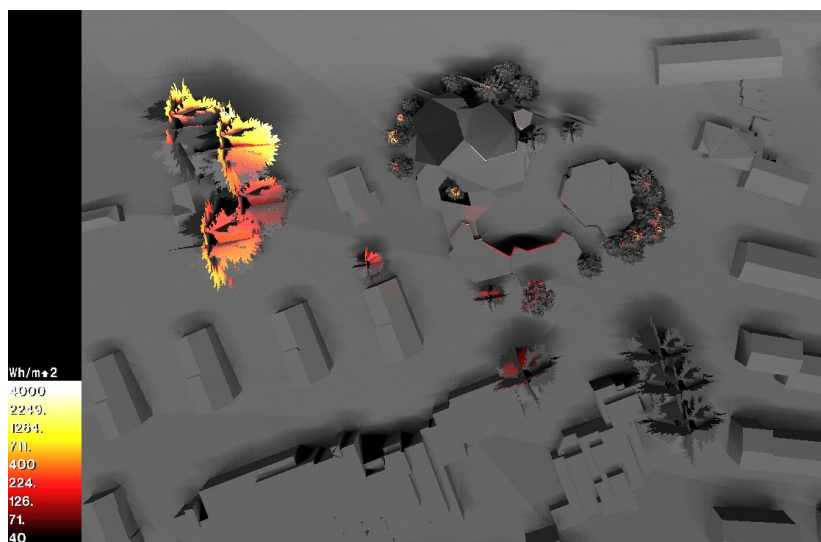
484 It is already evident from Figure 8 and Figure 9 that the candidate PV module BSDFs exhibit  
485 divergent scattering behaviour; while the standard PV is characterised by significant glossy reflection,  
486 the satinated PV is noticeably diffuse, and closely resembles the scattering behaviour of the original  
487 roof tile. This disparity is corroborated in the simulation results from the case study.

488 Figure 10 shows plan views of the absolute cumulative annual irradiance reflected from the  
489 two candidate PV samples and existing roof tile. The church model with simulated roof material is  
490 located in the centre. Note the irradiance scale (Watt-hours) is logarithmic, and only applies to the  
491 falsecoloured reflected component. The direct component is composited as background for orientation  
492 to identify potentially affected buildings in the environment.

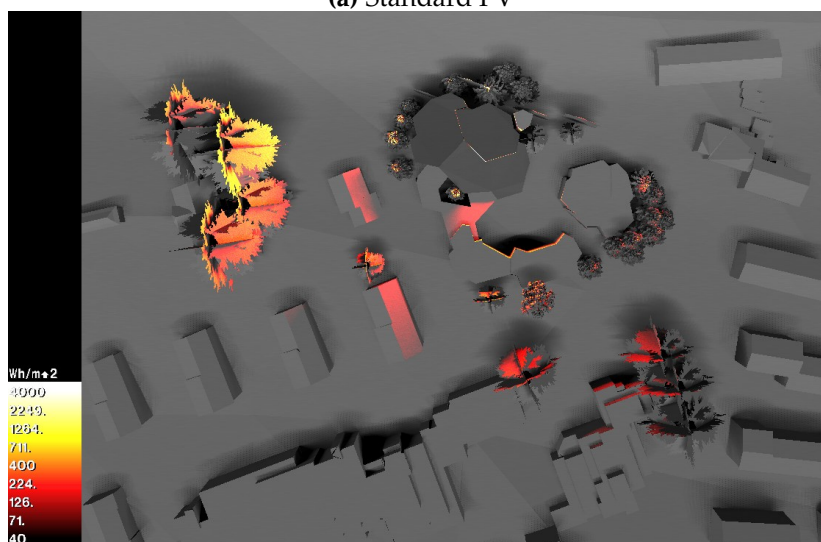
493 The reflection distribution in relation to the existing roof tile is shown in Figure 11. The reflected  
494 component is again falsecoloured, this time on a linear scale as ratio of the annual reflected irradiance  
495 from the candidate PV divided by the annual reflected irradiance from the existing roof tile. The  
496 red/yellow regions (ratio > 1) indicate directions in which the PV reflects more intensely than the roof  
497 tile, while the blue regions (ratio < 1) indicate subdued PV reflection compared to the roof tile. Regions  
498 with zero reflection (due to occlusion or because they lie outside the zone of influence) are coloured  
499 magenta.

500 Figure 12 shows both the cumulative annual irradiance and relative reflection distribution as  
501 cylindrical panorama view from the church roof. The view faces south in the centre, while the left and  
502 right edges wrap around and face north. The sun paths comprising the sky model for the simulated  
503 half-year are clearly visible above the horizon (although they are absent in the reflected irradiance  
504 maps). Part of the parish adjacent to the church can be seen in the foreground, while the church itself  
505 is clipped by the fore clipping plane so as not to occlude the view.

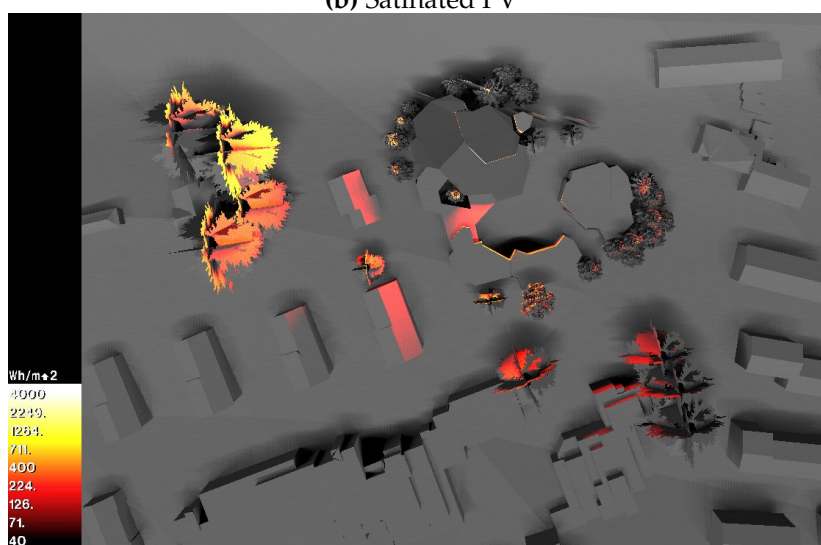
506 These visualisations provide a PV planner with a concise overview of the reflective distributions  
507 of candidate PV materials over the course of a year, and which neighbouring buildings are potentially  
508 subjected to glare. It is obvious from these results that the standard PV exhibits a pronounced  
509 heterogeneous reflection distribution, with a prominent hotspot towards the west, while the satinated  
510 PV exhibits more homogeneous reflection, on par with the existing roof tile used as reference. While  
511 the hotspot is present in all renderings, it varies in intensity depending on the roof material. For the  
512 standard PV, the absolute cumulative annual irradiance shown in Figure 12 peaks in this zone at ca.  
513 3000 Wh/m<sup>2</sup>, but only at ca. 1000 Wh/m<sup>2</sup> for the satinated PV. Note that this hotspot coincides with  
514 a group trees shielding a 2-storey chalet behind them, as can be observed left of the plan views in  
515 Figure 10 and Figure 11. This hotspot dominates in the early mornings in June, when the trees bear  
516 foliage. This is confirmed by the rendered luminance maps for June 11th at 8:30 AM in Figure 9(a,c,e),  
517 looking east from the approximate position of the hotspot. Note that the luminance from the standard  
518 PV module far exceeds the recommended threshold  $\tau_L$  of 50 kcd/m<sup>2</sup> in Table 2, correlating with the  
519 potential for glare indicated by the irradiance map.



