

Article

Magnetoresistance, Gating and Proximity Effects in Ultrathin NbN-Bi₂Se₃ Bilayers

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Abstract: Ultrathin Bi₂Se₃-NbN bilayers comprise a simple proximity system of a topological insulator and an s-wave superconductor for studying gating effects on topological superconductors. Here we report on 3 nm thick NbN layers of weakly connected superconducting islands, overlaid with 10 nm thick Bi₂Se₃ film which facilitates enhanced proximity coupling between them. Resistance versus temperature of the most resistive bilayers shows insulating behavior but with signs of superconductivity. We measured the magnetoresistance (MR) of these bilayers versus temperature with and without a magnetic field H normal to the wafer ($MR=[R(H)-R(0)]/([R(H)+R(0)]/2)$), and under three electric gate-fields of 0 and ± 2 MV/cm. The MR results showed a complex set of gate sensitive peaks which extended up to about 30 K. The results are discussed in terms of vortex physics, and the origin of the different MR peaks is identified and attributed to flux-flow MR in the isolated NbN islands and the different proximity regions in the Bi₂Se₃ cap-layer. The dominant MR peak was found to be consistent with enhanced proximity induced superconductivity in the topological edge currents regions. The high temperature MR data suggest a possible pseudogap phase or a highly extended fluctuation regime.

Keywords: superconductivity; topological Insulator; thin films; bilayers; proximity effect; magnetoresistance

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1. Introduction

Surface edge states of topological superconductors (TOS) are expected to support zero energy modes or Majorana fermions which are robust against disorder and decoherence [1,2]. These zero energy excitations could therefore be useful in potential application in spintronics and quantum computing [3,4]. Bulk TOS such as copper doped Bi₂Se₃ should have been the simplest materials to study TOS properties, but complications due to their inherent inhomogeneity [5] and the presence of possible superconducting impurity phases such as CuSe₂ [6], make them less attractive for such investigations. Recently however, bulk superconducting PbTaSe₂ with T_c of 3.8 K was found to have zero energy states at vortices which is a hallmark of TOS [7]. An alternative way for realizing TOS is by inducing superconductivity in a topological insulator or in semiconductor-nanowires with strong spin-orbit interaction via the proximity effect (PE) [8–11]. Unconventional superconductivity in these systems, such as revealed by the presence of zero bias conductance peaks (ZBCP), indicates zero energy bound states that might be due to Majorana zero energy modes, but could also originate in zero energy Andreev bound states in an unconventional superconductor. It is hard to distinguish between these two different phenomena, and efforts are ongoing in order to achieve this goal [12,13].

Spatial sharpness of the boundary region between the superconductor and the topological or semi-conducting material is also essential in order to distinguish between the near-zero-energy end states originating in Andreev bound states, and the Majorana zero energy modes in the topological case [14]. Since this boundary is generally created by gating in the experiments, its unavoidable gradual spatial change adds more uncertainty to the interpretation of the observed ZBCPs as due to the Majorana modes [10,11,15]. The role of gating in these nanowire-superconductor experiments was further investigated and a variety of additional phenomena such as ZBCP oscillations versus gate voltage and magnetic field were observed and interpreted in the context of Majorana modes as well as alternatives such as Kondo and disorder effects [16]. Hence, gating is sufficiently important in these studies and we decided to use a simple proximity system of a bilayer comprising of a topological insulator and a 2D superconductor for studying gating effects on topological superconductors [17]. In continuation to our previous studies of $Bi_2Se_3 - NbN$ junctions [18,19] we used ultra-thin bilayers of this system, even thinner than used before [17], where the superconducting NbN islands with weak-links in between them are overlaid with a thicker Bi_2Se_3 layer which enhances the coupling between the NbN islands via the proximity effect. Here we report on gating effects on the magnetoresistance (MR) of this hybrid system, which shows a highly gate sensitive, non-monotonous behavior versus temperature.

51

52 2. Experimental

53 2.1. choice of the bilayer parameters

Here we explain why a highly resistive 10 nm thick Bi_2Se_3 on 3 nm thick NbN bilayer was chosen for presentation. It turned out that the R and MR results of similar but less resistive bilayers, showed that the MR above T_c was very similar to that of a bare 10 nm Bi_2Se_3 film (see Figure S2 of the supplementary material [20]). This was a direct result from the fact that the links between superconducting islands of the 3 nm reference NbN film were still too strong, as is obvious from the almost full transition to zero resistance at low temperatures in Figure S1. We therefore had to weaken the inter-grain links even more. Since the use of 2.5 nm thick NbN films on FS yielded very resistive films, with R over a M Ω at low temperatures, with a lot of noise and a very weak signature of a transition at 2-3 K, we decided to stick with the 3 nm thick films in the bilayers. We thus prepared and characterized 7 wafers with the 10 nm Bi_2Se_3 on 3 nm NbN bilayers, and found out that their maximum resistance (at low temperatures) varied between about 1 and 10 k Ω . This depended mostly on the base pressure used before the deposition process ($1.5-3 \times 10^{-7}$ Torr), but probably also on the surface quality of the FS wafers. In any case, the most significant results were obtained with the highest resistance bilayers, and here we present the results on the most resistive one, which also has the weakest links as we originally planned to have.

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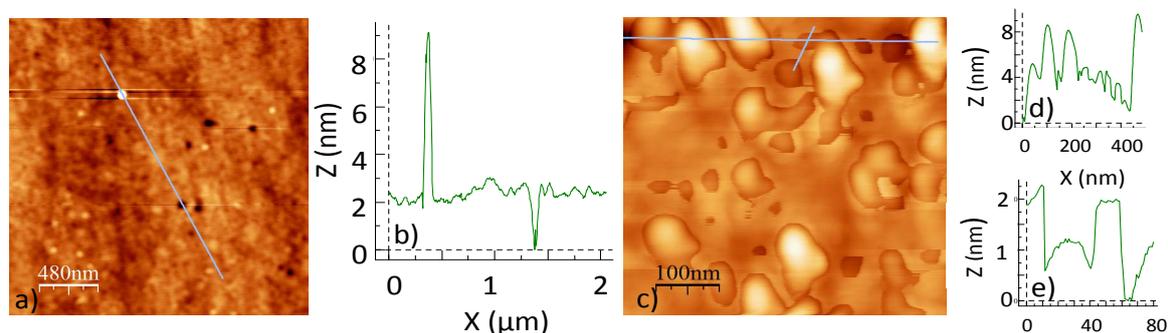


Figure 1. Atomic force microscope (AFM) images and line height profiles. **a)** Image of nominally 3 nm thick NbN layer. **b)** A line height profile along the line shown in **a)**. **c)** Image of a 10 nm Bi_2Se_3 on a 3 nm NbN bilayer. **d)** and **e)** are two line height profiles along the long and short lines shown in **c)**, respectively.

71 Figure 1 **a)** shows an atomic force microscope (AFM) image of the surface morphology of a 3
 72 nm thick NbN film. A typical line height profile is shown in **b)** along the line in **a)**. While the lateral
 73 size of the NbN grains is ~ 50 -100 nm, one can see larger bright areas of at least 1000 nm in size
 74 which represent thicker superconducting NbN islands. These are separated by broad darker areas
 75 which constitute thinner weak-links between these islands. This islands structure that comprises
 76 a network of strong superconducting regions connected by weak-links is essential for the present
 77 study, otherwise a superconducting short will mask all our transport data. SEM images of similar
 78 NbN films on glass showing their grainy nature can also be seen in [21]. In addition, Figure 1 **a)**
 79 shows a few 1-3 nm deep holes of about 60 nm diameter while the overall rms roughness of this film
 80 is ~ 0.35 nm.

81

82 Figure 1 **c)** shows an AFM image of the surface morphology of a 10 nm Bi_2Se_3 on a 3 nm NbN
 83 bilayer bilayer, together with two line height profiles in **d)** and **e)** along the long and short lines
 84 shown in **c)**, respectively. The bilayer shows taller grains on a smoother background, with grains
 85 height of 4-8 nm and some holes, the deepest of which is of about 5 nm deep. Shallower holes are
 86 also visible which reveal a step-like depth profile as seen in **(e)**, where the step heights are of about 1
 87 or 2 nm in agreement with one or two quintuples of the Bi_2Se_3 structure. The overall rms roughness
 88 of this bilayer is ~ 1.1 nm.

89

90 2.3.