(a) Standard PV

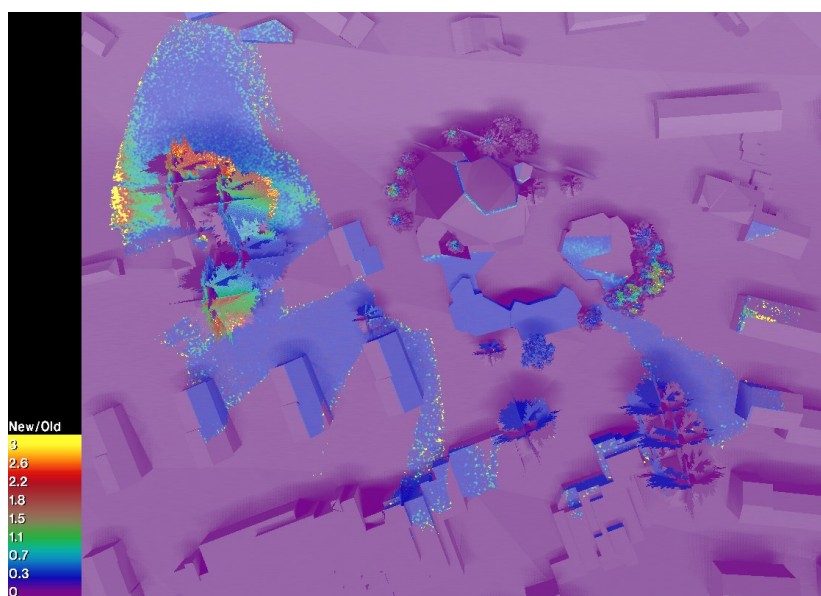


(b) Saturated PV

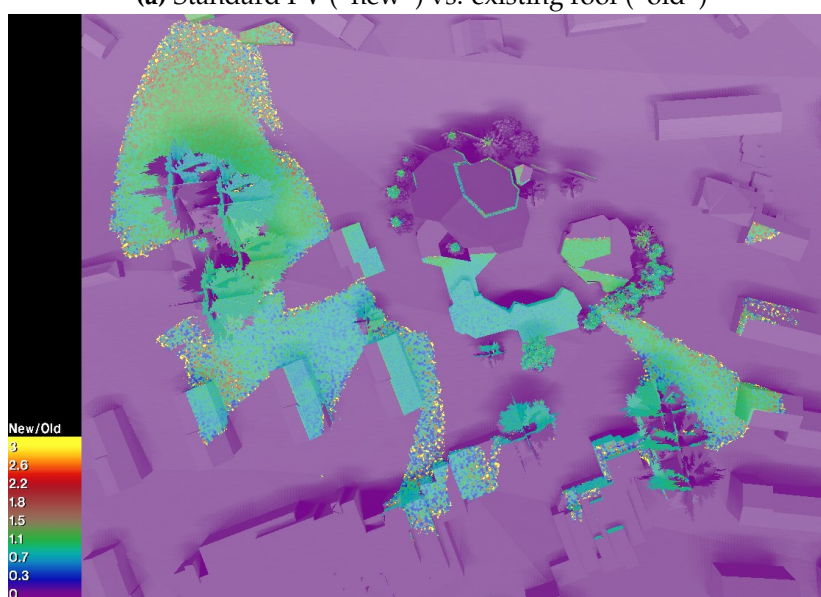


(c) Existing roof

**Figure 10.** Plan views of absolute cumulative annual irradiance in Wh/m<sup>2</sup> from standard PV (a), saturated PV (b) and existing roof tile (c).

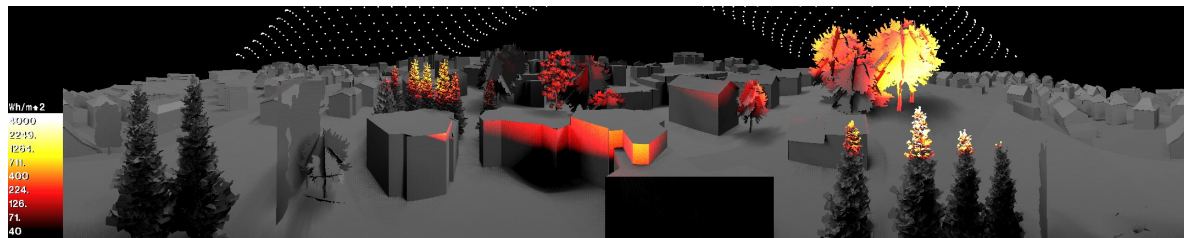


(a) Standard PV ("new") vs. existing roof ("old")

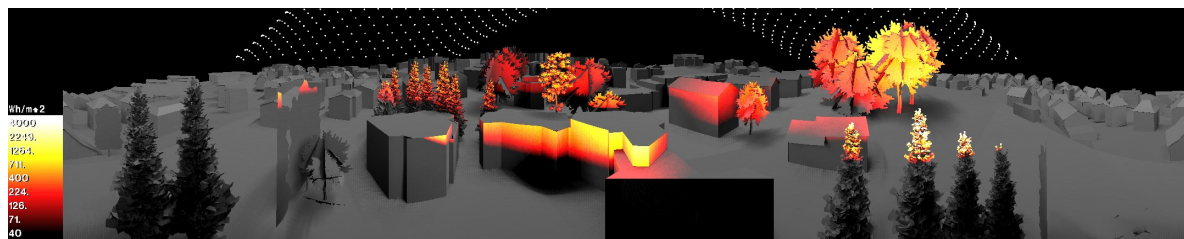


(b) Satinated PV ("new") vs. existing roof ("old")