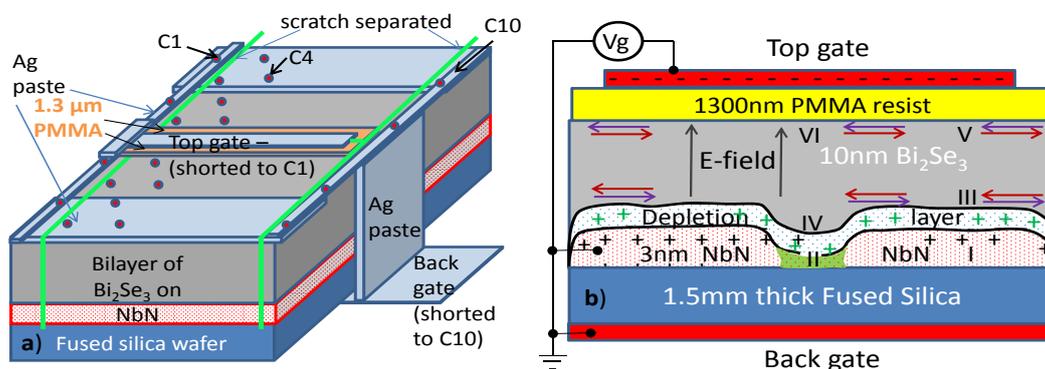


Figure 2. a) A schematic drawing of the Bi_2Se_3 on NbN bilayer, together with the top and bottom gates and some of the C_i contacts where $i=1$ to 10 (each C_i has 4-point contacts, the red dots along the y -direction). The $C1$ and $C10$ contacts are separated from the bilayer and dedicated for contacting the top and bottom gates, respectively. b) A schematic model cross-section of the bilayer and gates. Two superconducting NbN islands, marked by the red-dots area, are weakly connected by the non-superconducting green shaded area. Helical edge currents for the two spin orientations of the Bi_2Se_3 layer are depicted by the horizontal arrows on the top and bottom surfaces. The depletion layer in the Bi_2Se_3 is marked by the blue-dots area. The back gate is grounded and shorted to the bilayer in the present study, and a negative top gate voltage $-V_g$ corresponds to a positive electric field E .

91 Figure 2 a) depicts a schematic drawing of the bilayer, gates positions and 20 representative
 92 contacts. Contacts $C1$ and $C10$ are separated from the bilayer by two scratches, while the 4 contacts
 93 of each are shorted and connected to the top and bottom gates, respectively. Since the fused silica
 94 substrate is 1.5 mm thick and its dielectric constant is low, the bottom gate is useless here and is
 95 shorted to the bilayer and ground, as can be seen in the schematic cross-section of the bilayer and
 96 gates in Figure 2 b). The insulation layer of the top gate is made of a much thinner PMMA resist of
 97 $1.3 \mu\text{m}$ thickness. This allows for an electric field of $\pm 2 \text{ MV/cm}$ to be obtained when a voltage of
 98 $\mp 100 \text{ V}$ is applied to the top gate (opposite polarity). This will be marked in the following by ∓ 100
 99 V_g . Figure 2 b) shows two weakly connected NbN islands (red dots) together with their depletion
 100 layer (blue dots on white background) in the Bi_2Se_3 layer near the interface with the NbN islands.
 101 Proximity induced superconductivity also occurs in this layer and can extend up to the top surface
 102 of the Bi_2Se_3 film [17].

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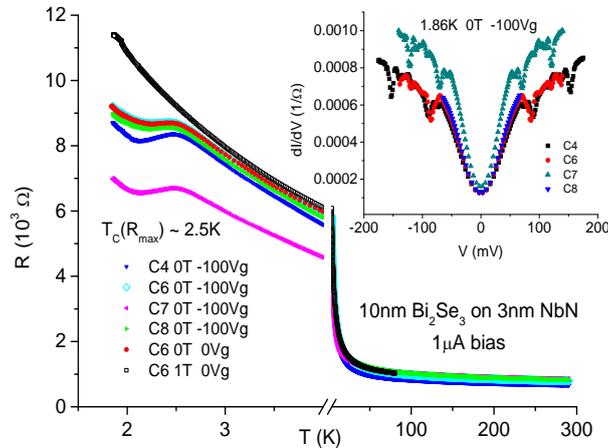
104 **3. Results and discussion**

Figure 3. Resistance versus temperature of a pristine 10 nm Bi_2Se_3 on 3 nm NbN on FS bilayer under different magnetic fields and gate voltages. The inset shows conductance spectra of this highly resistive bilayer at 1.86 K, 0 T and -100 Vg.

105 Figure 3 shows the resistance versus temperature of the 10 nm Bi_2Se_3 on 3 nm NbN on FS
 106 bilayer with the highest resistance at low temperatures. The temperature dependence of R clearly
 107 shows insulating behavior down to 2.5 K where a small decrease of resistance is observed. Similar
 108 behavior was observed also in 5 nm thin cuprate films [22]. We show data at four locations on the
 109 wafer which exhibits quite a spread, and also the data of contact C6 at 0 and 1 T magnetic field under
 110 0 Vg. Clearly, the small decrease of R below 2.5 K disappears under 1 T, and we thus conclude that
 111 it originates in superconductivity of the NbN islands which are very weakly linked. The inset shows
 112 conductance spectra of all these contacts at 1.86 K which clearly exhibit tunneling behavior between
 113 the superconducting islands. The gap-like feature appearing at about 70 meV, is a result of several
 114 weak-links connected in series between the voltage contacts. Assuming an energy gap Δ of 2 meV for
 115 the NbN islands [23] yields 35 such weak-links in series. The dips in the conductance spectra of the
 116 inset are due to heating effects as a result of reaching the critical current in the weak-links connecting
 117 the NbN islands [24].