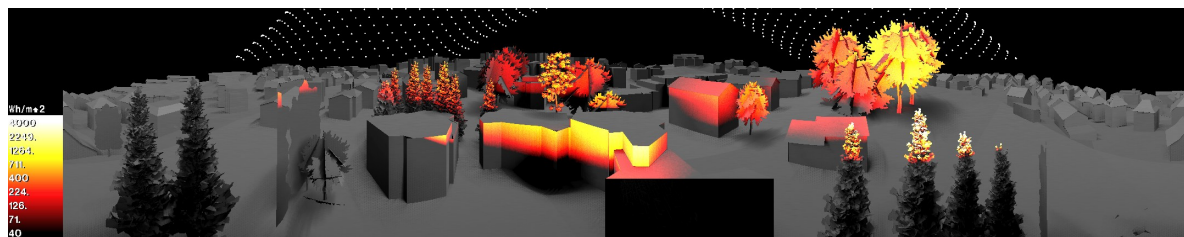
**Figure 11.** Plan views of reflection distribution from standard (a) and satinated (b) PV in relation to the existing roof tile, expressed as irradiance ratios.



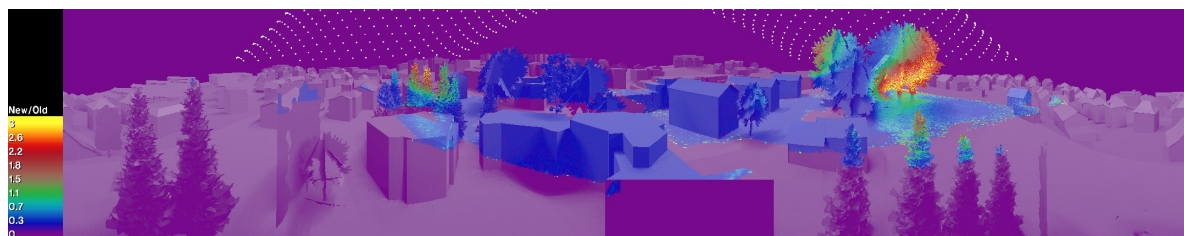
(a) Standard PV



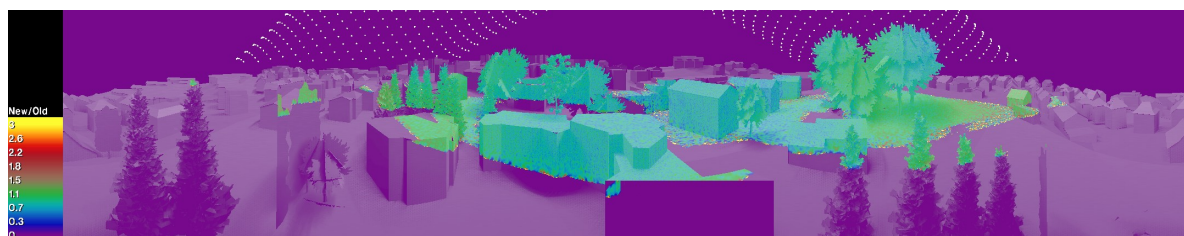
(b) Saturated PV



(c) Existing roof

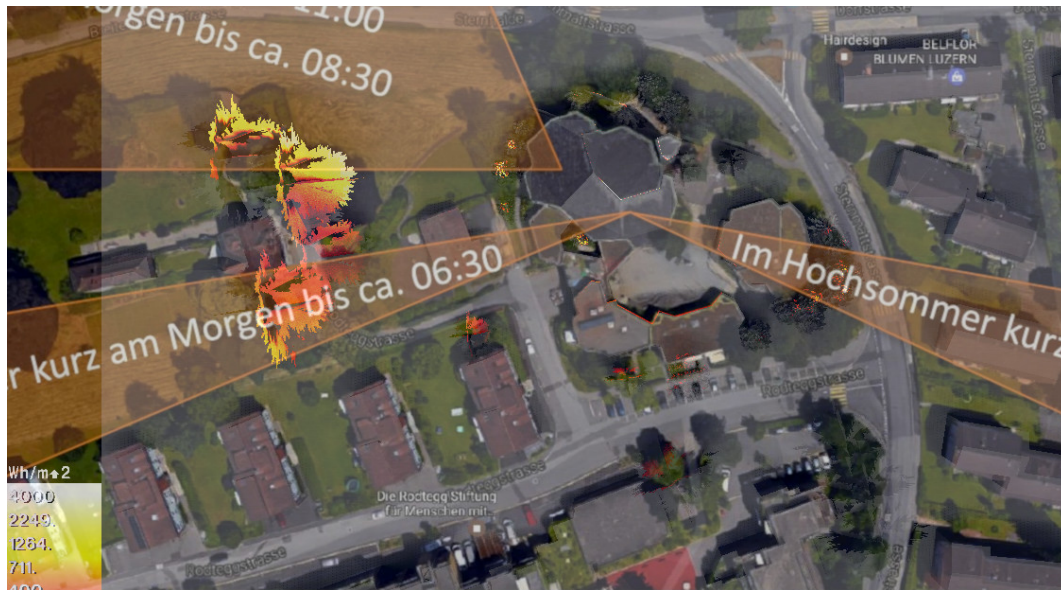


(d) Standard PV ("new") vs. existing roof ("old")



(e) Saturated PV ("new") vs. existing roof ("old")

**Figure 12.** Panoramic views of annual irradiance from standard PV (a, d), saturated PV (b, e) and existing roof tile (c), with centre facing south. Figures (a–c) are in absolute units, while figures (d–e) are reflection distributions in relation to the existing roof tile, expressed as irradiance ratios.



**Figure 13.** Reflection zones initially predicted by PV system installer (Figure 3) superimposed with plan view of simulated annual reflected irradiance obtained with the proposed method (Figure 10).

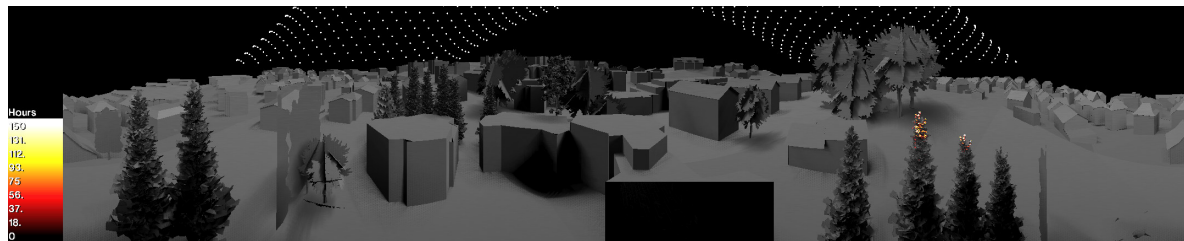
520 The results of the proposed method agree well with the predictions for the first PV roof retrofit  
 521 proposal in Figure 3. This is evident by superimposing a simulated plan view from Figure 10 obtained  
 522 with the proposed method. The resulting composite, shown in Figure 13, confirms the initial prediction  
 523 in terms of the locations and approximate timespans of the hotspots. The aforementioned hotspot  
 524 on the group of trees in the west, predicted on summer mornings before ca. 8:30 AM, matches well.  
 525 Note that while this initially predicted reflection zone extends towards the northwest, there are no  
 526 buildings in this direction within the maximum distance  $\tau_d$  of 100 m considered in the simulation. A  
 527 secondary hotspot on the edge of the trees in the west-southwest on midsummer mornings before ca.  
 528 6:30 AM also matches. Lastly, minor hotspots on the treetops immediately adjoining the complex in  
 529 the east-southeast on midsummer evenings after ca. 6:30 PM also correspond well.

### 530 5.2. Application of Recommended Criteria, Glare Duration

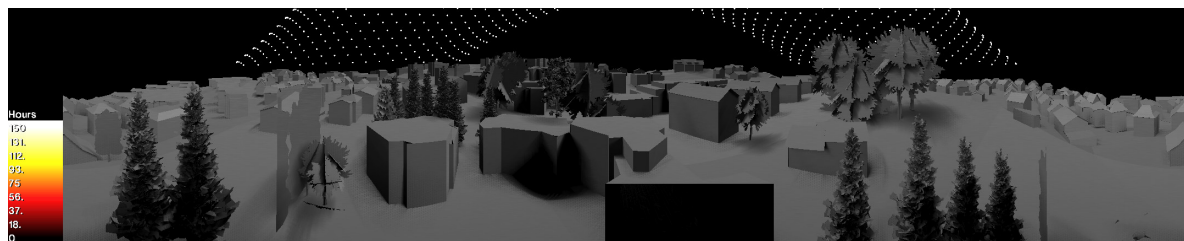
531 An assessment of the potential for glare from the aforementioned hotspot is obtained by applying  
 532 one of the recommended irradiance thresholds  $\tau_E$  from Table 2 to the time-series irradiance maps  
 533 in the spatio-temporal workflow. Figure 14 shows panoramic views of the cumulative annual glare  
 534 duration obtained with a  $\tau_E$  of 30 W/m<sup>2</sup> and 10 W/m<sup>2</sup> as recommended by Swissolar and Sandia  
 535 Labs, respectively. Figure 15 shows the maximum sustained glare duration for any day of the year, i.e.  
 536 per-pixel glare duration maxima for all simulated days. Again, this is shown as panoramic views for a  
 537  $\tau_E$  of 30 W/m<sup>2</sup> and 10 W/m<sup>2</sup>.

538 These visualisations provide a tangible prediction of likely glare according to the criteria. By  
 539 condensing the temporal dimension into a single image quantifying the glare duration, and by isolating  
 540 problematic zones, the visualisation is intuitive to PV planners, but more importantly, their clients  
 541 and municipal planning authorities who will review the results. Radiometric units (which may be  
 542 misinterpreted by non-experts) are replaced with the common unit of time, making this visualisation  
 543 highly accessible.

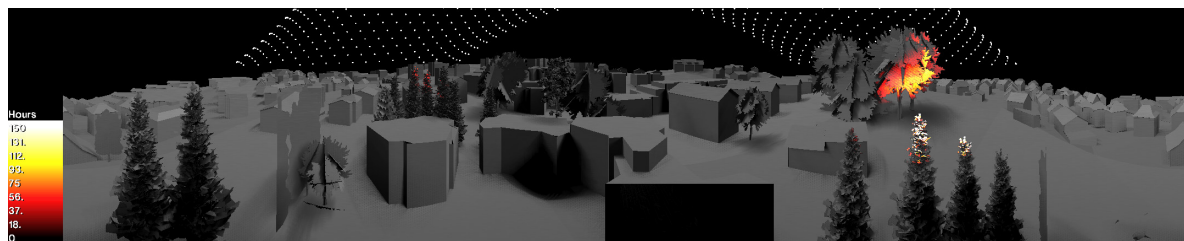
544 With  $\tau_E = 30 \text{ W/m}^2$ , there is no annual glare whatsoever from either candidate PV, as shown  
 545 in Figure 14 and Figure 15. In stark contrast, applying Sandia Labs' more conservative threshold  
 546  $\tau_E = 10 \text{ W/m}^2$  indicates significant annual glare durations of up to 100 hours in the group of trees to  
 547 the west with the standard PV module. This is twice the maximum annual duration  $\tau_T$  of 50 hours  
 548 recommended in Table 2. As Figure 15 reveals for the same  $\tau_E$ , this region experiences a maximum



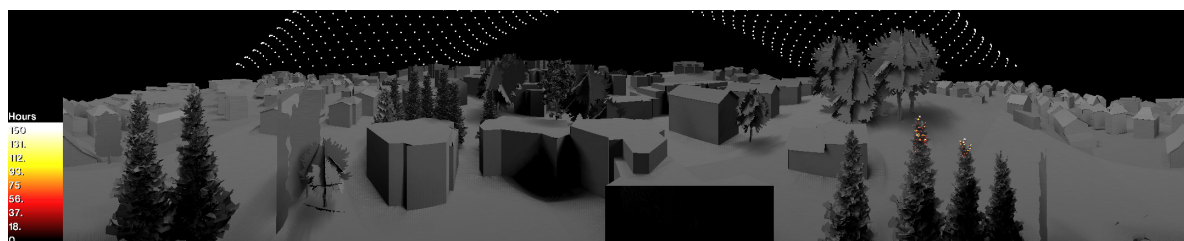
(a) Standard PV,  $\tau_E = 30 \text{ W/m}^2$