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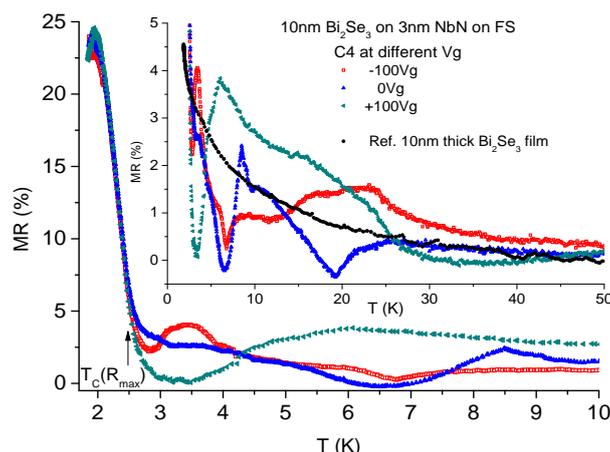


Figure 4. Magnetoresistance versus temperature of the C4 contact of the pristine bilayer of Figure 3, obtained for 0 and 1 T fields and under gate voltages of 0 and ± 100 Vg. All other contacts show similar behavior. The inset shows the full temperature range while the main panel is a zoom in on the low temperature regime. The inset also shows the MR of the reference 10 nm thick Bi_2Se_3 film of Figure S2 [20].

119 The main results of this study are presented in Figure 4 and its inset, where the MR of the bilayer
 120 of Figure 3 for 0 and 1 T and under different gate voltages shows a complex, non monotonous peaks
 121 structure. For comparison, the corresponding monotonous MR of the reference 10 nm Bi_2Se_3 film
 122 of Figure S2 is also shown [20]. Below 2.5 K, the MR is similar to the results in the inset to Figure
 123 S1 [20], but with a 3-5 times smaller signal at the maximum MR at ~ 1.9 K. The later reflects the fact
 124 that the weak-links here are much weaker than in Figure S1. There is also no visible effect of the gate
 125 voltage on the MR results in this regime. Above 2.5 K, the MR data becomes very sensitive to the gate
 126 voltage, and up to 7-8 K exhibit kind of anti-phase behavior versus temperature for ± 100 Vg where
 127 the peak and dip at 3.5 K reverse roles at 6-7 K. The MR under 0 Vg is somewhere in between these
 128 two at 3.5 K, but then becomes closer to the -100 Vg data at 6-7 K. At higher temperatures the MR
 129 data becomes even more complex, but clearly it goes down at 25-30 K, where it tends to follow the
 130 reference Bi_2Se_3 film. It should be stressed here that the MR behavior of Figure 4 for the C4 contact,
 131 was observed also for the other contacts on this wafer (C6 and C8), while C7 had an additional strong
 132 oscillatory behavior above 10 K as shown in Figure 5 for 0 Vg. This oscillatory behavior was washed
 133 out under ± 100 Vg. The inset to Figure 5 is a zoom-in on weaker oscillations or plateaus in the MR of
 134 C7 in the range of 3-8 K. Such plateaus and knees, although weaker, appear also in the other contacts.
 135 As far as we know, there is no theory that predicts oscillations of MR versus temperature in a 2D
 136 topological superconductor.

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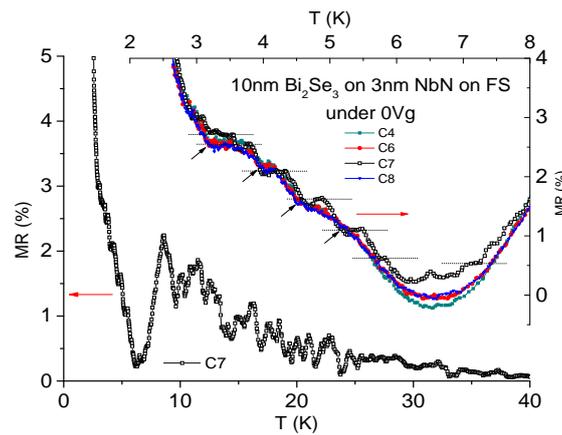


Figure 5. MR versus temperature at 0Vg of the C7 contact on the wafer of Figure 3. The oscillations were smeared out under ± 100 Vg. The inset is a zoom in on the data at low temperatures. Only this C7 contact showed the pronounced oscillations versus temperature, although plateaus and less pronounced knees were observed also in the other contacts as seen in the inset and marked by the arrows.

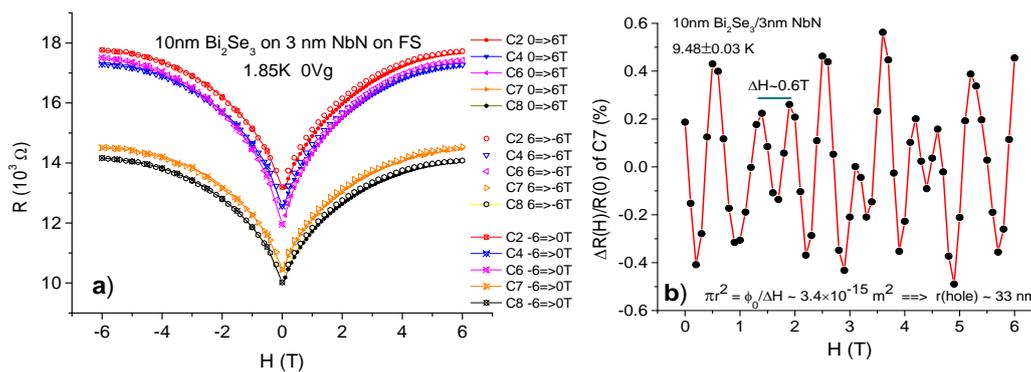


Figure 6. a) Resistance versus magnetic field of the bilayer of Figure 3 at 1.85 K and 0 Vg. Although this bilayer was kept in dry air for one month prior to this measurement, it deteriorated (aged) as can be seen from the increase of its resistance values at 0 T by about 4 k Ω as compared to Figure 3. b) Oscillations of normalized R minus background $[\Delta R(H)/R(0)]$ of the C7 contact of Figure 5 versus magnetic field at 9.48 K and 0 Vg.