(b) Satinated PV,  $\tau_E = 30 \text{ W/m}^2$

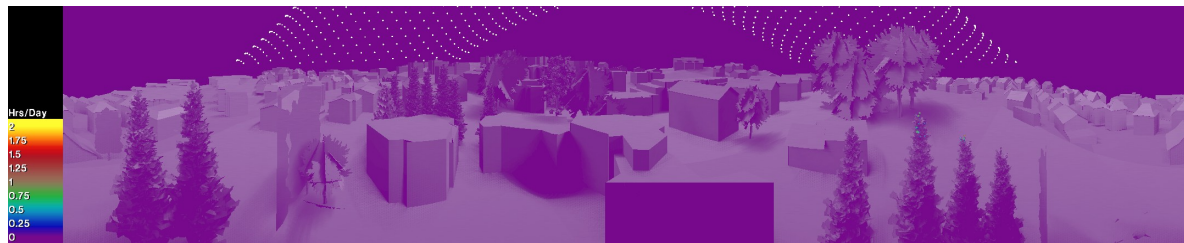


(c) Standard PV,  $\tau_E = 10 \text{ W/m}^2$

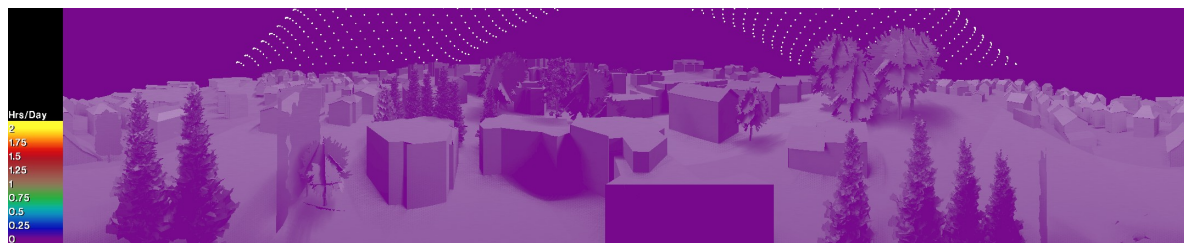


(d) Satinated PV,  $\tau_E = 10 \text{ W/m}^2$

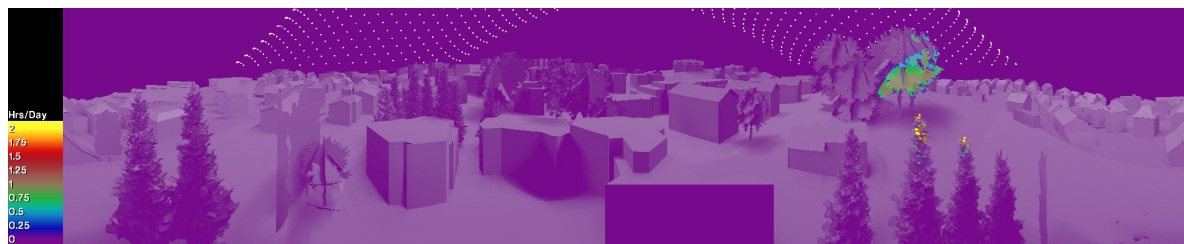
**Figure 14.** Panoramic views of cumulative annual glare duration in hours for standard (a,c) and satinated (b,d) PV modules. Glare is identified according to irradiance thresholds  $\tau_E = 30 \text{ W/m}^2$  as recommended by Swissolar (a,b), and  $\tau_E = 10 \text{ W/m}^2$  as suggested by Sandia Labs (c,d).



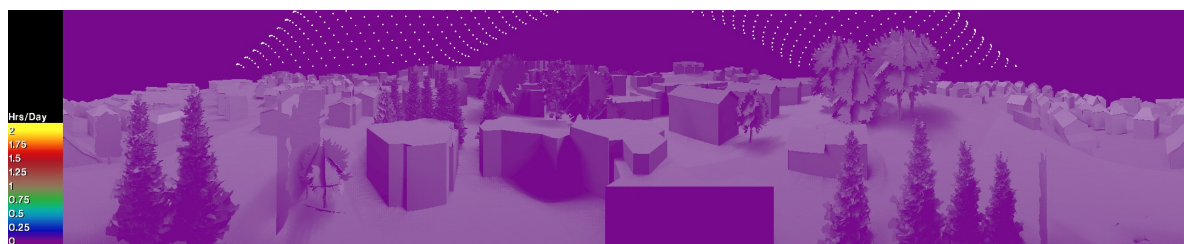
(a) Standard PV,  $\tau_E = 30 \text{ W/m}^2$



(b) Satinated PV,  $\tau_E = 30 \text{ W/m}^2$



(c) Standard PV,  $\tau_E = 10 \text{ W/m}^2$



(d) Satinated PV,  $\tau_E = 10 \text{ W/m}^2$

**Figure 15.** Panoramic views of maximum sustained glare duration in hours for any day of the year incurred by reflections from standard (a,c) and satinated (b,d) PV modules. Glare is identified according to irradiance thresholds  $\tau_E = 30 \text{ W/m}^2$  as recommended by Swissolar (a,b), and  $\tau_E = 10 \text{ W/m}^2$  as suggested by Sandia Labs (c,d).

549 sustained glare duration of up to 1 hour; again, twice the maximum glare duration  $\tau_t$  of 30 minutes  
550 for any day of the year as recommended in Table 2. These glare incidents would be considered  
551 problematic were they to lie on adjacent buildings, warranting a luminance-based assessment from the  
552 corresponding observation point. In the context of this case study, however, it is assumed vegetation is  
553 impervious to glare, and will not take any recourse.

554 Both candidate PV materials are therefore considered viable for the retrofit and not critical in  
555 terms of glare. Subject to the constraints of the heritage protection board, the decision will likely be  
556 based on which candidate better preserves the existing appearance of the roof, with the satinated PV  
557 clearly being the favourable choice.

### 558 5.3. Practical Applications and Impact

559 The proposed method is expected to find applications in the following contexts, possibly in the  
560 form of a consultation service:

- 561 • Assessing proposed PV installations for compliance with regulations by building authorities and  
562 urban planners.
- 563 • Developing low-glare PV module surfaces by PV manufacturers.
- 564 • Defining PV glare assessment criteria, thresholds, and technical guidelines by trade associations.
- 565 • Establishing urban regulations concerning PV installations by government agencies.

566 The primary impact is expected to be an increased awareness of the side-effects from PV  
567 installations in urban environments, which will become more prevalent in the future. It is hoped this  
568 will also spawn further research towards refining the existing assessment criteria. With the proposed  
569 tool, the current thresholds can be refined in relation to their perception (e.g. discomfort or disability  
570 glare) by drawing on documented cases for which measurements are available, and simulating these.  
571 This can yield criteria that better accommodate individual responses and tolerances to glare, as well as  
572 providing insight into how these translate to simulation results.

### 573 5.4. Limitations

574 It should be acknowledged that the proposed workflow, as currently implemented, is a proof of  
575 concept, and therefore limited in a number aspects. Among these are:

- 576 • While using irradiance as physical metric is convenient to indicate potential glare, it is an integral  
577 quantity; as such, it may underrepresent isolated incidents of high radiance/luminance from  
578 reflectors subtending very small solid angles within an observer's field of view. While the  
579 resulting glare can even be disabling, such events tend to be of short duration (corresponding to  
580 glint), and may not appreciably impact the sustained glare duration.
- 581 • The background luminance (and therefore contrast) is not considered.
- 582 • The simulation depends on the accuracy and timeliness of the digital terrain model; in particular,  
583 vegetation is assumed to be a static, effectively opaque barrier irrespective of season in the case  
584 study.
- 585 • The PV surface models are derived from new production samples, and do not take weathering  
586 or manufacturing tolerances into account.
- 587 • While a sunny sky assesses the worst-case scenario, a more realistic assessment would be  
588 obtained using a climate-based sky model that accounts for typical cloud cover on site.
- 589 • The temporal resolution is currently 15 minutes, which may be insufficient in detecting  
590 high-frequency glare. While the timestep increments can be finer grained, this increases  
591 simulation and postprocessing times.
- 592 • Timestamp increments are fixed, thus the simulation also expends considerable computational  
593 effort on timestamps that contribute negligible irradiance, rather than sampling adaptively.
- 594 • The current workflow is static and non-interactive, since the simulation must complete before  
595 the results can be assessed.

596 Some of these issues are addressed as future work in the conclusions.

## 597 6. Conclusions and Future Work

598 This paper presented a novel image-based methodology for assessing glare from PV reflections.  
599 The proposed methodology contributes the following to the existing body of work:

- 600 • A general workflow to assess cumulative annual irradiance from PV reflection, both in absolute  
601 terms and in relation to a reference material in order to compare different candidate PV surface  
602 materials.
- 603 • A novel, image-based spatio-temporal workflow that applies recommended assessment criteria  
604 and thresholds to quantify the cumulative annual glare duration, and the maximum sustained  
605 glare duration for any day of the year.
- 606 • A PV reflection simulation using data-driven material models of measured BSDFs.
- 607 • A digital terrain model of the site providing the urban context of the simulation.
- 608 • Photon mapping to efficiently precompute only the reflected component from the PV on the  
609 surrounding buildings.
- 610 • A falsecolour visualisation of reflected irradiance in the context of the built environment suitable  
611 for practitioners, municipal planning authorities and clients of PV installations. Including  
612 a background image of the built environment enables identification of potentially affected  
613 buildings. Such a visualisation is readily accessible to non-experts as well as practitioners.

614 The proposed method was demonstrated with a representative case study of a PV roof retrofit on  
615 a heritage protected site. Two candidate PV modules, standard and satinated, were measured from  
616 physical samples and simulated as data-driven BSDFs. Glare was then assessed by applying two  
617 alternative irradiance thresholds,  $\tau_E = 30 \text{ W/m}^2$ , as recommended by Swissolar, and  $\tau_E = 10 \text{ W/m}^2$ , as  
618 recommended by Sandia Labs. The results of the case study lead to the following conclusions:

- 619 • While the satinated PV module exhibits a homogeneous reflection distribution and no potential  
620 for glare at all, the standard PV module concentrates its reflections towards the west of the site  
621 during summer mornings (see [Figure 11](#)).
- 622 • The proposed spatio-temporal workflow identifies glare in the west when applying the  
623 conservative irradiance threshold of  $10 \text{ W/m}^2$ , which translates into an annual glare duration of  
624 ca. 100 h (see [Figure 14](#)) and a maximum sustained glare duration of 1h for any day of the year  
625 (see [Figure 15](#)). These exceed the recommended limits of  $\tau_T = 50 \text{ h}$  and  $\tau_t = 30 \text{ min}$ , respectively.
- 626 • While the standard PV module is likely to cause glare according to Sandia Labs' threshold, the  
627 affected zone is not critical, since it is populated by vegetation shielding a residential building  
628 behind it. This is noticeable in the plan views (see [Figure 10](#) and [Figure 11](#)).
- 629 • In consideration of the noncritical nature of the identified glare with the standard PV module,  
630 both candidates are viable replacements for the current roof. Because the site is heritage protected  
631 however, the satinated PV is more suitable in preserving the current appearance of the roof (see  
632 [Figure 9](#)).
- 633 • A comparison with predictions made in an earlier proposal for a PV roof retrofit confirmed  
634 that the proposed method indeed complements and supports the expertise of a PV planner (see  
635 [Figure 13](#)).

636 It should be emphasised that applying the recommended criteria in the proposed workflow does  
637 not constitute their validation. Whether the predicted glare is actually perceived as disturbing is, as  
638 the criteria themselves, highly subjective. Note, however, that the irradiance threshold recommended  
639 by Swissolar is based on a theoretical maximum. By contrast, the lower limits proposed by Sandia  
640 Labs and MIT are based on experimental data. If in doubt, either of the latter may be preferable in  
641 order to accommodate a higher tolerance in individual perception and reduce the likelihood of glare.