138 To find out whether these oscillations and plateaus originate in magnetic field effects, we
 139 measured R versus H for all the contacts on the wafer of Figure 3 at 1.85 K. The results are depicted
 140 in Figure 6 a), and they are quite similar to those of the inset to Figure S2 [20], besides the difference
 141 in overall resistance and aging effects. We have also measured R versus H under 0 Vg on this wafer
 142 (when it was 1.5 month old) at higher temperatures. A background of a polynomial of order 2 fit
 143 to the data was subtracted from the data, and the resulting resistance variation ΔR versus H
 144 was obtained. The normalized $\Delta R(H)/R(0)$ results at ~ 9.5 K are plotted in Figure 6 b) versus magnetic
 145 field. Presuming that the observed oscillations originate in flux quantization in nano-holes in the
 146 bilayer, we obtain from the period $\Delta H \sim 0.6$ T a hole diameter of 66 nm, which agrees quite well
 147 with the AFM image and line profile of the 3 nm thick NbN film of Figure 1 a) and b). This result
 148 suggests that superconductivity in the bilayer persists at least up to ~ 9.5 K. Similar oscillations were
 149 observed also in the other contacts at 3.7 and 5.3 K, but they disappeared at 15.1 K in the noise level
 150 of the measurements. Thus T_c of the NbN islands in this bilayer should be between 9.5 and 15.1 K.
 151 This is in agreement with the the MR onset in Figure S6 under 4 T (12.2 K) [20], or the temperatures

152 of maximum resistance of Figure S5 (12-13 K) [20], although in that case the NbN film was 4 nm
153 thick and not 3 nm thick as in the present bilayer. We conclude from these findings that T_c of the
154 superconducting islands in our bilayer can reach 12-13 K, and that if fluctuations are taken into
155 account, superconductivity could persist in our bilayers up to ~ 15 K. Thus, it should be possible to
156 observe flux-flow effects of vortices up to this temperature, but this however, does not explain the
157 non monotonous MR features observed in Figures 4 and 5. Above 15 K, any MR effect different from
158 that due to the reference 10 nm Bi_2Se_3 film, should have a different origin.

159
160 Next, we discuss possible explanations for the complex behavior of the MR results of Figure
161 4. In principle, the present bilayer as drawn schematically in Figure 2 b), comprises of six distinct
162 superconducting regions, marked in this figure by I to VI. The NbN islands (I) and the inter-islands
163 regions (II) are the obvious ones, but proximity induced superconductivity occurs also in the Bi_2Se_3
164 layer above these regions, in particular, at the bottom and top surfaces of this doped topological layer
165 where the helical edge currents flow. This yields four more superconductive regions in the cap Bi_2Se_3
166 layer, two above the islands (III and V) and two above the inter-islands regions (IV and VI). Due
167 to proximity effect and distances from the superconducting NbN islands (I), we can safely assume
168 that $T_c(I) > T_c(III) > T_c(II) > T_c(IV)$. We shall assume first that the MR results observed in Figure 4
169 originates in vortex physics, and discuss them in terms of pinning in the different superconducting
170 regimes I-VI. Then, for the remaining unidentified features, we shall discuss possible contributions
171 to the MR from zero energy Majorana modes and unconventional superconductivity.

172
173 In the context of vortex physics, the MR peaks seen in Figure 4 as a function of temperature
174 originate in flux-flow, and are due to two competing phenomena. One is the increased vortex
175 generation on cooling down due to newly formed proximity induced superconducting areas in the
176 bilayer which eventually saturates, and the other is increased pinning with decreasing temperature.
177 The result of these effects is an MR peak versus temperature below which all vortex motion stops
178 and the MR goes to zero. Such MR peaks have been clearly observed in similar cuprate bilayers
179 [25], as well as in the inset to Figure S1 [20]. Since the bottom Bi_2Se_3 surface of regions III and
180 IV are very close to regions I and II, the proximity induced superconductivity in them is stronger
181 than in the more distant regions V and VI. We shall first discuss the MR versus T result of Figure 4
182 under 0 Vg. The MR of this data is most always lower than that of the reference Bi_2Se_3 film. This
183 looks like MR suppression in the bilayer, but since there are zero MR regimes in the bilayer data (at
184 6-7 and 18-20 K), it looks more like an indication of strongly interacting layers in the bilayer. This
185 interaction seems to play a lesser role only above 25 K where the two curves coincide, apparently
186 because no superconductivity affects the MR results at this high temperature range. We attribute the
187 double MR peak between 7-15 K to flux flow, vortex generation and pinning in regions I and III. We
188 note here that the above analysis was facilitated by the fact that this double peak is fully separated
189 from the other features of the MR curve. Using similar arguments, we can attribute the broad MR
190 knee between 2.5 and 6.5 K to pinning in regions II, and the large MR peak below 2.5 K to pinning
191 effects in region IV. The fact that the MR peak below 2.5 K is so strong might be due to enhance
192 proximity induced superconductivity by the surface currents of the topological layer in region IV, or
193 to additional contributions from other effects, to be discussed below.