642 The proposed methodology is still a proof of concept both in terms of technological realisation  
643 and visualisation of the results. To address this and the limitations summarised in [subsection 5.4](#), the  
644 following avenues are being considered as future work:

- 645 • Optimisation of the scripts comprising the spatio-temporal workflow, particularly the memory  
646 footprint of the sustained glare extraction, which currently limits it to iteratively processing daily  
647 timesteps as the matrices tend to be very large (several gigabytes).
- 648 • Improvements to the daylight simulation engine. Progressive photon mapping techniques with  
649 visual feedback, for example, would introduce a degree of interaction to the simulations by  
650 allowing a planner to identify and react to hotspots early, while the results are still being refined.  
651 Currently the simulation runs to completion before the results can be reviewed.
- 652 • On a more fundamental level, the light transport algorithm at the heart of the simulation engine  
653 should be modified to more efficiently sample adaptively in the spatial *and* temporal domains.  
654 The raytracing algorithms currently employed in RADIANCE do not account for the latter, and  
655 annual simulations always use large numbers of fixed timesteps, with few actually contributing  
656 significantly to the results (i.e. as detectable glare in the analysis).
- 657 • The proposed method should be applied to a more comprehensive suite of extant case studies  
658 and recommended criteria, with the goal of refining the latter in terms of how the predicted glare  
659 is actually perceived on site.

660 With this paper, the authors intend to draw attention to the growing problem of glare from BIPV,  
661 as well as glass façades in general, and hope that the proposed method presented herein will stimulate  
662 future research in this field. Though still a proof of concept, this work can, after some maturation,  
663 support trade associations in defining assessment criteria, government agencies in establishing urban  
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679 ran the simulations, processed the data, visualised the results, and wrote the relevant sections comprising the  
680 bulk of the paper. Christian Renken advised on the proposed criteria and requirements from a practitioner's  
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682 All authors reviewed the publication.

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684 **References**

- 685 1. Danks, R.; Good, J.; Sinclair, R. Assessing reflected sunlight from building facades: A literature  
686 review and proposed criteria. *Building and Environment* **2016**, *103*, 193 – 202. Available  
687 online: <https://www.sciencedirect.com/science/article/pii/S0360132316301354> (accessed 24.01.2018),  
688 doi:10.1016/j.buildenv.2016.04.017.
- 689 2. Jakubiec, J.A.; Reinhart, C.F. Assessing Disability Glare Potential of Reflections from New Construction:  
690 Case Study Analysis and Recommendations for the Future. *Transportation Research Record* **2014**,  
691 *2449*, 114–122. Available online: <https://journals.sagepub.com/doi/10.3141/2449-13> (accessed 11.07.2018),  
692 doi:10.3141/2449-13.
- 693 3. Carlucci, S.; Causone, F.; Rosa, F.D.; Pagliano, L. A review of indices for assessing visual comfort with a  
694 view to their use in optimization processes to support building integrated design. *Renewable and Sustainable*  
695 *Energy Reviews* **2015**, *47*, 1016 – 1033. Available online: [http://www.sciencedirect.com/science/article/  
696 pii/S1364032115002154](http://www.sciencedirect.com/science/article/pii/S1364032115002154) (accessed 13.07.2018), doi:<https://doi.org/10.1016/j.rser.2015.03.062>.
- 697 4. Henley, J. From the Walkie Talkie to the Death Ray Hotel: Buildings turn up the heat. *The Guardian*, 3  
698 *September 2013*. Available online: [https://www.theguardian.com/artanddesign/shortcuts/2013/sep/03/  
699 walkie-talkie-death-ray-buildings-heat](https://www.theguardian.com/artanddesign/shortcuts/2013/sep/03/walkie-talkie-death-ray-buildings-heat) (accessed 12.07.2018).
- 700 5. Burbank, L. L.A.'s Disney Hall Shines – A Bit Too Brightly. National Public Radio Inc., 2005. Available  
701 online: <https://www.npr.org/templates/story/story.php?storyId=4541963> (accessed 12.07.2018).
- 702 6. Hayward, M. Airport controllers complain of solar panels' glare. *New Hampshire Union Leader*, 30 August  
703 *2012*. Available online: <http://www.unionleader.com/article/20120830/NEWS02/708309966> (accessed  
704 12.07.2018).
- 705 7. Bohren, A. Blendung von Solaranlagen: Übersicht zur aktuellen Rechtslage. Proceedings Symposium  
706 Thermische Solarenergie; OTTI: Bad Staffelstein, Germany, 2015. Available online: [http://www.spf.ch/  
707 fileadmin/daten/publ/Bohren\\_Blendung.pdf](http://www.spf.ch/fileadmin/daten/publ/Bohren_Blendung.pdf) (accessed 12.07.2018).
- 708 8. 20min.ch. Solaranlage darf Nachbarn blenden. *20 Minuten*, 7 March 2012. Available online: [http://www.  
709 20min.ch/schweiz/news/story/Solaranlage-darf-Nachbarn-blenden-20629849](http://www.20min.ch/schweiz/news/story/Solaranlage-darf-Nachbarn-blenden-20629849) (accessed 12.07.2018).
- 710 9. Battaglia, G. Grauer Star wegen Solarpanel. *Blick*, 15 May 2017. Available  
711 online: [https://www.blick.ch/news/schweiz/geblendet-von-nachbarin-marlis-lauffer-traut-sich-bei-  
712 schoenem-wetter-kaum-noch-in-den-garten-grauer-star-wegen-solarpanel-id6663759.html](https://www.blick.ch/news/schweiz/geblendet-von-nachbarin-marlis-lauffer-traut-sich-bei-schoenem-wetter-kaum-noch-in-den-garten-grauer-star-wegen-solarpanel-id6663759.html) (accessed  
713 12.07.2018).
- 714 10. Bundesversammlung der Schweizerischen Eidgenossenschaft. Bundesgesetz über die Raumplanung  
715 (Raumplanungsgesetz) RPG; SR 700, 2018. Available online: [https://www.admin.ch/opc/de/classified-  
716 compilation/19790171/index.html](https://www.admin.ch/opc/de/classified-compilation/19790171/index.html) (accessed 6.03.2018).
- 717 11. Der Schweizerische Bundesrat. Raumplanungsverordnung RPV; SR700.1, 2016. Available online: [https://  
718 www.admin.ch/opc/de/classified-compilation/20000959/index.html](https://www.admin.ch/opc/de/classified-compilation/20000959/index.html) (accessed 6.03.2018).
- 719 12. Reichenbach, A.; Baumann, J.; Hofmann, D.; Nötzli, J.; Vonlanthen, J.; Wyss-Käppeli, B. Vollzugshilfe  
720 Lichtemissionen. Technical Report P282-1581, Bundesamt für Umwelt BAFU, 2017. Available  
721 online: [https://www.bafu.admin.ch/bafu/de/home/themen/elektrosmog/fachinformationen/  
722 lichtemissionen--lichtverschmutzung-/konsultation-vollzugshilfe-lichtemissionen.html](https://www.bafu.admin.ch/bafu/de/home/themen/elektrosmog/fachinformationen/lichtemissionen--lichtverschmutzung-/konsultation-vollzugshilfe-lichtemissionen.html) (accessed  
723 28.03.2018).
- 724 13. LAI. Hinweise zur Messung, Beurteilung und Minderung von Lichtimmissionen. Technical report,  
725 Bund/Länder-Arbeitsgemeinschaft für Immissionsschutz (LAI), Potsdam, Germany, 2015. Available online:  
726 [https://www.lai-immissionsschutz.de/documents/hinweise\\_1503575680.pdf](https://www.lai-immissionsschutz.de/documents/hinweise_1503575680.pdf) (accessed 26.01.2018).
- 727 14. Stichelberger, D.; Moll, C. Leitfaden Solaranlagen. Technical report, Swissolar, Schweizerischer  
728 Fachverband für Sonnenenergie, Zürich, 2017. Available online: [http://www.swissolar.ch/fileadmin/  
729 user\\_upload/Shop/170707\\_Leitfaden\\_RPG\\_Langfassung.pdf](http://www.swissolar.ch/fileadmin/user_upload/Shop/170707_Leitfaden_RPG_Langfassung.pdf) (accessed 26.01.2018).
- 730 15. Ho, C.K.; Ghanbari, C.M.; Diver, R.B. Hazard Analyses of Glint and Glare from Concentrating  
731 Solar Power Plants. Proceedings of SolarPACES; AIP: Berlin, 2009. Available online:  
732 [https://www.semanticscholar.org/paper/Hazard-Analyses-of-Glint-and-Glare-from-Solar-Power-Ho-  
733 Ghanbari/dcf8c285917f8b46cff00b0be425481c767deb57](https://www.semanticscholar.org/paper/Hazard-Analyses-of-Glint-and-Glare-from-Solar-Power-Ho-Ghanbari/dcf8c285917f8b46cff00b0be425481c767deb57) (accessed 27.03.2018).
- 734 16. Larson, G.W.; Shakespeare, R. *Rendering With Radiance: The Art And Science Of Lighting Visualization*;  
735 Booksurge Llc, 2004.