194
195 We shall now analyze the MR results of Figure 4 under different gate voltages and try to
196 explain the two prominent peaks at 3.5 and 6 K under -100 Vg and +100 Vg, respectively. We
197 note that transport, and therefore also the MR data, is strongly dependent on the conductance of
198 regions II and IV, since they comprise the weak-links for current flow in the bilayer. As a result,
199 they will be more sensitive to gating than region III. Under -100 Vg, the depletion layer in Figure
200 2 b) in between the NbN islands (region II), is positively charged or simply electron depleted.
201 This makes region II, (as well as the adjacent region IV just above it), less conducting (or more

202 insulating), thus lowering its T_c onset to about 4 K compared to its value without gating (onset at
203 ~ 6.5 K). The MR peak at 3.5 K under -100 Vg is consistent with this scenario, and therefore seems
204 to originate in region II. The large MR peak at 1.9 K seems to be unaffected by either of the present
205 gate voltages of ± 100 Vg, and this again might originate in topological effects in region IV. Under
206 +100 Vg, the depletion layer is electron rich (more conducting), thus its proximity induced T_c in
207 region II is higher than the 4 K obtain before under -100 Vg. The MR peak at 6 K under +100 Vg
208 can thus originate also in region II. Besides the two prominent peaks at 3.5 and 6 K, additional
209 MR features under gating can be seen in Figure 4. These include the broad hump under +100
210 Vg between 10 and 25 K, and the broad peak between 15 and 30 K under -100 Vg. As discussed
211 before, superconductivity dies off at about 15 K, and any proximity induced T_c will obviously be
212 lower. Therefore, if one wishes to invoke vortex motion as the origin of these extra MR features,
213 one has to assume the existence of a pseudogap phase for the present bilayers. Signature of such a
214 phase was found in point contact conductance spectra measurements of copper doped $Cu_{0.2}Bi_2Se_3$
215 single crystals with $T_c \sim 3$ K, where a depletion of density of states at low bias was observed
216 up to ~ 20 K [26]. Considering that in the present bilayers the NbN islands have a much higher
217 $T_c \sim 12$ -13 K, the conjectured pseudogap phase could easily reach 25-30 K. Hence, to summarize,
218 the extra MR features in Figure 4 above 15 K could originate in flux flow, provided a pseudogap
219 phase exists in our system. In the cuprates, where the pseudogap phase is well established, such
220 vortices were detected in thermoelectric measurements under a magnetic field (the Nernst effect) [27].

221
222 Finally, we focus on the intensity or magnitude of the MR peaks in Figure 4, and on what might
223 contribute extra strength to the dominant peak at 1.9 K. We note that the volume fraction of the
224 superconducting NbN islands with the highest T_c values is apparently very small, as can be inferred
225 from the very small resistive transition at 2.5 K in Figure 3. Previously, in the vortex pinning context,
226 we attributed the MR double peak under 0 Vg at 7-15 K to regions I and III, the knee between 2.5
227 and 6.5 K to region II, and the large MR peak below 2.5 K to region IV. It was hard to reconcile how
228 region IV, with its presumably weakest superconductivity, leads to such a large MR peak. Thus, if the
229 enhanced MR peak at 1.9 K is still due to pinning effects, we are led to the conclusion that region IV
230 must have enhanced superconductivity just as well. Such enhancement might originate in a longer
231 normal coherence length ξ_N in the Bi_2Se_3 at low temperatures, which is possibly enhanced further
232 by hybridization of the helical surface currents of regions IV and VI. We know of no theory that
233 predicts such effects, and therefore this interpretation is only a hypothesis at the present time. An
234 alternative scenario for the interpretation of our results is that the MR knee between 2.5 and 6.5 K is
235 due to pinning effects in both region II and region IV. This would leave the dominant MR peak at 1.9
236 K unaccounted for, and other effects as for its origin should be explored. But this time, vortices in the
237 bilayer are fully pinned and presumably form a vortex lattice. Vortices in general, in a topological
238 superconductor, are predicted to host zero energy Majorana modes in the vortex cores [2]. Thus, in
239 a dense periodic vortex lattice, interactions between these modes lead to the creation of new energy
240 bands in the band gap of this system, some of which could be quite flat [28]. Whether or not these
241 Majorana bands contribute to the MR of the bilayer is unknown at the present time. Rigorous MR
242 calculation versus temperature are needed in order to test if this scenario actually occurs in the
243 present bilayers.

245 4. Materials and Methods

246 The NbN and Bi_2Se_3 thin films were prepared as described in detail previously [17]. Briefly,
247 laser ablation deposition was used where the NbN films were deposited under 30 mTorr of N_2 gas
248 flow and at 600 $^{\circ}C$ heater block temperature, while the Bi_2Se_3 layers were deposited under vacuum
249 and at 300 $^{\circ}C$. All films and bilayers were deposited on fused silica wafers and yielded grainy films
250 with rms roughness of $\sim 10\%$ of the films thickness. All the $Bi_2Se_3 - NbN$ bilayers in the present

study were obtained using an "in-situ" process where both the 3 nm thick NbN film and the 10 nm thick Bi_2Se_3 cap layer were prepared in the same deposition run without breaking the vacuum. This kept the interface between the NbN and Bi_2Se_3 layers protected against contamination and oxidation which occur if the NbN surface is exposed to air [17,29]. Transport measurements were done using an array of 40 gold coated spring loaded spherical tips for the 4-probe measurements on 10 different locations on the wafer (Ci with $i=1$ to 10, 4 contacts for each location).

5. Conclusions

A comprehensive study of ultra thin bilayers comprising of weakly connected s-wave superconducting islands and a continuous topological insulator cap-layer reveal interesting gate and temperature dependent magnetoresistance features. These features could be explained as originating in vortex physics, where proximity induced superconductivity and pinning effects in the different regions of the bilayer play a major role. In particular, the present results are consistent with enhanced superconductivity in the surface region of the topological layer in contact with the superconductor, where the helical edge currents flow. Signature of a pseudogap was found, and a possible contribution to the data from Majorana bands was discussed.

Supplementary Materials: Supplementary material is available online at www.mdpi.com/link.

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Conflicts of Interest: The author declare no conflict of interest.

References

1. Hassan, M. Z.; Kane, C. L. Colloquium: Topological insulators. *Rev. Mod. Phys.* **2010** *82*, 3045-3067.
2. Fu, Liang; Kane, C. L. Superconducting Proximity Effect and Majorana Fermions at the Surface of a Topological Insulator. *Phys. Rev. Lett.* **2008** *100*, 096407.
3. Pesin, D.; MacDonald, A. H. Spintronics and pseudospintronics in graphene and topological insulators. *Nat. Mater.* **2012** *11*, 409-416.
4. Bravyi, S. B.; Kitaev, A. Yu. Fermionic quantum computation. *Annals of Physics* **2002** *298*, 210-226.
5. Kriener, M.; Segawa, K.; Ren, Zhi; Sasaki, S.; Wada, S.; Kuwabata, S.; Ando, Y. Electrochemical synthesis and superconducting phase diagram of $Cu_xBi_2Se_3$. *Phys. Rev. B* **2011** *84*, 054513.
6. Ando, Y. Topological insulator materials. *J. Phys. Soc. Jpn.* **2013** *82*, 102001.
7. Guan, Syu-You.; Chen, Peng-Jen.; Chu, Ming-Wen.; Sankar, R.; Chu, F.; Jeng, H. T.; Chang, C. S.; Chuang, T. M. Superconducting topological surface states in the noncentrosymmetric bulk superconductor $PbTaSe_2$. *Sci. Adv.* **2016** *2*, e1600894-1-8.
8. Koren, G.; Kirzhner, T.; Lahoud, E.; Chashka, K. B.; Kanigel, A. Proximity induced superconductivity by Bi in topological Bi_2Te_2Se and Bi_2Se_3 films: Evidence for a robust zero energy bound state that could be due to Majorana Fermions. *Phys. Rev. B* **2011** *84*, 224521.
9. Yang, Fan.; Ding, Y.; Qu, F.; Shen, J.; Chen, Jun.; Wei, Z.; Ji, Z.; Liu, G.; Fan, J.; Yang, C.; Xiang, T.; Lu, Li. Proximity effect at superconducting $Sn - Bi_2Se_3$ interface. *Phys. Rev. B* **2012** *85*, 104508.
10. Mourik, V.; Zuo, K.; Frolov, S. M.; Plissard, S. R.; Bakkers, E. P. A. M.; Kouwenhoven, L. P. Signatures of Majorana fermions in hybrid superconductor-semiconductor nanowire devices. *Science* **2012** *336*, 1003.
11. Das, A.; Ronen, Y.; Most, Y.; Oreg, Y.; Heiblum, M.; Shtrikman, H. Zero-bias peaks and splitting in an Al-InAs nanowire topological superconductor as a signature of Majorana fermions. *Nature Phys.* **2012** *8*, 887-895.
12. Xu, Jin-Peng.; Liu, C.; Wang, M. X.; Ge, V.; Liu, Z. L.; Yang, X.; Chen, Yan.; Liu, Ying.; Xu, Z. A.; Gao, C. L.; Qian, D.; Zhang, G. C.; Jia, J. F. Artificial topological superconductor by the proximity effect. *Phys. Rev. Lett.* **2014** *112*, 217001.
13. Haim, A.; Berg, E.; von Oppen, F.; Oreg, Y. Signatures of Majorana zero modes in spin-resolved current correlations. *Phys. Rev. Lett.* **2015** *114*, 166406.