- 736 17. Rose, T.; Wollert, A. The dark side of photovoltaic – 3D simulation of glare assessing risk  
737 and discomfort. *Environmental Impact Assessment Review* **2015**, *52*, 24 – 30. Available  
738 online: <http://www.sciencedirect.com/science/article/pii/S0195925514000730> (accessed 23.03.2018),  
739 doi:<https://doi.org/10.1016/j.eiar.2014.08.005>.
- 740 18. Sandia National Laboratories. Solar Glare Hazard Analysis Tool (SGHAT), 2017. Available online:  
741 <https://share.sandia.gov/phlux> (accessed 27.03.2018).
- 742 19. Sims Industries. GlareGauge – Comprehensive Solar Glare Analysis, 2018. Available online: <https://www.forgesolar.com/tools/glaregauge/>  
743 (accessed 27.03.2018).
- 744 20. Yang, X.; Grobe, L.; Wittkopf, S. Simulation of Reflected Daylight from Building Envelopes. Proceedings  
745 Building Simulation 2013; IBPSA: Chambeéry, France, 2013. Available online: [http://www.ibpsa.org/proceedings/BS2013/p\\_1232.pdf](http://www.ibpsa.org/proceedings/BS2013/p_1232.pdf)  
746 (accessed 6.03.2018).
- 747 21. Schregle, R. Development and Integration of the RADIANCE Photon Map Extension.  
748 Technical report, Lucerne University of Applied Sciences and Arts, 2015. Available  
749 online: [https://www.researchgate.net/publication/272497518\\_Development\\_and\\_Integration\\_of\\_the\\_](https://www.researchgate.net/publication/272497518_Development_and_Integration_of_the_RADIANCE_Photon_Map_Extension_v112)  
750 [RADIANCE\\_Photon\\_Map\\_Extension\\_v112](https://www.researchgate.net/publication/272497518_Development_and_Integration_of_the_RADIANCE_Photon_Map_Extension_v112) (accessed 27.03.2018, doi:10.13140/2.1.3332.9449).
- 751 22. Kunz, G. *Kirchen in Luzern*; Baukultur entdecken, Innerschweizer Heimatschutz (IHS), 2009.
- 752 23. Kanton Luzern. Geodaten-Portal, 2018. Available online: <https://geoportail.lu.ch/geodaten> (accessed  
753 16.05.2018).
- 754 24. Grobe, L.O.; Wittkopf, S.; Kazanasmaz, Z.T. High-resolution data-driven models of Daylight Redirection  
755 Components. *Journal of Façade Design and Engineering* **2017**, *5*, 101–113. Available online: <http://ojs-lib.tudelft.nl/index.php/jfde/article/view/1743>  
756 (accessed 27.03.2018), doi:10.7480/jfde.2017.2.1743.
- 757 25. Ward, G.; Kurt, M.; Bonneel, N. Reducing Anisotropic BSDF Measurement to Common Practice.  
758 Proceedings of the Eurographics 2014 Workshop on Material Appearance Modeling: Issues and Acquisition;  
759 Eurographics Association: Aire-la-Ville, Switzerland, 2014; MAM '14, pp. 5–8. Available online:  
760 <http://dl.acm.org/citation.cfm?id=2855560.2855562> (accessed 27.03.2018).
- 761 26. Schregle, R.; Grobe, L.; Wittkopf, S. An out-of-core photon mapping approach to daylight coefficients.  
762 *Journal of Building Performance Simulation* **2016**, *9*, 620–632. Available online: <https://www.tandfonline.com/doi/full/10.1080/19401493.2016.1177116>  
763 (accessed 27.03.2018), doi:10.1080/19401493.2016.1177116.
- 764 27. Schregle, R. The RADIANCE Photon Map Manual, 2016. Available online: [https://www.researchgate.net/publication/303406111\\_The\\_RADIANCE\\_Photon\\_Map\\_Manual](https://www.researchgate.net/publication/303406111_The_RADIANCE_Photon_Map_Manual)  
765 (accessed 16.05.2018), doi:10.13140/RG.2.1.4330.8405.
- 766
- 767 28. Jones, E.; Oliphant, T.; Peterson, P.; et al. SciPy: Open source scientific tools for Python, 2001–. Available  
768 online: <http://www.scipy.org/> (accessed 14.05.2018).