- 298 14. Kells, G.; Meidan, D.; Brouwer, P. W. Near-zero-energy end states in topologically trivial spin-orbit coupled
299 superconducting nanowires with a smooth confinement. *Phys. Rev. B* **2012** *86*, 100503(R).
- 300 15. Higginbotham, A. P.; Albrecht, S. M.; Kirsanskas, G.; Chang, W.; Kueemeth, F.; Krogstrup, P.; Jespersen, T.
301 S.; Nygard, J.; Flensberg, K.; Marcus, C. M. Parity lifetime of bound states in a proximitized semiconductor
302 nanowire. *Nature Physics* **2015** *11*, 1017-1021.
- 303 16. Churchill, H. O. H.; Fatemi, V.; Grove-Rasmussen, K.; Deng, M. T.; Caroff, P.; Xu, H. Q.; Marcus, C. M.
304 Superconductor-nanowire devices from tunneling to the multichannel regime: Zero-bias oscillations and
305 magnetoconductance crossover. *Phys. Rev. B* **2013** *87*, 241401(R).
- 306 17. Koren, Gad. Proximity effects at the interface of a superconductor and a topological insulator in $NbN -$
307 Bi_2Se_3 thin film bilayers. *Supercond. Sci. Technol.* **2015** *28*, 025003.
- 308 18. Koren, G.; Kirzhner, T. Zero-energy bound states in tunneling conductance spectra at the interface of an
309 s-wave superconductor and a topological insulator in $NbN/Bi_2Se_3/Au$ thin-film junctions. *Phys. Rev. B*
310 **2012** *86*, 144508.
- 311 19. Koren, G.; Kirzhner, T.; Kalcheim, Y.; Millo, O. Signature of proximity-induced px + ipy triplet pairing in
312 the doped topological insulator Bi_2Se_3 by the s-wave superconductor NbN. *EPL* **2013** *103*, 67010.
- 313 20. Supplementary material is available online at www.mdpi.com/link.
- 314 21. Xin-kang, D.; Tian-min, W.; Cong, W.; Bu-liang, C.; Long, Z. Microstructure and Optical Characterization
315 of Magnetron Sputtered NbN Thin Films. *Chinese. J. Aero.* **2007** *20*, 140-144.
- 316 22. Koren, G.; Millo, O. Conventional proximity effect in bilayers of superconducting underdoped
317 $La_{1.88}Sr_{0.12}CuO_4$ islands coated with nonsuperconducting overdoped $La_{1.65}Sr_{0.35}CuO_4$. *Phys. Rev. B* **2009**
318 *80*, 054507.
- 319 23. Kamlapure, A.; Mondal, M.; Chand, M.; Mishra, A.; Jesudasan, J.; Bagwe, V.; Benfatto, L.; Tripathi, V.;
320 Raychaudhuri, P. Measurement of magnetic penetration depth and superconducting energy gap in very
321 thin epitaxial NbN films. *Appl. Phys. Lett.* **2010** *96*, 072509.
- 322 24. Sheet, G.; Mukhopadhyay, S.; Raychaudhuri, P. Role of critical current on the point-contact Andreev
323 reflection spectra between a normal metal and a superconductor. *Phys. Rev. B* **2004** *69*, 134507.
- 324 25. Koren, G.; Millo, O. Enhancement of the superconducting transition temperature of $La_{2-x}Sr_xCuO_4$ and
325 $La_{1.875}Ba_{0.125}CuO_4$ bilayers: Bilayer and reference film prepared on the same wafer. *Phys. Rev. B* **2010** *81*,
326 134516.
- 327 26. Kirzhner, T.; Lahoud, E.; Chaska, K. B.; Salman, Z.; Kanigel, A. *Phys. Rev. B* **2012** *86*, 064517.
- 328 27. Wang, Yayu.; Li, Lu.; Ong, N. P. Nernst effect in high- T_c superconductors. *Phys. Rev. B* **2006** *73*, 024510.
- 329 28. Liu, Tianyu.; Franz, M. Electronic structure of topological superconductors in the presence of a vortex
330 lattice. *Phys. Rev. B* **2015** *92*, 134519.
- 331 29. Darlinski, A.; Halbritter, J. Angle-resolved XPS Studies of Oxides at NbN, NbC, and Nb Surfaces *Surf.*
332 *Interface Anal.* **1987** *10*, 223-237.



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